The University of the State of New York
REGENTS HIGH SCHOOL EXAMINATION

GEOMETRY

Friday, August 17, 2018 — 12:30 to 3:30 p.m., only

Student Name: _____

School Name: _____

> **The possession or use of any communications device is strictly prohibited when taking this examination. If you have or use any communications device, no matter how briefly, your examination will be invalidated and no score will be calculated for you.**

Print your name and the name of your school on the lines above.

A separate answer sheet for **Part I** has been provided to you. Follow the instructions from the proctor for completing the student information on your answer sheet.

This examination has four parts, with a total of 35 questions. You must answer all questions in this examination. Record your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers to the questions in **Parts II, III,** and **IV** directly in this booklet. All work should be written in pen, except for graphs and drawings, which should be done in pencil. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale.

The formulas that you may need to answer some questions in this examination are found at the end of the examination. You may remove this sheet from this booklet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. You may remove this sheet from this booklet. Any work done on this sheet of scrap graph paper will *not* be scored.

When you have completed the examination, you must sign the statement printed at the end of the answer sheet, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer sheet cannot be accepted if you fail to sign this declaration.

Notice…
A graphing calculator, a straightedge (ruler), and a compass must be available for you to use while taking this examination.


DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN.

Answer all **24** questions in this part. Each correct answer will receive **2** credits. No partial credit will be allowed. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For each statement or question, choose the word or expression that, of those given, best completes the statement or answers the question. Record your answers on your separate answer sheet. [48]

Use this space for computations.

1 In the diagram below, $\overline{AEFB} \parallel \overline{CGD}$, and $\overline{GE}$ and $\overline{GF}$ are drawn.
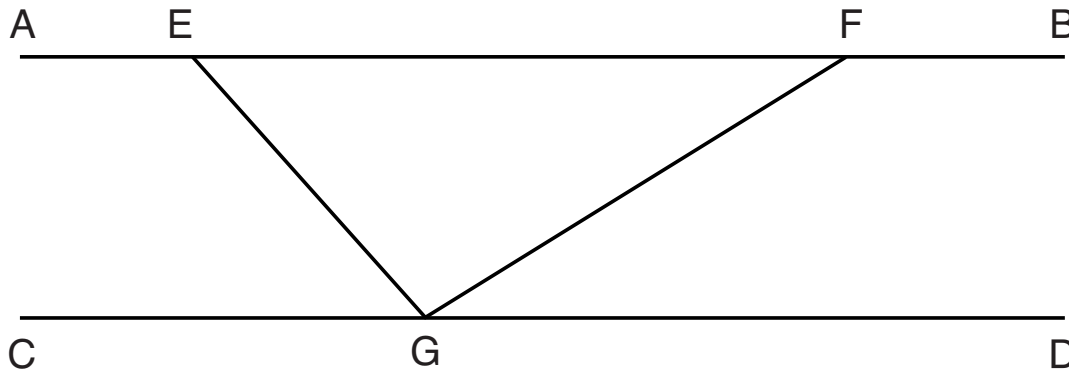
If m∠*EFG* = 32° and m∠*AEG* = 137°, what is m∠*EGF*?

(1) 11° (3) 75°

(2) 43° (4) 105°

2 If $\triangle ABC$ is mapped onto $\triangle DEF$ after a line reflection and $\triangle DEF$ is mapped onto $\triangle XYZ$ after a translation, the relationship between $\triangle ABC$ and $\triangle XYZ$ is that they are always
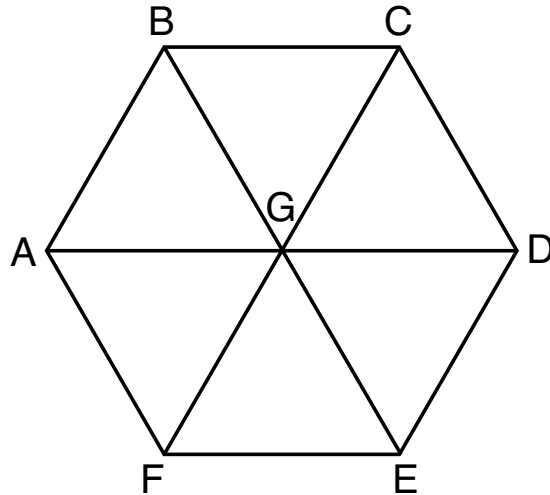
(1) congruent and similar

(2) congruent but not similar

(3) similar but not congruent

(4) neither similar nor congruent

3 An isosceles right triangle whose legs measure 6 is continuously rotated about one of its legs to form a three-dimensional object. The three-dimensional object is a

(1) cylinder with a diameter of 6

(2) cylinder with a diameter of 12

(3) cone with a diameter of 6

(4) cone with a diameter of 12

4 In regular hexagon *ABCDEF* shown below, $\overline{AD}$, $\overline{BE}$, and $\overline{CF}$ all intersect at *G*.

When △*ABG* is reflected over $\overline{BG}$ and then rotated 180° about point *G*, △*ABG* is mapped onto

(1) △*FEG*   (3) △*CBG*

(2) △*AFG*   (4) △*DEG*

5 A right cylinder is cut perpendicular to its base. The shape of the cross section is a

(1) circle   (3) rectangle

(2) cylinder   (4) triangular prism

6 Yolanda is making a springboard to use for gymnastics. She has 8-inch-tall springs and wants to form a 16.5° angle with the base, as modeled in the diagram below.
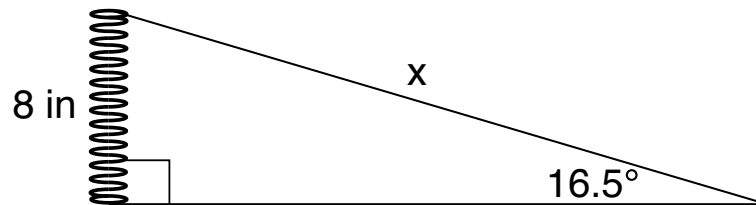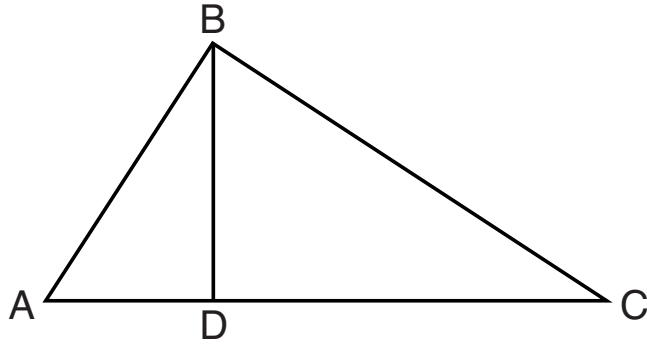

To the *nearest tenth of an inch*, what will be the length of the springboard, x?

