

The University of the State of New York
REGENTS HIGH SCHOOL EXAMINATION

ALGEBRA II

Tuesday, August 18, 2026 — 12:30 to 3:30 p.m., only

MODEL RESPONSE SET

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Question 25

25 In order to keep the store properly stocked with produce, a grocery store manager wants to determine the most popular day of the week for people to buy apples and oranges. She randomly collects a sample of sales records for each day for three consecutive weeks. Is this type of data collection method a survey, an observational study, or an experiment? Explain your reasoning.

it is an observational
Study ~~which~~ because she isn't
doing an experiment with a
control group and experimentation
group, she isn't surveying people
on when they enter the
store or buy apples, but is
just collecting data that
she observes in the store

Score 2: The student gave a complete and correct response.

Question 25

- 25** In order to keep the store properly stocked with produce, a grocery store manager wants to determine the most popular day of the week for people to buy apples and oranges. She randomly collects a sample of sales records for each day for three consecutive weeks. Is this type of data collection method a survey, an observational study, or an experiment? Explain your reasoning.

It's an observational study, because the manager ~~isn't~~ isn't asking anyone about their preferences neither he is changing conditions of the experiment, so I can eliminate these two options. What I'm left with is an observational study.

Answer: observational study.

Score 2: The student gave a complete and correct response.

Question 25

25 In order to keep the store properly stocked with produce, a grocery store manager wants to determine the most popular day of the week for people to buy apples and oranges. She randomly collects a sample of sales records for each day for three consecutive weeks. Is this type of data collection method a survey, an observational study, or an experiment? Explain your reasoning.

This study is an observational study
because she is not changing any
variables.

Score 1: The student's explanation is incomplete.

Question 25

25 In order to keep the store properly stocked with produce, a grocery store manager wants to determine the most popular day of the week for people to buy apples and oranges. She randomly collects a sample of sales records for each day for three consecutive weeks. Is this type of data collection method a survey, an observational study, or an experiment? Explain your reasoning.

~~Survey because she isn't~~
~~just observing~~

Observational, she is observing
the sales, not getting involved
with anything.

Score 1: The student's explanation is incomplete.

Question 25

- 25** In order to keep the store properly stocked with produce, a grocery store manager wants to determine the most popular day of the week for people to buy apples and oranges. She randomly collects a sample of sales records for each day for three consecutive weeks. Is this type of data collection method a survey, an observational study, or an experiment? Explain your reasoning.

Experiment because they are collecting data of a certain item for each day for three consecutive weeks so it is an experiment cause you are trying to find something out by using data over a certain period of time.

Score 0: The student did not satisfy the criteria for one or more credits.

Question 25

25 In order to keep the store properly stocked with produce, a grocery store manager wants to determine the most popular day of the week for people to buy apples and oranges. She randomly collects a sample of sales records for each day for three consecutive weeks. Is this type of data collection method a survey, an observational study, or an experiment? Explain your reasoning.

This is a survey
because she is
trying to figure
out what she needs
to do not what
is happening
(observ. & exper.)
She needs this
information
to do something
not just study it

Score 0: The student did not satisfy the criteria for one or more credits.

Question 26

26 Given the following functions $f(x) = 2x^2 + 3x - 7$ and $g(x) = 2x - 5$, determine $f(x) - g(x)$, and express the result in standard form.

$$\begin{aligned} f(x) - g(x) &= (2x^2 + 3x - 7) - (2x - 5) \\ &= 2x^2 + 3x - 7 - 2x + 5 \\ &= 2x^2 + x - 2 \end{aligned}$$

$2x^2 + x - 2$

Score 2: The student gave a complete and correct response.

Question 26

26 Given the following functions $f(x) = 2x^2 + 3x - 7$ and $g(x) = 2x - 5$, determine $f(x) - g(x)$, and express the result in standard form.

$$\begin{array}{r} (2x^2 + 3x - 7) - (2x - 5) \\ 2x^2 + 3x - 7 \\ - 2x + 5 \\ \hline 2x^2 + x - 2 \end{array}$$

Score 2: The student gave a complete and correct response.

Question 26

- 26** Given the following functions $f(x) = 2x^2 + 3x - 7$ and $g(x) = 2x - 5$, determine $f(x) - g(x)$, and express the result in standard form.

$$2x^2 + 3x - 7 - 2x - 5$$

$$2x^2 + 1x - 12$$

Score 1: The student made a computational error.

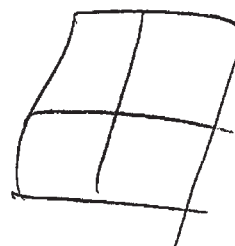
Question 26

- 26** Given the following functions $f(x) = 2x^2 + 3x - 7$ and $g(x) = 2x - 5$, determine $f(x) - g(x)$, and express the result in standard form.

$$(2x^2 + 3x - 7) - (2x - 5)$$

$$2x^2 + 3x - 7 - 2x + 10$$

$$2x^2 + x + 3$$



Score 1: The student made a computational error.

Question 26

- 26** Given the following functions $f(x) = 2x^2 + 3x - 7$ and $g(x) = 2x - 5$, determine $f(x) - g(x)$, and express the result in standard form.

$$\begin{array}{r} 2x^2 + 3x - 7 \\ 2x \begin{array}{|c|c|c|} \hline 4x^3 & 6x^2 & -14x \\ \hline \end{array} \\ - \\ 5 \begin{array}{|c|c|c|} \hline 10x^2 & -15x & 35 \\ \hline \end{array} \end{array}$$

$$4x^3 + 6x^2 - 14x + 10x^2 - 15x + 35$$

$$4x^3 + 16x^2$$

Score 0: The student made multiple errors.

Question 26

- 26 Given the following functions $f(x) = 2x^2 + 3x - 7$ and $g(x) = 2x - 5$, determine $f(x) - g(x)$, and express the result in standard form.

$$\begin{array}{r} 2x^2 + 3x - 7 = 0 \\ - (-2x - 5) \\ \hline 2x^2 + 5x - 2 = 0 \end{array}$$

$$\frac{-(5) \pm \sqrt{(5)^2 - 4(2)(-2)}}{2(2)}$$

$$\frac{-5 \pm \sqrt{9}}{4}$$

$$\frac{-5 \pm 3}{4}$$

$$\frac{-5 + 3}{4}$$

$$\frac{-5 - 3}{4}$$

$$\frac{-2}{4}$$

$$-\frac{1}{2}$$

$$\frac{-8}{4}$$

$$-2$$

$$2(-2) - 5 = -9$$

$$2(-2)^2 + 3(-2) - 7 = -5$$

$$2(-\frac{1}{2})^2 + 3(-\frac{1}{2}) + 7 = 6$$

$$2(-\frac{1}{2}) - 5 = -6$$

$$6 - (-6) = 12$$

$$-5 - (-9) = 4$$

Score 0: The student did not satisfy the criteria for one or more credits.

Question 27

27 Determine algebraically the zeros of $f(x) = x^3 - 4x^2 - 9x + 36$.

$$\begin{aligned}x^3 - 4x^2 - 9x + 36 &= 0 \\x^2(x-4) - 9(x-4) &= 0 \\(x^2-9)(x-4) &= 0 \\(x+3)(x-3)(x-4) &= 0\end{aligned}$$

$x+3=0$ $\underline{-3-3}$ $x=-3$	$x-3=0$ $\underline{+3+3}$ $x=3$	$x-4=0$ $\underline{+4+4}$ $x=4$
---	--	--

$x = -3$

$x = 3$

$x = 4$

Score 2: The student gave a complete and correct response.

Question 27

27 Determine algebraically the zeros of $f(x) = x^3 - 4x^2 - 9x + 36$.

	$x - 4$	
x^2	x^3	$-4x^2$
-9	$-9x$	$+36$

$$f(x) = x^3 - 4x^2 - 9x + 36$$

$$(x-4)(x^2-9)$$

$$0 = (x-4)(x+3)(x-3)$$

$$\begin{array}{r} x-4=0 \\ +4 \quad +4 \\ \hline x=4 \end{array}$$

$$\begin{array}{r} x+3=0 \\ -3 \quad -3 \\ \hline x=-3 \end{array}$$

$$\begin{array}{r} x-3=0 \\ +3 \quad +3 \\ \hline x=3 \end{array}$$

$$f(4) = 4^3 - 4(4)^2 - 9(4) + 36 = 0$$

$$f(-3) = -3^3 - 4(-3)^2 - 9(-3) + 36 = 0$$

$$f(3) = 3^3 - 4(3)^2 - 9(3) + 36 = 0$$

Score 2: The student gave a complete and correct response.

Question 27

27 Determine algebraically the zeros of $f(x) = x^3 - 4x^2 - 9x + 36$.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$a = 1 \quad b = -4$$

	x	-4
x^2	x^3	$-4x^2$
-9	$-9x$	$+36$

$$(x-4)(x^2-9)$$

$$(x-4)(x-3)(x+3)$$

$$x+4 \quad x-3 \quad x+3$$

$$\{-4, +3, -3\}$$

Score 1: The student reached a benchmark for one credit.

Question 27

27 Determine algebraically the zeros of $f(x) = x^3 - 4x^2 - 9x + 36$.

$$\begin{aligned}x^3 - 4x^2 - 9x + 36 &= 0 \\x^2(x-4) - 9(x-4) &= 0 \\(x^2-9)(x-4) &= 0 \\(x+3)(x-3)(x-4) &= 0 \\\{ \pm 3, 4, 0 \}\end{aligned}$$

Score 1: The student incorrectly included zero as part of the solution.

Question 27

27 Determine algebraically the zeros of $f(x) = x^3 - 4x^2 - 9x + 36$.

$$\begin{array}{l}
 x^3 - 4x^2 \\
 x^2(x-4) \\
 x^2(x+2)(x-2) \\
 (x^2-9)(x+2)(x-2) \\
 (x+3)(x-3)(x+2)(x-2) \\
 \begin{array}{cccc}
 x-2 = & x-3 = & x+2 = & x+3 = 0 \\
 +2 & +3 & -2 & -3 \\
 \cancel{x-2} & \boxed{x=3} & \cancel{x+2} & \boxed{x=-3}
 \end{array}
 \end{array}$$

Score 0: The student made multiple errors.

Question 27

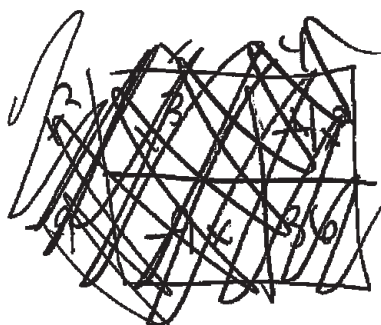
27 Determine algebraically the zeros of $f(x) = \frac{x^3 - 4x^2 - 9x + 36}{x^2 - 9}$.