(1) 2.3   (3) 27.0

(2) 8.3   (4) 28.2

7 In the diagram below of right triangle ABC, altitude $\overline{BD}$ is drawn to hypotenuse $\overline{AC}$.
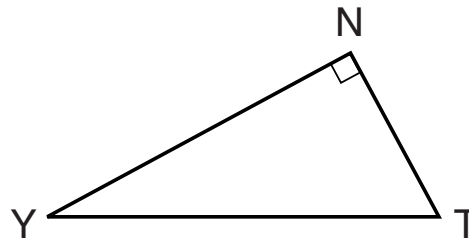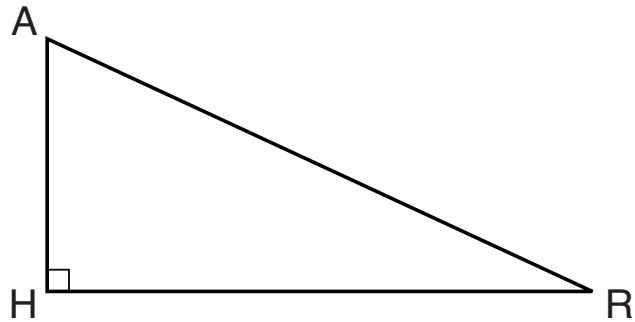

If $BD = 4$, $AD = x - 6$, and $CD = x$, what is the length of $\overline{CD}$?

(1) 5   (3) 8

(2) 2   (4) 11

8 Rhombus $STAR$ has vertices $S(-1,2)$, $T(2,3)$, $A(3,0)$, and $R(0,-1)$. What is the perimeter of rhombus $STAR$?

(1) $\sqrt{34}$ (3) $\sqrt{10}$

(2) $4\sqrt{34}$ (4) $4\sqrt{10}$

9 In the diagram below of $\triangle HAR$ and $\triangle NTY$, angles H and N are right angles, and $\triangle HAR \sim \triangle NTY$.
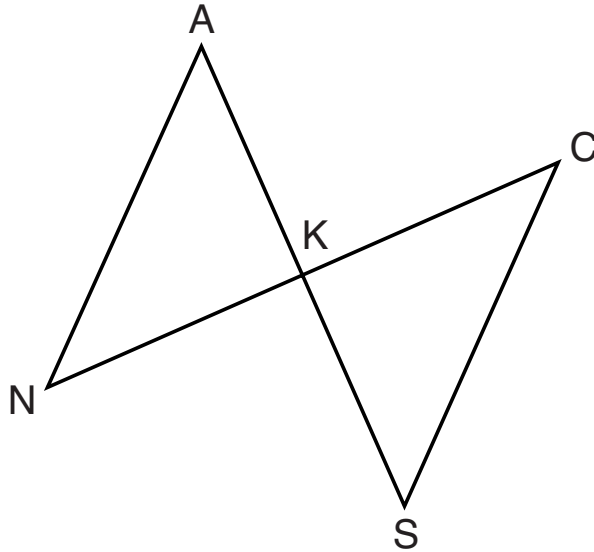
If $AR = 13$ and $HR = 12$, what is the measure of angle Y, to the *nearest degree*?

(1) 23°

(3) 65°

(2) 25°

(4) 67°

10 In the diagram below, $\overline{AKS}$, $\overline{NKC}$, $\overline{AN}$, and $\overline{SC}$ are drawn such that $\overline{AN} \cong \overline{SC}$.

Which additional statement is sufficient to prove
$\triangle KAN \cong \triangle KSC$ by AAS?

(1) $\overline{AS}$ and $\overline{NC}$ bisect each other.

(2) K is the midpoint of $\overline{NC}$.

(3) $\overline{AS} \perp \overline{CN}$

(4) $\overline{AN} \parallel \overline{SC}$

11 Which equation represents a line that is perpendicular to the line represented by $y = \frac{2}{3}x + 1$?
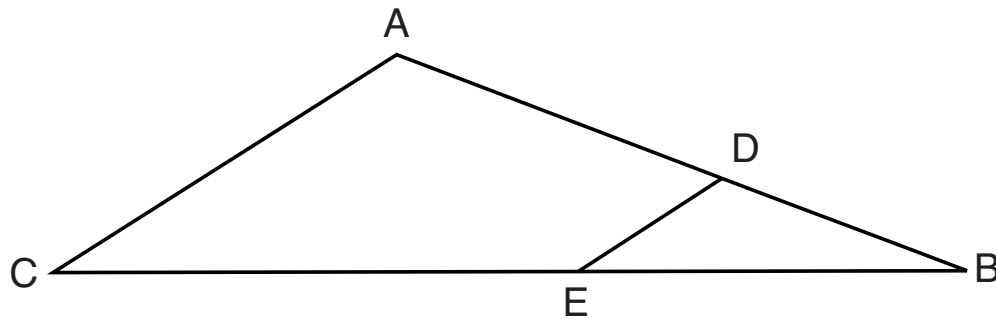
(1) $3x + 2y = 12$ (3) $y = \frac{3}{2}x + 2$

(2) $3x - 2y = 12$ (4) $y = -\frac{2}{3}x + 4$

12 In the diagram of $\triangle ABC$ below, points D and E are on sides $\overline{AB}$ and $\overline{CB}$ respectively, such that $\overline{DE} \parallel \overline{AC}$.

If EB is 3 more than DB, $AB = 14$, and $CB = 21$, what is the length of $\overline{AD}$?

(1) 6   (3) 9

(2) 8   (4) 12

13 Quadrilateral *MATH* has both pairs of opposite sides congruent and parallel. Which statement about quadrilateral *MATH* is always true?

(1) $\overline{MT} \cong \overline{AH}$
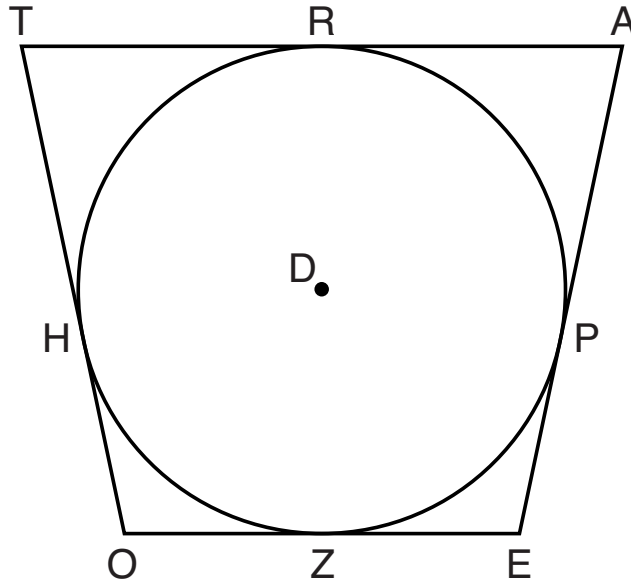
(3) $\angle MHT \cong \angle ATH$

(2) $\overline{MT} \perp \overline{AH}$

(4) $\angle MAT \cong \angle MHT$

GO RIGHT ON TO THE NEXT PAGE ➡

14 In the figure shown below, quadrilateral *TAEO* is circumscribed around circle *D*. The midpoint of $\overline{TA}$ is *R*, and $\overline{HO} \cong \overline{PE}$.