$$x^2(x-4) - 9(x-4)$$

$$(\sqrt{x^2-9})(x-4)$$

$$(x-9)(x+9)$$

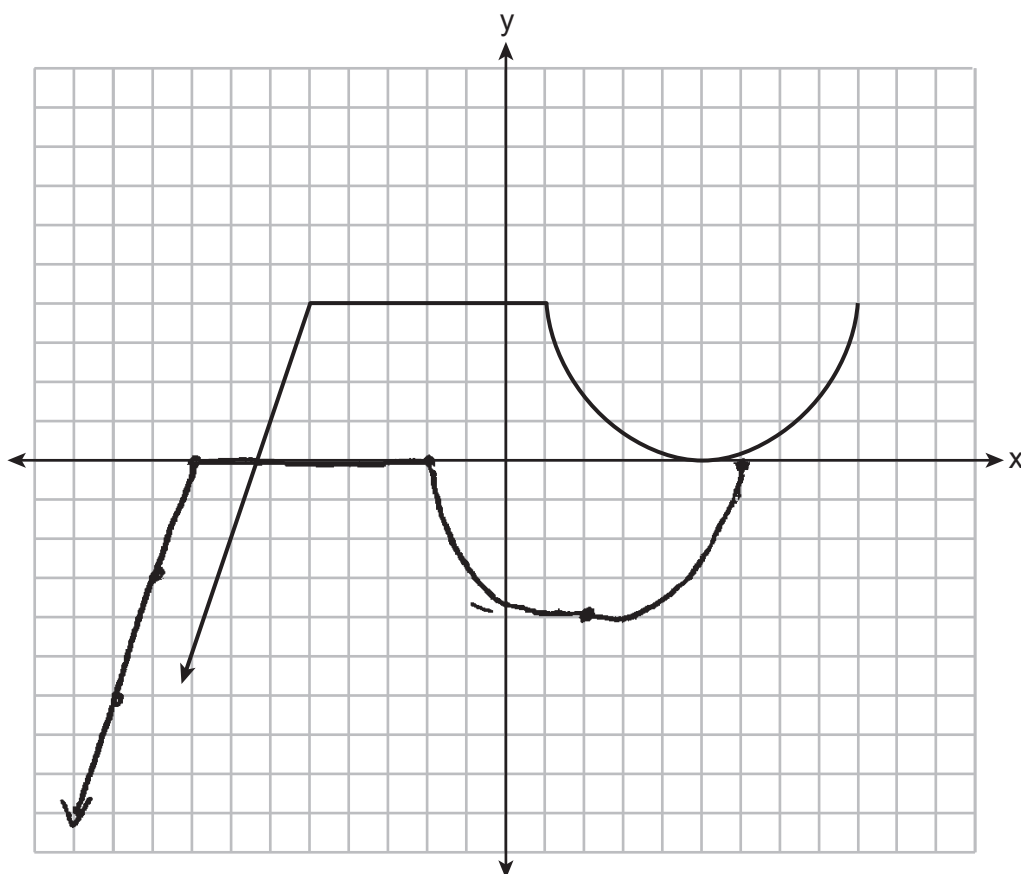
$x = 9$
 $x = -9$



Score 0: The student did not satisfy the criteria for one or more credits.

Question 28

28 The graph of $y = f(x)$ is shown below. On the same set of axes, graph $y = f(x + 3) - 4$.

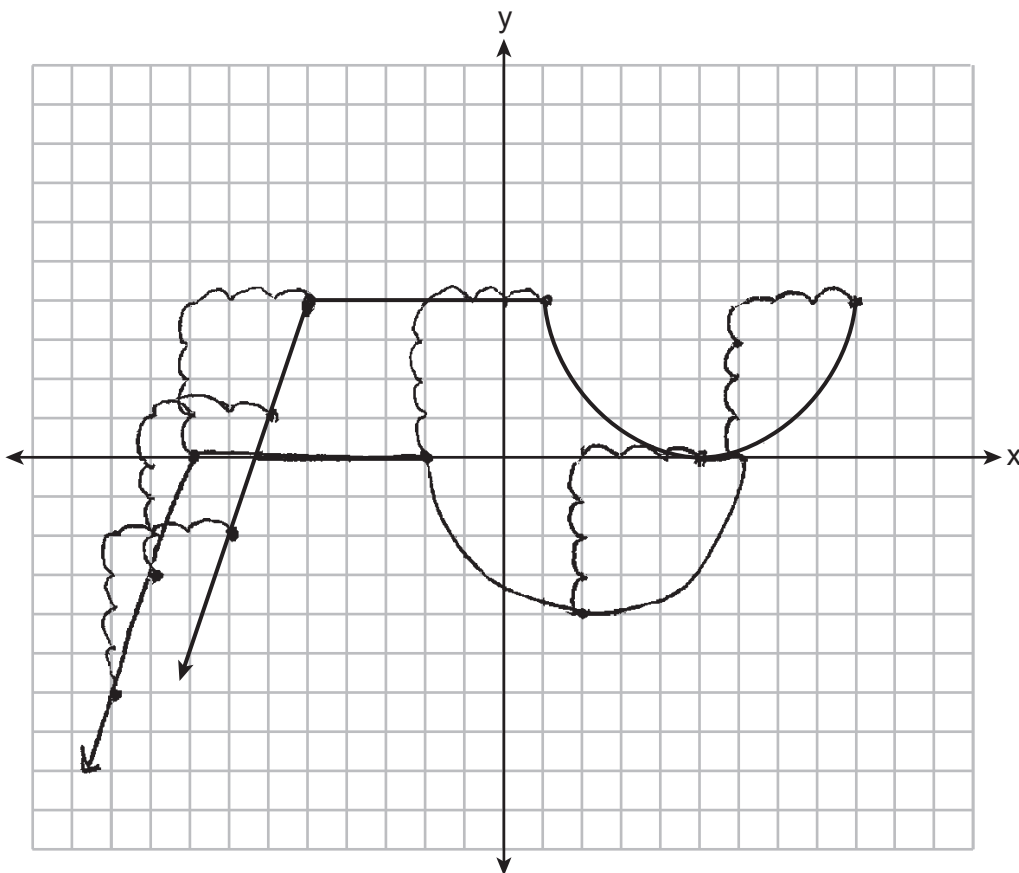


left 3 down 4

Score 2: The student gave a complete and correct response.