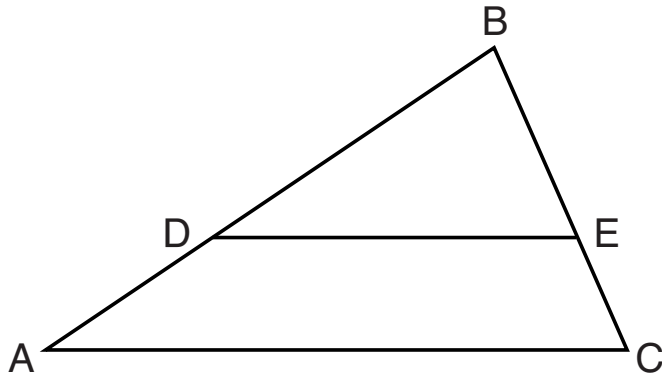If *AP* = 10 and *EO* = 12, what is the perimeter of quadrilateral *TAEO*?

(1) 56

(3) 72

(2) 64

(4) 76

15 The coordinates of the endpoints of directed line segment ABC are $A(-8,7)$ and $C(7,-13)$. If $AB{:}BC = 3{:}2$, the coordinates of B are

(1) $(1,-5)$ (3) $(-3,0)$

(2) $(-2,-1)$ (4) $(3,-6)$

16 In triangle ABC, points D and E are on sides $\overline{AB}$ and $\overline{BC}$, respectively, such that $\overline{DE} \parallel \overline{AC}$, and $AD{:}DB = 3{:}5$.
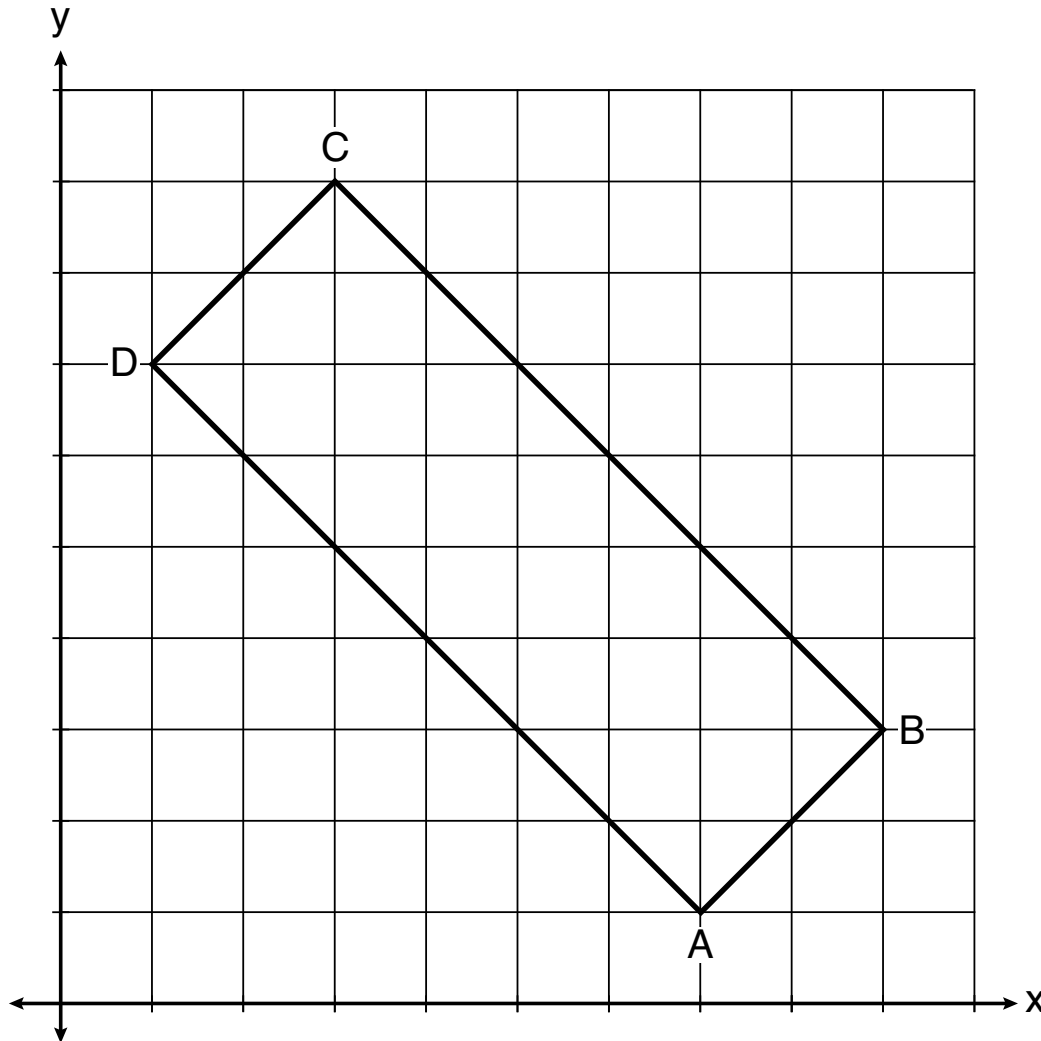

If $DB = 6.3$ and $AC = 9.4$, what is the length of $\overline{DE}$, to the *nearest tenth*?

(1) 3.8   (3) 5.9

(2) 5.6   (4) 15.7

GO RIGHT ON TO THE NEXT PAGE ➡

17 In the diagram below, rectangle $ABCD$ has vertices whose coordinates are $A(7,1)$, $B(9,3)$, $C(3,9)$, and $D(1,7)$.

Which transformation will *not* carry the rectangle onto itself?

(1) a reflection over the line $y = x$

(2) a reflection over the line $y = -x + 10$

(3) a rotation of 180° about the point (6,6)

(4) a rotation of 180° about the point (5,5)

18 A circle with a diameter of 10 cm and a central angle of 30° is drawn
   below.
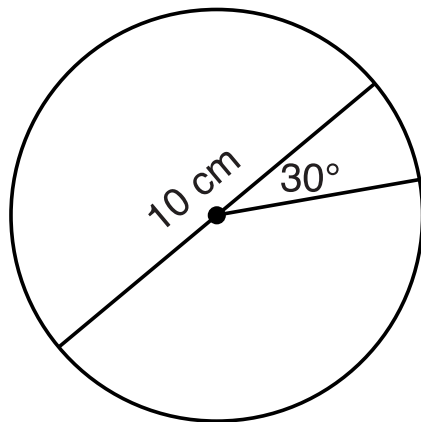
What is the area, to the *nearest tenth of a square centimeter*, of the
sector formed by the 30° angle?

(1) 5.2   (3) 13.1

(2) 6.5   (4) 26.2

19 A child's tent can be modeled as a pyramid with a square base whose sides measure 60 inches and whose height measures 84 inches. What is the volume of the tent, to the *nearest cubic foot*?
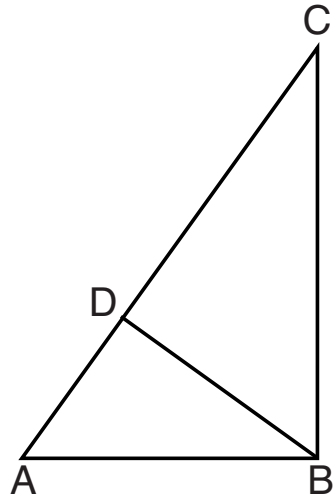
(1) 35

(3) 82

(2) 58

(4) 175

20 In the accompanying diagram of right triangle ABC, altitude $\overline{BD}$ is drawn to hypotenuse $\overline{AC}$.

Which statement must always be true?

(1) $\dfrac{AD}{AB} = \dfrac{BC}{AC}$

(3) $\dfrac{BD}{BC} = \dfrac{AB}{AD}$

(2) $\dfrac{AD}{AB} = \dfrac{AB}{AC}$

(4) $\dfrac{AB}{BC} = \dfrac{BD}{AC}$

21 An equation of circle O is $x^2 + y^2 + 4x - 8y = -16$. The statement that best describes circle O is the

  (1) center is $(2,-4)$ and is tangent to the x-axis

  (2) center is $(2,-4)$ and is tangent to the y-axis

  (3) center is $(-2,4)$ and is tangent to the x-axis

  (4) center is $(-2,4)$ and is tangent to the y-axis

22 In $\triangle ABC$, $\overline{BD}$ is the perpendicular bisector of $\overline{ADC}$. Based upon this information, which statements below can be proven?

  I. $\overline{BD}$ is a median.

  II. $\overline{BD}$ bisects $\angle ABC$.

  III. $\triangle ABC$ is isosceles.

  (1) I and II, only   (3) II and III, only

  (2) I and III, only   (4) I, II, and III

23 Triangle RJM has an area of 6 and a perimeter of 12. If the triangle is dilated by a scale factor of 3 centered at the origin, what are the area and perimeter of its image, triangle $R'J'M'$?

   (1) area of 9 and perimeter of 15

   (2) area of 18 and perimeter of 36

   (3) area of 54 and perimeter of 36

   (4) area of 54 and perimeter of 108

24 If $\sin (2x + 7)° = \cos (4x - 7)°$, what is the value of x?

   (1) 7   (3) 21

   (2) 15   (4) 30

Answer all **7** questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [14]
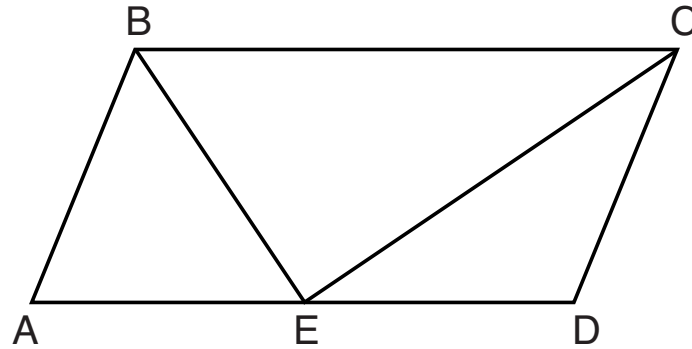
25 In the circle on the next page, $\overline{AB}$ is a chord. Using a compass and straightedge, construct a a diameter of the circle. [Leave all construction marks.]

The diagram for question 26 is on the next page.
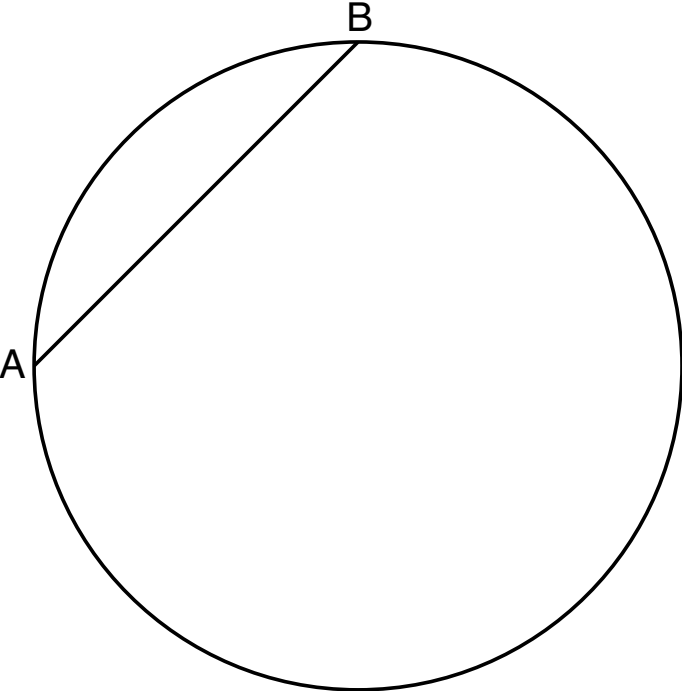
26 In parallelogram $ABCD$ shown below, the bisectors of $\angle ABC$ and $\angle DCB$ meet at E, a point on $\overline{AD}$.
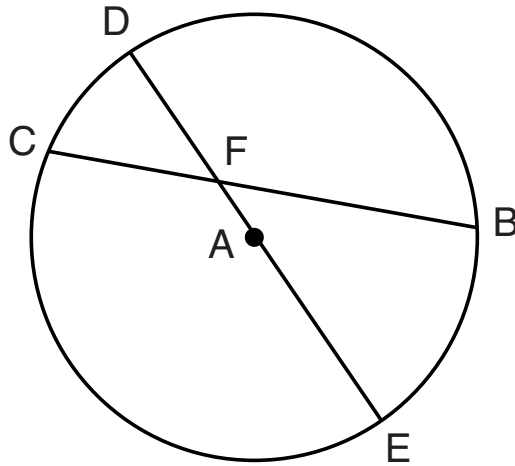

If m$\angle A = 68°$, determine and state m$\angle BEC$.

Work space for question 26 is continued on the next page.