Question 28

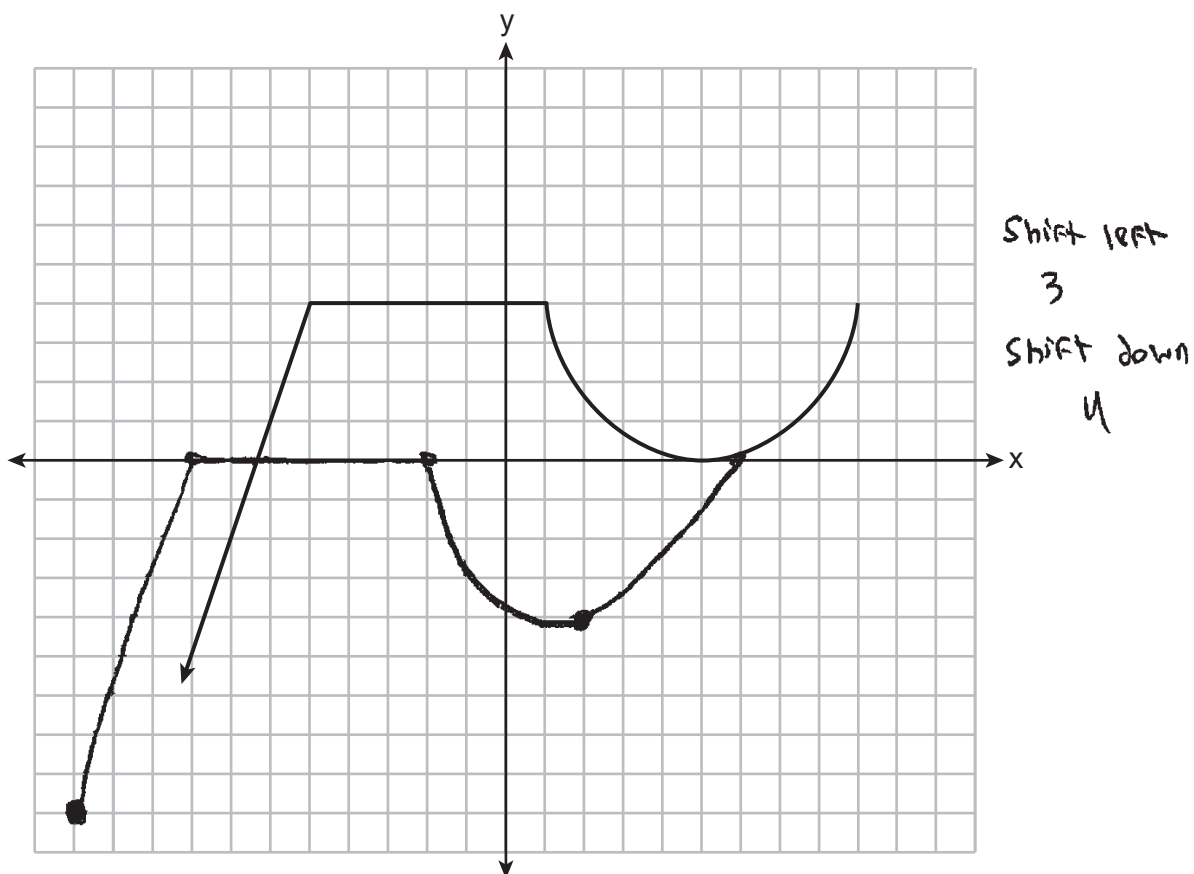
28 The graph of $y = f(x)$ is shown below. On the same set of axes, graph $y = f(x + 3) - 4$.



Score 2: The student gave a complete and correct response.

Question 28

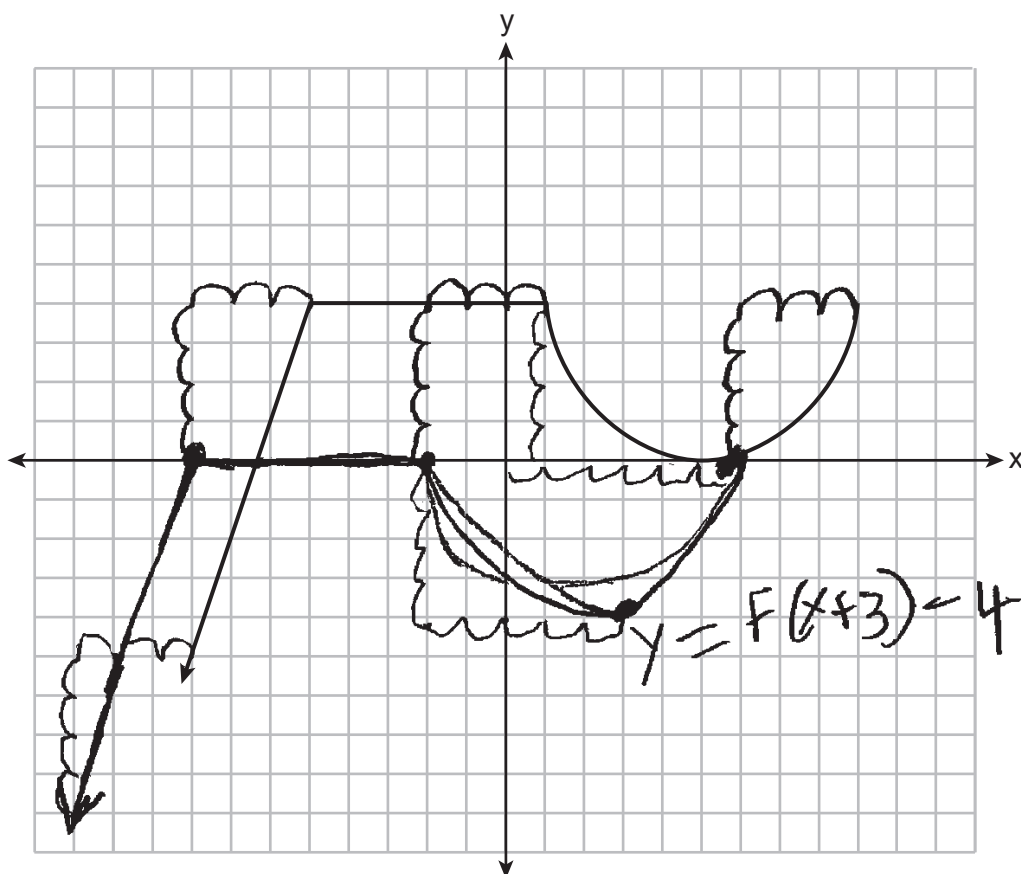
28 The graph of $y = f(x)$ is shown below. On the same set of axes, graph $y = f(x + 3) - 4$.



Score 1: The student did not draw an arrow.