Question 26 continued

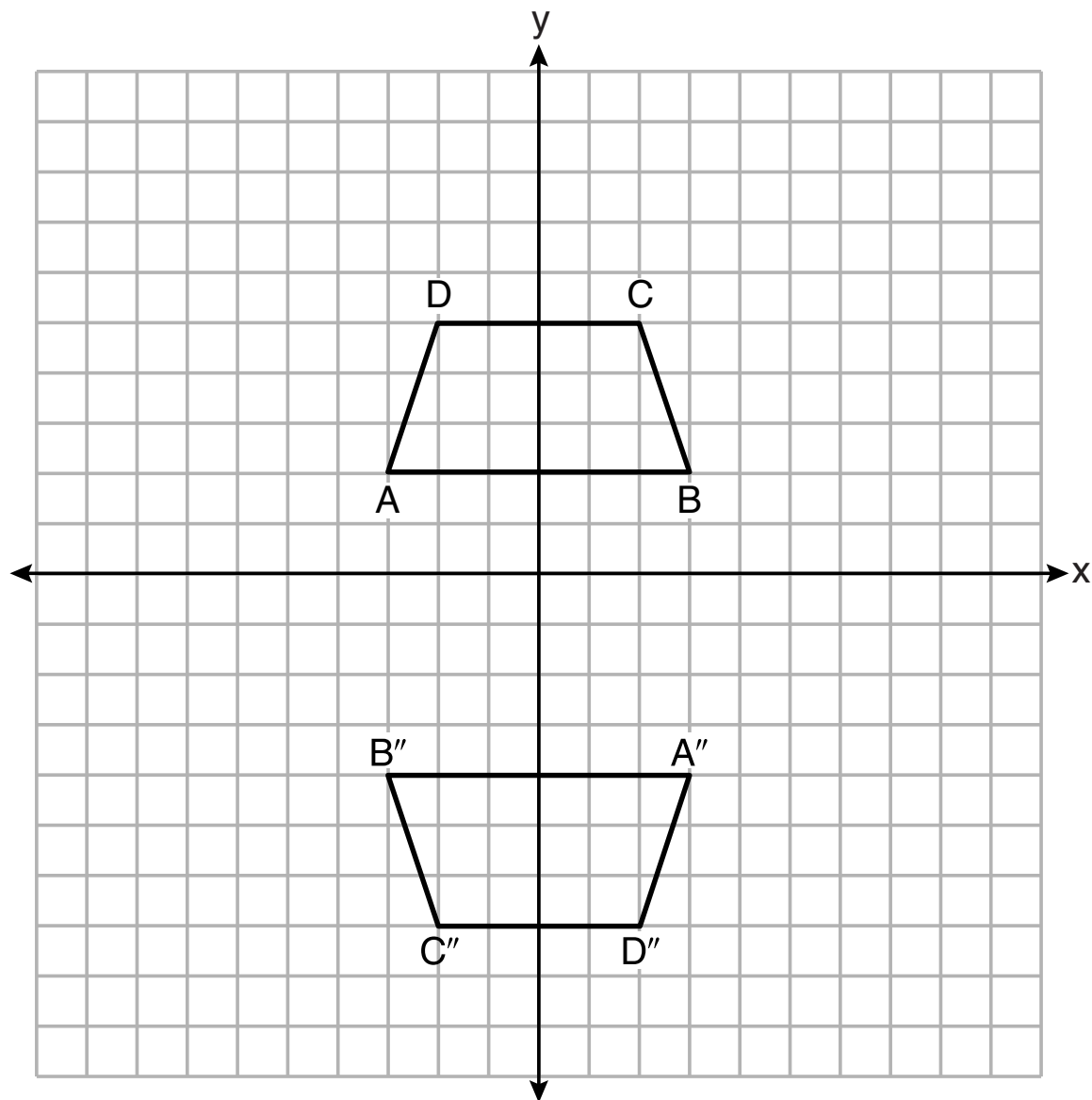**27** In circle A below, chord $\overline{BC}$ and diameter $\overline{DAE}$ intersect at F.

If $m\overset{\frown}{CD} = 46°$ and $m\overset{\frown}{DB} = 102°$, what is $m\angle CFE$?

Work space for question 27 is continued on the next page.

Question 27 continued

28 Trapezoids *ABCD* and *A″B″C″D″* are graphed on the set of axes below.
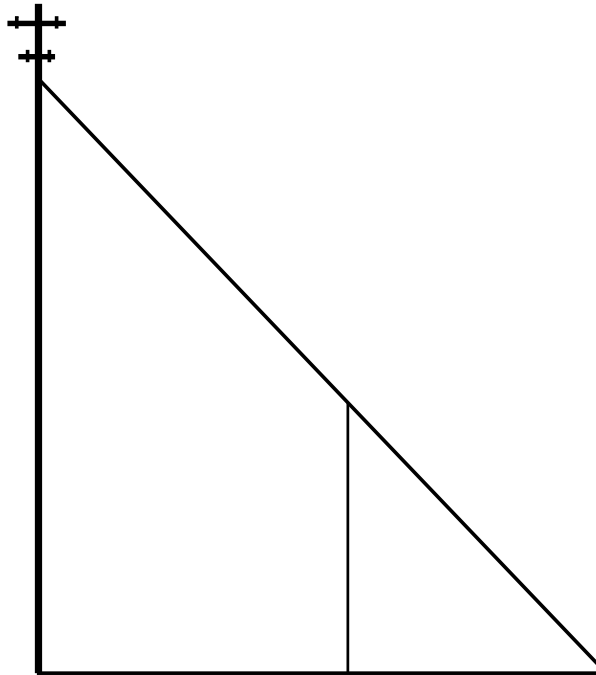
Question 28 continued

Describe a sequence of transformations that maps trapezoid *ABCD* onto trapezoid *A″B″C″D″*.

29 In the model below, a support wire for a telephone pole is attached to the pole and anchored to a stake in the ground 15 feet from the base of the telephone pole. Jamal places a 6-foot wooden pole under the support wire parallel to the telephone pole, such that one end of the pole is on the ground and the top of the pole is touching the support wire. He measures the distance between the bottom of the pole and the stake in the ground.

Jamal says he can approximate how high the support wire attaches to the telephone pole by using similar triangles. Explain why the triangles are similar.

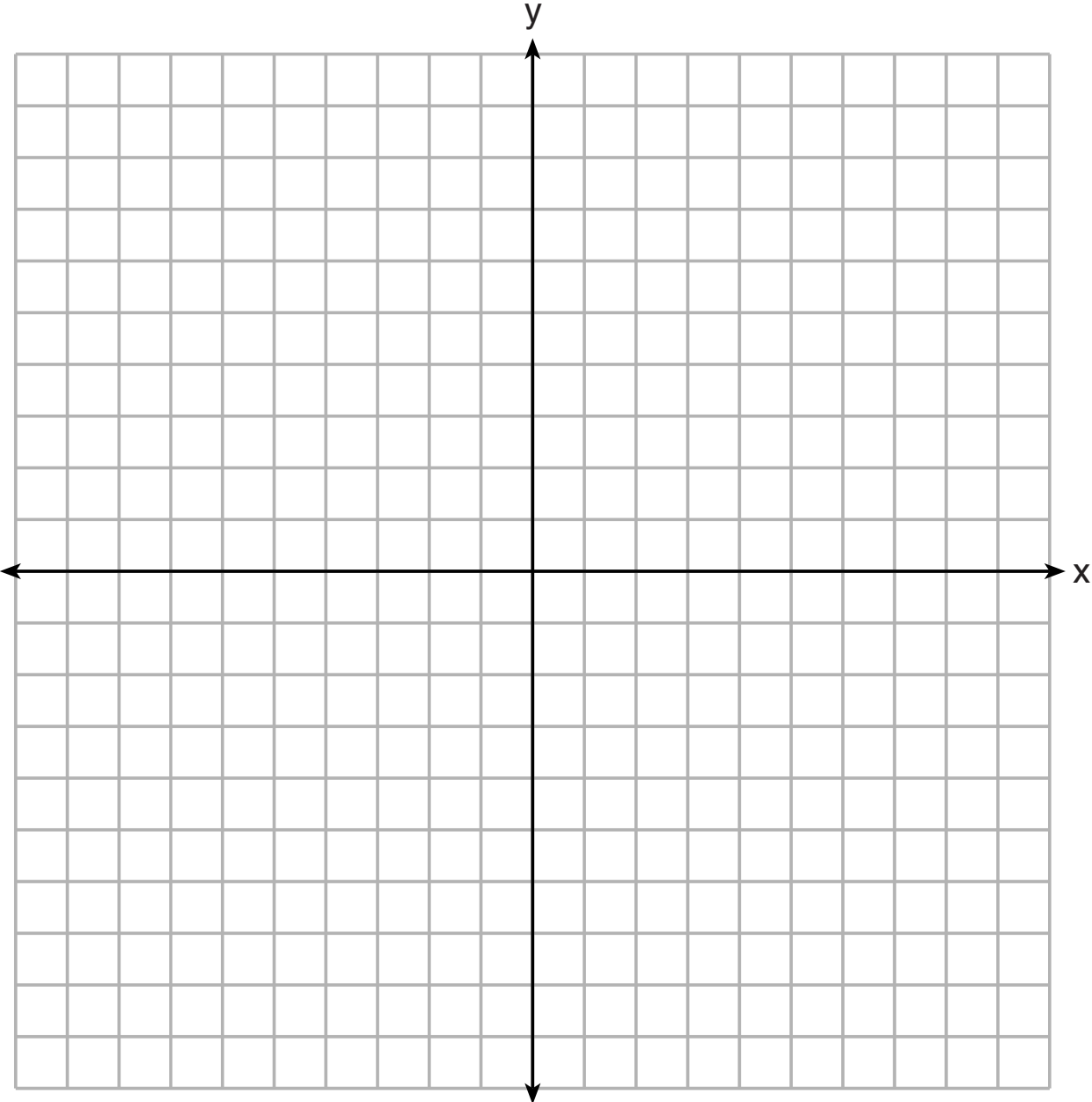**Work space for question 29 is continued on the next page.**

Question 29 continued

30 Aliyah says that when the line $4x + 3y = 24$ is dilated by a scale factor of 2 centered at the point $(3,4)$, the equation of the dilated line is $y = -\dfrac{4}{3}x + 16$. Is Aliyah correct? Explain why.
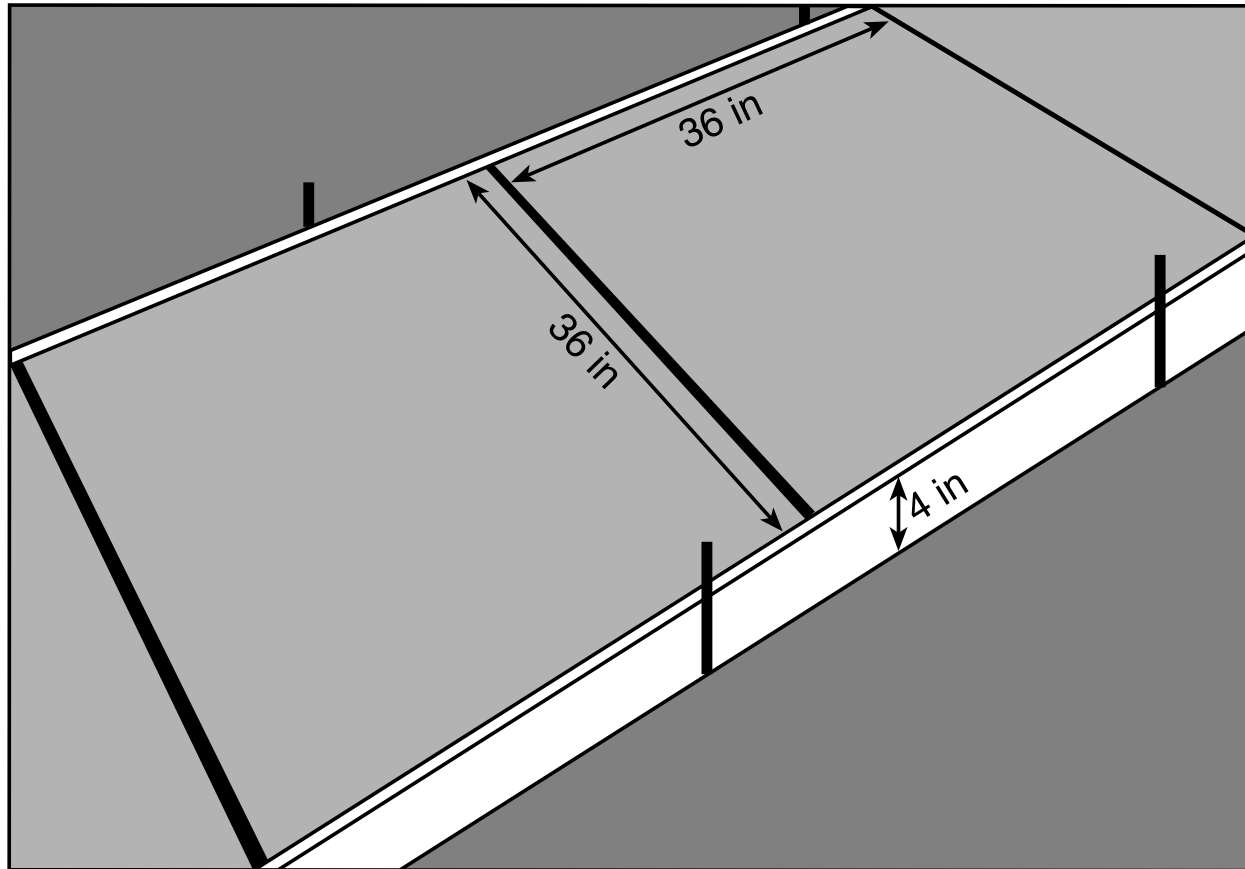
[The use of the set of axes on the next page is optional.]

Question 30 continued

31 Ian needs to replace two concrete sections in his sidewalk, as modeled below. Each section is 36 inches by 36 inches and 4 inches deep. He can mix his own concrete for $3.25 per cubic foot.

How much money will it cost Ian to replace the two concrete sections?

**Work space for question 31 is continued on the next page.**

Question 31 continued

Answer all 3 questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil.   [12]

32 Given: $\triangle ABC$, $\overline{AEC}$, $\overline{BDE}$ with $\angle ABE \cong \angle CBE$, and $\angle ADE \cong \angle CDE$

Prove: $\overline{BDE}$ is the perpendicular bisector of $\overline{AC}$
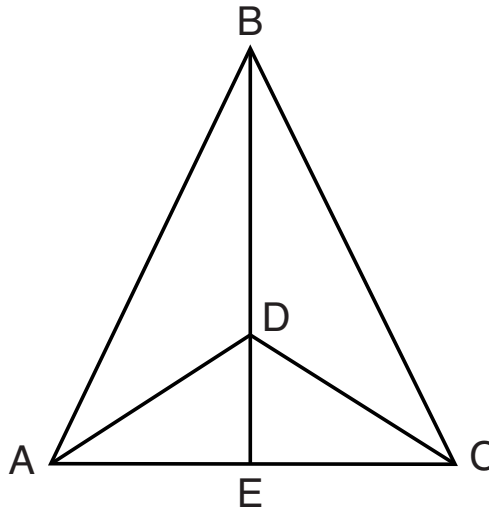
Fill in the missing statement and reasons below.