Question 28

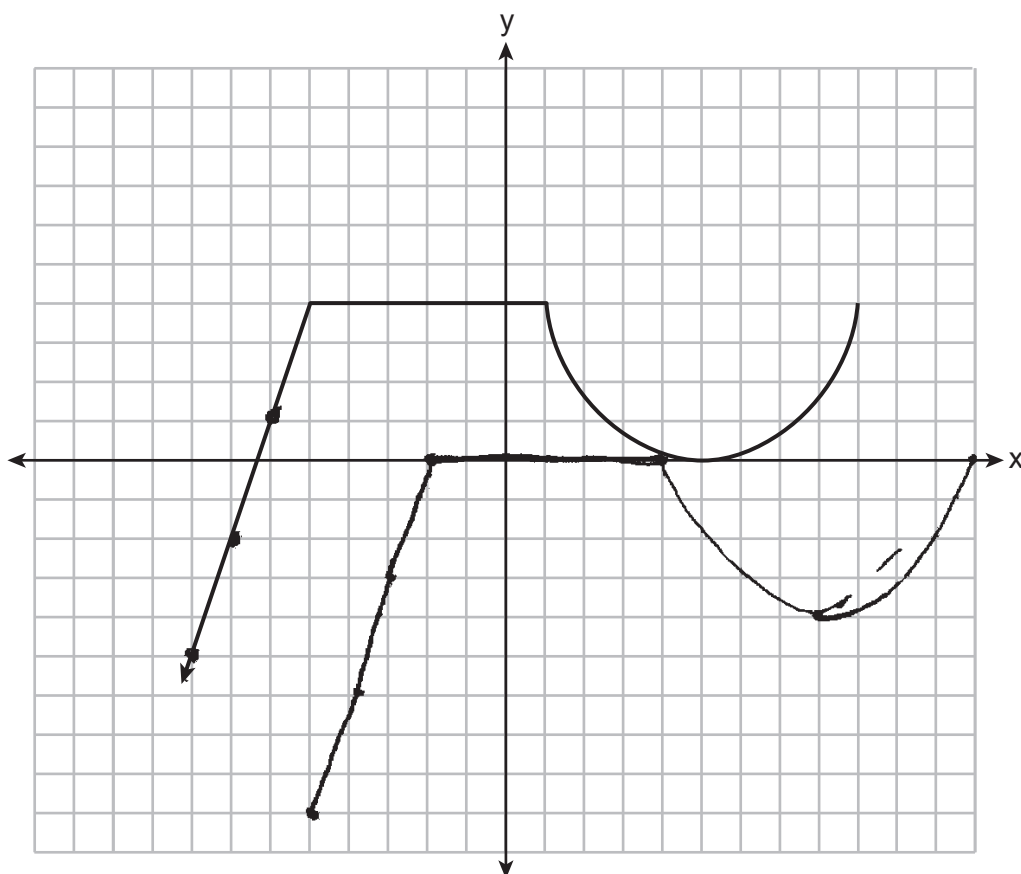
28 The graph of $y = f(x)$ is shown below. On the same set of axes, graph $y = f(x + 3) - 4$.



Score 1: The student made a graphing error translating the semicircle.

Question 28

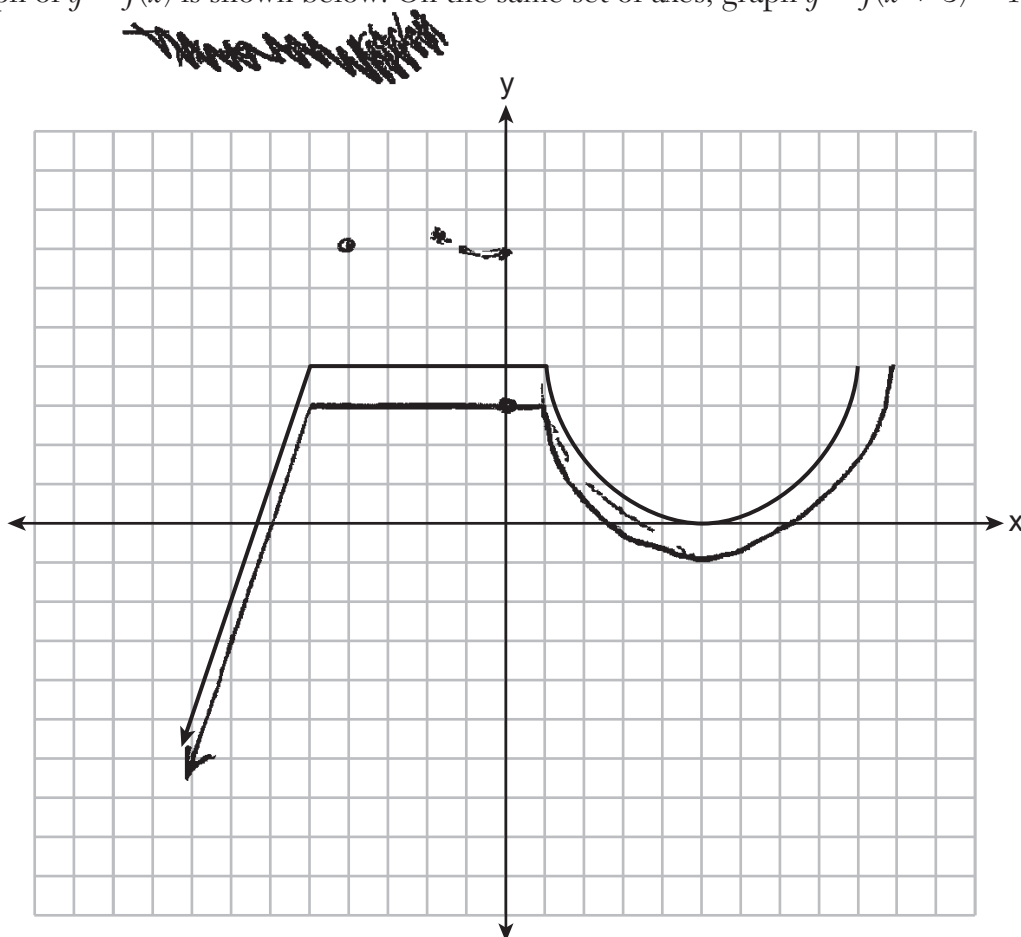
28 The graph of $y = f(x)$ is shown below. On the same set of axes, graph $y = f(x + 3) - 4$.



Score 0: The student made multiple graphing errors.

Question 28

28 The graph of $y = f(x)$ is shown below. On the same set of axes, graph $y = f(x + 3) - 4$.



Score 0: The student made multiple graphing errors.