Statements	Reasons
(1) $\triangle ABC$, $\overline{AEC}$, $\overline{BDE}$ with $\angle ABE \cong \angle CBE$ and $\angle ADE \cong \angle CDE$	(1) Given
(2) $\overline{BD} \cong \overline{BD}$	(2) _____
(3) $\angle BDA$ and $\angle ADE$ are supplementary. $\angle BDC$ and $\angle CDE$ are supplementary.	(3) Linear pairs of angles are supplementary.
(4) _____	(4) Supplements of congruent angles are congruent.
(5) $\triangle ABD \cong \triangle CBD$	(5) ASA
(6) $\overline{AD} \cong \overline{CD}$, $\overline{AB} \cong \overline{CB}$	(6) _____
(7) $\overline{BDE}$ is the perpendicular bisector of $\overline{AC}$.	(7) _____ _____ _____ _____

33 A homeowner is building three steps leading to a deck, as modeled by the diagram below. All three step rises, $\overline{HA}$, $\overline{FG}$, and $\overline{DE}$, are congruent, and all three step runs, $\overline{HG}$, $\overline{FE}$, and $\overline{DC}$, are congruent. Each step rise is perpendicular to the step run it joins. The measure of $\angle CAB = 36°$ and $m\angle CBA = 90°$.
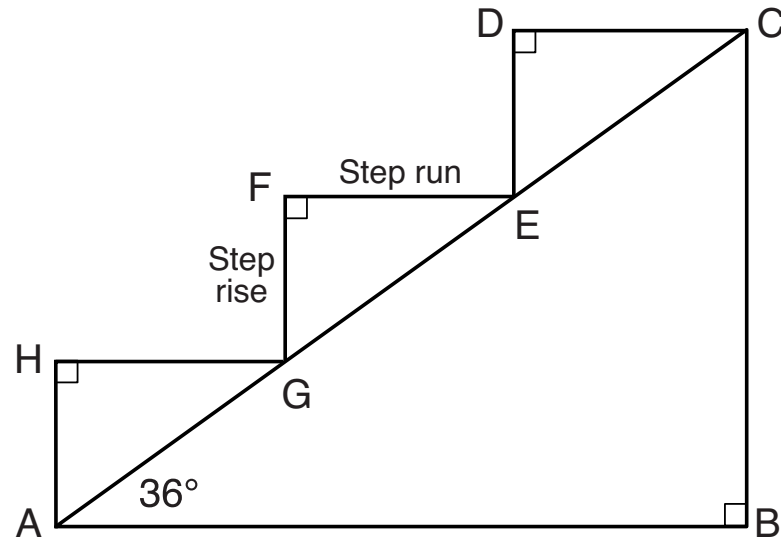
If each step run is parallel to $\overline{AB}$ and has a length of 10 inches, determine and state the length of each step rise, to the *nearest tenth of an inch*.

Question 33 is continued on the next page.

Determine and state the length of $\overline{AC}$, to the *nearest inch*.

34 A bakery sells hollow chocolate spheres. The larger diameter of each sphere is 4 cm. The thickness of the chocolate of each sphere is 0.5 cm. Determine and state, to the *nearest tenth of a cubic centimeter*, the amount of chocolate in each hollow sphere.

Question 34 continued

The bakery packages 8 of them into a box. If the density of the chocolate is 1.308 g/cm^3, determine and state, to the *nearest gram,* the total mass of the chocolate in the box.

Answer the question in this part. A correct answer will receive 6 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for the question to determine your answer. Note that diagrams are not necessarily drawn to scale. For the question in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil.   [6]

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35 The vertices of quadrilateral *MATH* have coordinates $M(-4,2)$, $A(-1,-3)$, $T(9,3)$, and $H(6,8)$.

Prove that quadrilateral *MATH* is a parallelogram.

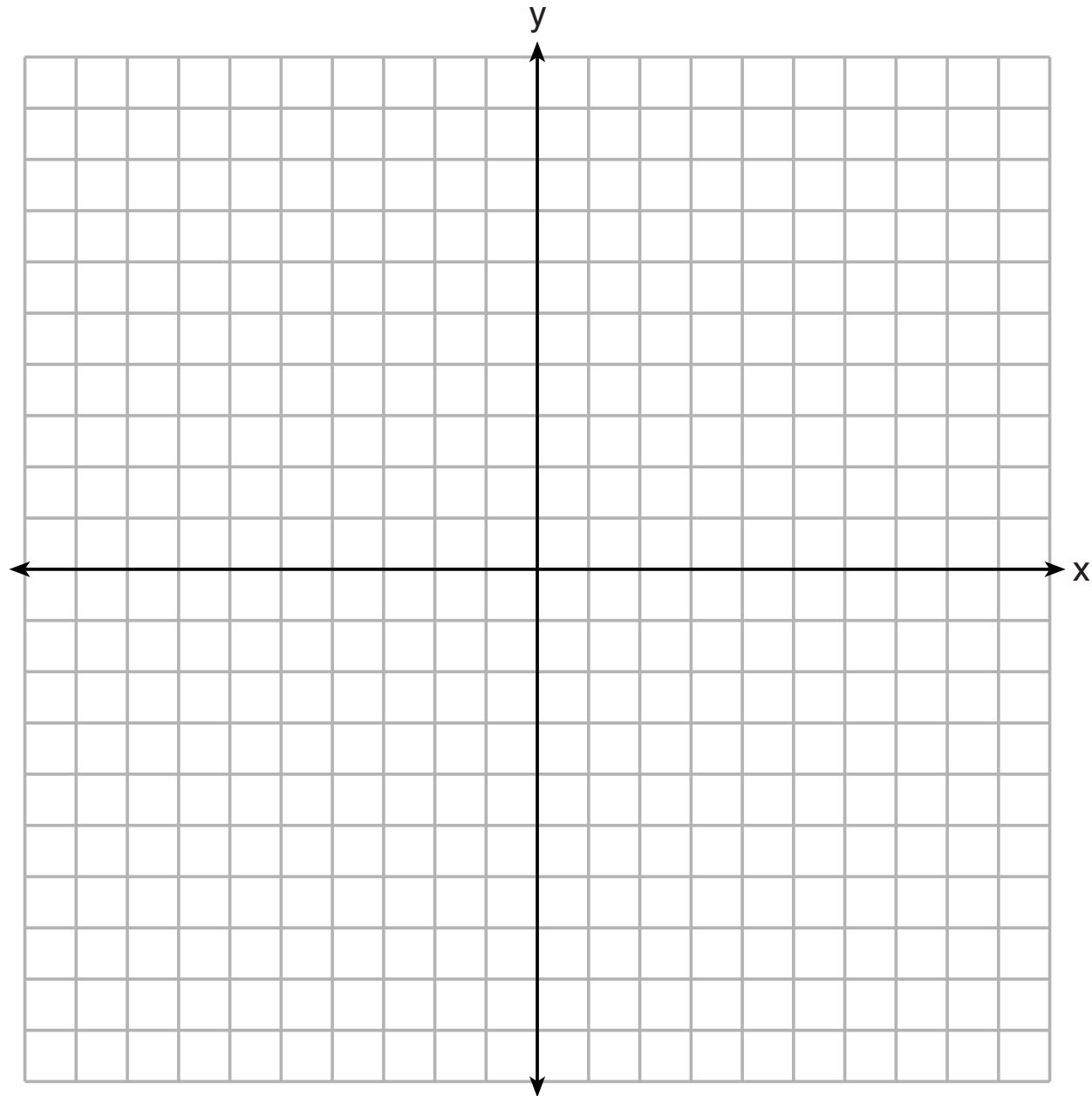[The use of the set of axes on page 44 is optional.]