Question 29

29 Express $(-2 + \sqrt{-25})^2$ in simplest $a + bi$ form. Justify your answer.

$$(-2 + 5i)^2$$

$$(-2 + 5i)(-2 + 5i)$$

$$4 - 10i - 10i + 25i^2$$

$$\boxed{-21 + (-20i)}$$

$$25i^2 - 20i + 4$$

$$-25 - 20i + 4$$

Score 2: The student gave a complete and correct response.

Question 29

29 Express $(-2 + \sqrt{-25})^2$ in simplest $a + bi$ form. Justify your answer.



$$\begin{aligned} &(-2 + 5i)^2 \\ &(-2 + 5i)(-2 + 5i) \\ &4 - 10i - 10i - 25 \\ &-20i - 21 \end{aligned}$$

Score 2: The student gave a complete and correct response.

Question 29

29 Express $(-2 + \sqrt{-25})^2$ in simplest $a + bi$ form. Justify your answer.

$$(-2 + \sqrt{-25}) (-2 + \sqrt{-25})$$

$$4 - 2\sqrt{-25} - 2\sqrt{-25} - 25$$

$$-4\sqrt{-25} - 21$$

$$-4i(5) - 21$$

$$-21 - 20i$$

$$21 + 20i$$

Score 1: The student's final answer is incorrect.

Question 29

29 Express $(-2 + \sqrt{-25})^2$ in simplest $a + bi$ form. Justify your answer.

Handwritten work:

$$\begin{aligned}
 & \cancel{(-2 + \sqrt{-25})} \\
 & \quad (4 + \\
 & \quad (-2 + \sqrt{-25}) \overset{-10i}{\cancel{(-2 + \sqrt{-25})}} \\
 & \quad \quad (4 - 10i - 10i + 25) \\
 & \quad \quad (4 - 20i + 25) \\
 & \quad \quad \downarrow \\
 & \quad \quad (29 - 20i)
 \end{aligned}$$

Score 1: The student made a computational error.

Question 29

29 Express $(-2 + \sqrt{-25})^2$ in simplest $a + bi$ form. Justify your answer.

$$\begin{array}{l} a + bi \\ (-2 + \sqrt{-25})^2 \\ -2 + 5i^2 \\ \text{---} \\ \boxed{-2 + 25i} \end{array}$$

Score 0: The student did not satisfy the criteria for one or more credits.

Question 29

29 Express $(-2 + \sqrt{-25})^2$ in simplest $a + bi$ form. Justify your answer.

$$\begin{aligned} & (-2 + \sqrt{-25})(-2 + \sqrt{-25}) \\ & \quad \quad \quad \cdot \sqrt{-1} \sqrt{25} \\ & (-2 + i\sqrt{25})(-2 + i\sqrt{25}) \\ & (-2 + 5i)(-2 + 5i) \\ & 4 + 25i^2 \end{aligned}$$

Score 0: The student made multiple errors.

Question 30

30 The most common radioactive form of cesium is cesium-137. The half-life of cesium-137 is 30 years.

Suppose 2.7 micrograms of cesium-137 are found in a soil sample. Write a function for the amount of cesium-137 remaining, $c(t)$, in micrograms, in terms of the number of years, t , since the soil sample was taken.

$$A_t = A_0 \left(\frac{1}{2}\right)^{\frac{t}{h}}$$

$$c(t) = 2.7 \left(\frac{1}{2}\right)^{\frac{t}{30}}$$

Score 2: The student gave a complete and correct response.

Question 30

30 The most common radioactive form of cesium is cesium-137. The half-life of cesium-137 is 30 years.

Suppose 2.7 micrograms of cesium-137 are found in a soil sample. Write a function for the amount of cesium-137 remaining, $c(t)$, in micrograms, in terms of the number of years, t , since the soil sample was taken.

$$c(t) = 2.7(0.5)^{t/30}$$

Score 2: The student gave a complete and correct response.

Question 30

30 The most common radioactive form of cesium is cesium-137. The half-life of cesium-137 is 30 years.

Suppose 2.7 micrograms of cesium-137 are found in a soil sample. Write a function for the amount of cesium-137 remaining, $c(t)$, in micrograms, in terms of the number of years, t , since the soil sample was taken.

$$y = 2.7 \left(\frac{1}{2}\right)^{\frac{x}{30}}$$

Score 1: The student used incorrect notation.

Question 30

- 30** The most common radioactive form of cesium is cesium-137. The half-life of cesium-137 is 30 years.

Suppose 2.7 micrograms of cesium-137 are found in a soil sample. Write a function for the amount of cesium-137 remaining, $c(t)$, in micrograms, in terms of the number of years, t , since the soil sample was taken.

$$2.7(0.5)^{\frac{t}{30}}$$

2.7 = initial rate

0.5 = half life

30 yrs = one half life

t = years

Score 1: The student wrote an expression.

Question 30

30 The most common radioactive form of cesium is cesium-137. The half-life of cesium-137 is 30 years.

Suppose 2.7 micrograms of cesium-137 are found in a soil sample. Write a function for the amount of cesium-137 remaining, $c(t)$, in micrograms, in terms of the number of years, t , since the soil sample was taken.

A handwritten scribble consisting of several overlapping horizontal lines, with the number '30' written at the end of the lines.

$$137 = 30 \left(\frac{1}{2} \right)^{\frac{t}{30}}$$

Score 0: The student made multiple errors.

Question 30

30 The most common radioactive form of cesium is cesium-137. The half-life of cesium-137 is 30 years.

Suppose 2.7 micrograms of cesium-137 are found in a soil sample. Write a function for the amount of cesium-137 remaining, $c(t)$, in micrograms, in terms of the number of years, t , since the soil sample was taken.

$$(2.7) \div 2^{\frac{t}{30}}$$

Score 0: The student made multiple errors.

Question 31

31 Solve algebraically for x:

$$\sum_{a=0}^4 (ax - 3) = 5$$

$$(0x - 3) + (1x - 3) + (2x - 3) + (3x - 3) + (4x - 3) = 5$$

$$-3 + \boxed{x} - 3 + \boxed{2x} - 3 + \boxed{3x} - 3 + \boxed{4x} - 3 = 5$$

$$10x - 15 = 5$$

$$\frac{10x}{10} = \frac{20}{10}$$

$$\boxed{x = 2}$$

Score 2: The student gave a complete and correct response.

Question 31

31 Solve algebraically for x :

$$\sum_{a=0}^4 (ax - 3) = 5$$

$$\left. \begin{array}{l} a = 0 \\ a = 1 \\ a = 2 \\ a = 3 \\ a = 4 \end{array} \right\} 5$$

$$S_n = \frac{n(a_1 + a_n)}{2}$$

$$\left. \begin{array}{l} 0(x) - 3 = \\ 1(x) - 3 = \\ 2(x) - 3 = \\ 3(x) - 3 = \\ 4(x) - 3 = \end{array} \right\} 5$$

$$5 = \frac{5(-3 + 4x - 3)}{2}$$

$$10 = 5(-3 + 4x - 3)$$

$$2 = -3 + 4x - 3$$

$$2 = 4x - 6$$

$$8 = 4x$$

$$x = 2$$

$$\cancel{-3} + \cancel{1(x) - 3} + \cancel{2(x) - 3} + \cancel{3(x) - 3} + \cancel{4(x) - 3} = 5$$

$$-15 + 10x = 5$$

$$10x = 20$$

$$\boxed{x = 2}$$

Score 2: The student gave a complete and correct response.

Question 31

31 Solve algebraically for x:

$$\sum_{a=0}^4 (ax - 3) = 5$$

$$(0x - 3) = 5$$

$$(1x - 3) = 5$$

$$(2x - 3) = 5$$

$$(3x - 3) = 5$$

$$(4x - 3) = 5$$

+

$$\begin{array}{r} (10x - 15) = 25 \\ +15 \quad +15 \end{array}$$

$$\frac{10x = 40}{10} \quad x = 4$$

Score 1: The student made a conceptual error.

Question 31

31 Solve algebraically for x :

$$\sum_{a=0}^4 (ax - 3) = 5$$

$x = 2$

$$\begin{aligned}(0x - 3) &= -3 \\ (1x - 3) &= -1 \\ (2x - 3) &= 1 \\ (3x - 3) &= 3 \\ (4x - 3) &= 5\end{aligned}$$

$x = 2$

Score 1: The student used a method other than algebraic.

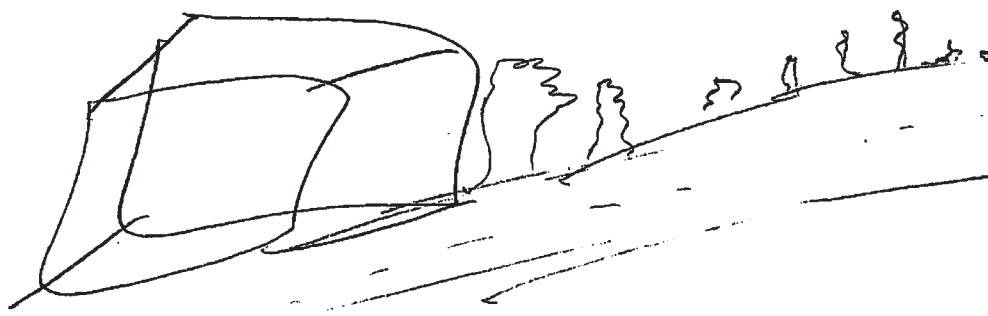
Question 31

31 Solve algebraically for x :

$$\sum_{a=0}^4 (ax - 3) = 5$$

~~$$4(0x - 3) = 5$$
$$(-12) = 5$$~~

~~$$4(x - 3) = 5$$
$$+6 \quad +3$$
$$4x = 8$$
$$\frac{4x}{4} = \frac{8}{4}$$
$$x = 2$$~~



Score 0: The student obtained a correct response by an obviously incorrect procedure.

Question 31

31 Solve algebraically for x:

$$\sum_{a=0}^4 (ax - 3) = 5$$

$$\begin{array}{l|l} 4 & (ax-3)=5 \\ \hline 0 & (0x-3)=5 \\ 1 & (1x-3)=5 \\ 2 & (2x-3)=5 \\ 3 & (3x-3)=5 \\ 4 & (4x-3)=5 \\ \hline & (10x-15)=25 \end{array}$$

$$\sqrt{10x-15} = \sqrt{25}$$

$$\begin{array}{r} 10x-15 = 5 \\ +15 \quad +15 \\ \hline \end{array}$$

$$\begin{array}{r} 10x = 20 \\ \hline 10 \quad 10 \end{array}$$

$$\underline{x = 2}$$

Score 0: The student made multiple errors and obtained a correct response by an obviously incorrect procedure.

Question 32

32 Given the exponential function $y = 5.381e^{0.214x}$, rewrite the function in the form of $y = a(b)^x$, rounding values to the *nearest thousandth*.

$$y = 5.381(1.239)^x$$
$$e^{0.214} = 1.239$$

Score 2: The student gave a complete and correct response.

Question 32

32 Given the exponential function $y = 5.381e^{0.214x}$, rewrite the function in the form of $y = a(b)^x$, rounding values to the *nearest thousandth*.

$$y = 5.381(1.239)^x$$

Score 2: The student gave a complete and correct response.

Question 32

32 Given the exponential function $y = 5.381e^{0.214x}$, rewrite the function in the form of $y = a(b)^x$, rounding values to the nearest thousandth.

$$\begin{aligned} y &= 5.381(e)^{0.214x} & y &= 5.381 \cdot 1.239^x \\ y &= 14.627^{0.214x} \\ y &= 1.776^x \end{aligned}$$

Score 1: The student did not clearly indicate their final answer.

Question 32

32 Given the exponential function $y = 5.381e^{0.214x}$, rewrite the function in the form of $y = a(b)^x$, rounding values to the nearest thousandth.

$$5.381e^{0.214x} \qquad 5.381e^{0.214(1)} = 6.665028$$

$$5.381(b)^x = 5.381e^{0.214x} \qquad \frac{6.665028}{5.381} = 1.2386$$

$$\boxed{5.381(1.239)^x} = 5.381e^{0.214x}$$

$$a^{bc} = (a^b)^c$$

$$5.381e^{0.214x} = (5.381e^{0.214})^x$$

Score 1: The student wrote an expression.