Question 35 continued

Prove that quadrilateral *MATH* is a rectangle.

[The use of the set of axes on the next page is optional.]

Work space for question 35 is continued on the next page.

High School Math Reference Sheet

1 inch = 2.54 centimeters   1 kilometer = 0.62 mile   1 cup = 8 fluid ounces

1 meter = 39.37 inches   1 pound = 16 ounces   1 pint = 2 cups

1 mile = 5280 feet   1 pound = 0.454 kilogram   1 quart = 2 pints

1 mile = 1760 yards   1 kilogram = 2.2 pounds   1 gallon = 4 quarts

1 mile = 1.609 kilometers   1 ton = 2000 pounds   1 gallon = 3.785 liters

1 liter = 0.264 gallon

1 liter = 1000 cubic centimeters

Triangle	$A = \frac{1}{2}bh$
Parallelogram	$A = bh$
Circle	$A = \pi r^2$
Circle	$C = \pi d$ or $C = 2\pi r$
General Prisms	$V = Bh$

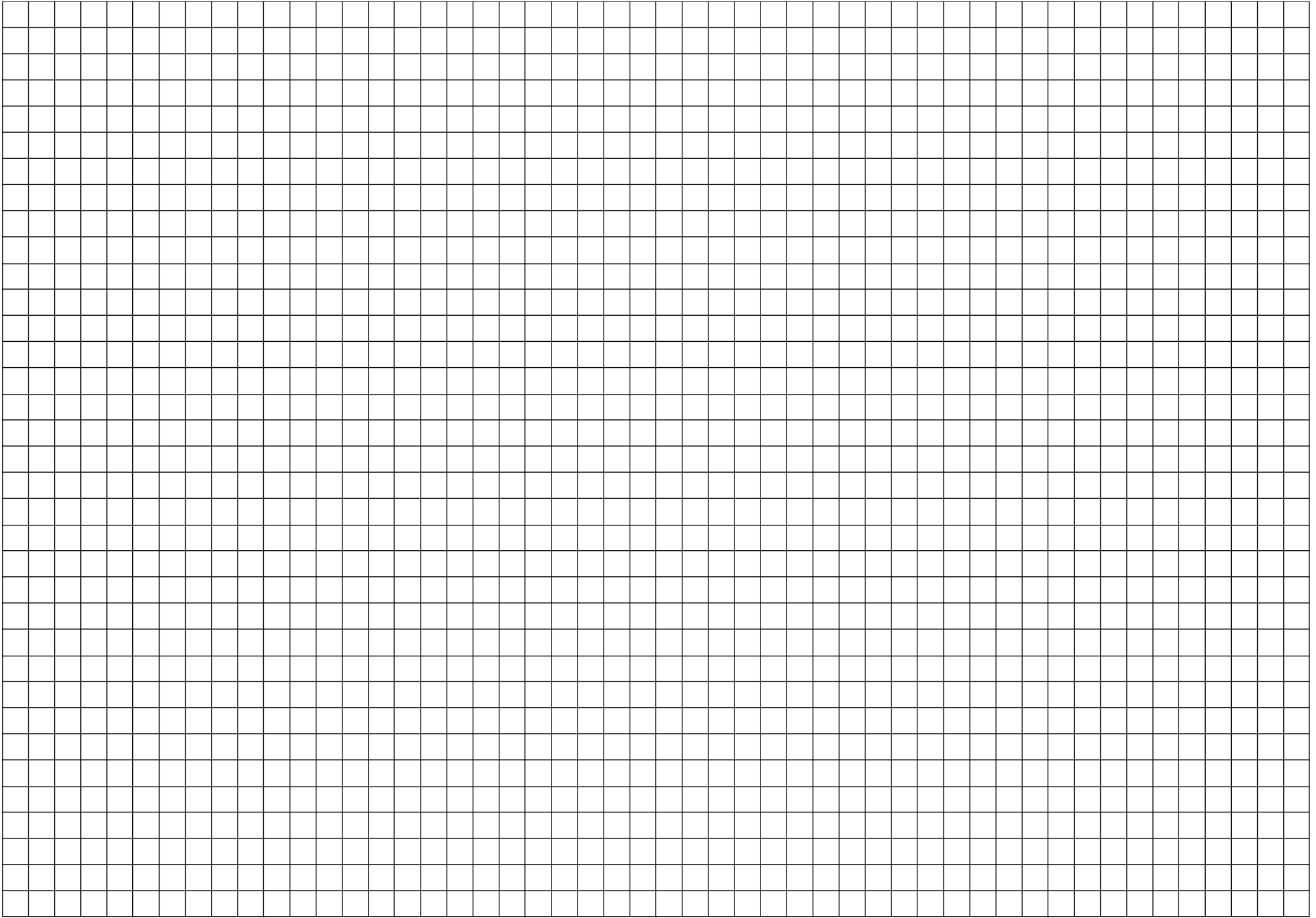|	
Pythagorean Theorem	$a^2 + b^2 = c^2$
Quadratic Formula	$x = \dfrac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
Arithmetic Sequence	$a_n = a_1 + (n - 1)d$
Geometric Sequence	$a_n = a_1 r^{n-1}$
Geometric Series	$S_n = \dfrac{a_1 - a_1 r^n}{1 - r}$ where $r \neq 1$

The Reference Sheet is continued on the next page.

Reference Sheet — concluded

Cylinder	$V = \pi r^2 h$
Sphere	$V = \dfrac{4}{3}\pi r^3$
Cone	$V = \dfrac{1}{3}\pi r^2 h$
Pyramid	$V = \dfrac{1}{3}Bh$

Radians	1 radian = $\dfrac{180}{\pi}$ degrees
Degrees	1 degree = $\dfrac{\pi}{180}$ radians
Exponential Growth/Decay	$A = A_0 e^{k(t - t_0)} + B_0$

Scrap Graph Paper — This sheet will *not* be scored.