Question 32

32 Given the exponential function $y = 5.381e^{0.214x}$, rewrite the function in the form of $y = a(b)^x$, rounding values to the *nearest thousandth*.

$$f(x) = 5.381(1.2386)^x$$

$$f(x) = 6.665^x$$

Score 0: The student made a conceptual and notational error.

Question 32

32 Given the exponential function $y = 5.381e^{0.214x}$, rewrite the function in the form of $y = a(b)^x$, rounding values to the *nearest thousandth*.

$$14.627^{.214x}$$

Score 0: The student made multiple errors.

Question 33

33 Determine the quotient and remainder of the expression below.

$$\frac{2x^4 - 27x^2 + 33x - 8}{x^2 + 3x - 5}$$

Express the result in the form $q(x) + \frac{r(x)}{d(x)}$.

$$\begin{array}{r}
 2x^2 - 6x + 1 \\
 \overline{x^2 + 3x - 5 \over 2x^4 + 0x^3 - 27x^2 + 33x - 8} \\
 \underline{-2x^4 + 6x^3 + 10x^2} \\
 -6x^3 - 17x^2 + 33x \\
 \underline{+6x^3 + 18x^2 + 30x} \\
 x^2 + 3x - 8 \\
 \underline{-x^2 + 3x + 5} \\
 -3
 \end{array}$$

$2x^2 - 6x + 1 - \frac{3}{x^2 + 3x - 5}$

Score 4: The student gave a complete and correct response.

Question 33

33 Determine the quotient and remainder of the expression below.

$$\frac{2x^4 - 27x^2 + 33x - 8}{x^2 + 3x - 5}$$

Express the result in the form $q(x) + \frac{r(x)}{d(x)}$.

$$\begin{array}{r} x^2 + 3x - 5 \overline{) 2x^4 - 27x^2 + 33x - 8} \\ \underline{2x^4 - 6x^3 + 10x^2} \\ -6x^3 - 17x^2 + 33x - 8 \\ \underline{+ 6x^3 + 18x^2 - 30x} \\ x^2 + 3x - 8 \\ \underline{- x^2 - 3x + 5} \\ -3 \end{array}$$

$$\frac{2x^4 - 27x^2 + 33x - 8}{x^2 + 3x - 5} = 2x^2 - 6x + 1 + \left(\frac{-3}{x^2 + 3x - 5} \right)$$

Score 4: The student gave a complete and correct response.

Question 33

33 Determine the quotient and remainder of the expression below.

$$\frac{2x^4 - 27x^2 + 33x - 8}{x^2 + 3x - 5}$$

Express the result in the form $q(x) + \frac{r(x)}{d(x)}$.

$$\begin{array}{r}
 2x^2 - 6x + 1 \\
 x^2 + 3x - 5 \overline{) 2x^4 + 0x^3 - 27x^2 + 33x - 8} \\
 \underline{+ -2x^4 + 6x^3 + 10x^2} \downarrow \\
 -6x^3 - 17x^2 + 33x \downarrow \\
 \underline{+ 6x^3 + 18x^2 + 30x} \downarrow \\
 x^2 + 63x - 8 \\
 \underline{+ -x^2 - 3x + 5} \\
 60x - 3
 \end{array}$$

$$2x^2 - 6x + 1 + \frac{60x - 3}{x^2 + 3x - 5}$$

Score 3: The student made one computational error.

Question 33

33 Determine the quotient and remainder of the expression below.

$$\frac{2x^4 - 27x^2 + 33x - 8}{x^2 + 3x - 5}$$

Express the result in the form $q(x) + \frac{r(x)}{d(x)}$.

~~$2x^2 - 6x + 1$~~

$$\begin{array}{r}
 2x^2 - 6x + 1 \\
 \hline
 x^2 + 3x - 5 \overline{) 2x^4 + 0x^3 - 27x^2 + 33x - 8} \\
 \underline{-(x^2 + 3x - 5)} \\
 -6x^3 - 17x^2 + 33x \\
 \underline{-(6x^3 + 18x^2 - 30x)} \\
 -3x^2 + 3x - 8 \\
 \underline{-(x^2 + 3x - 5)} \\
 -3
 \end{array}$$

~~$x = \frac{3 \pm \sqrt{9 - 4(-5)}}{2}$~~

~~$x = \frac{3 \pm \sqrt{29}}{2}$~~

Score 3: The student did not express the result in $q(x) + \frac{r(x)}{d(x)}$ form.

Question 33

33 Determine the quotient and remainder of the expression below.

$$\frac{2x^4 - 27x^2 + 33x - 8}{x^2 + 3x - 5}$$

Express the result in the form $q(x) + \frac{r(x)}{d(x)}$

$$\begin{array}{r} x^2+3x-5 \overline{) 2x^4-27x^2+33x-8} \\ \underline{-(2x^4+6x^3-10x^2)} \\ -6x^3-17x^2+33x-8 \\ \underline{-(-6x^3-18x^2+30x)} \\ x^2-3x-8 \\ \underline{-(x^2+3x-5)} \\ -6x-3 \end{array}$$

$$2x^2 - 6x + 1 + \frac{-6x-3}{2x^4-27x^2+33x-8}$$

Score 2: The student made a computational error and wrote an incorrect $d(x)$.

Question 33

33 Determine the quotient and remainder of the expression below.

$$\frac{2x^4 - 27x^2 + 33x - 8}{x^2 + 3x - 5}$$

Express the result in the form $q(x) + \frac{r(x)}{d(x)}$.

$$\begin{array}{r}
 2x^4 - 27x^2 + 33x - 8 \\
 \hline
 x^2 + 3x - 5
 \end{array}$$

Handwritten work shows two methods of polynomial division. The left method is a long division process with multiple steps, including subtraction and bringing down terms, leading to a remainder of $32x - 48$. The right method is a more compact representation of the same process, also resulting in a remainder of $32x - 48$.

$$\begin{array}{r}
 2x^2 - 3x - 8 \\
 \hline
 x^2 + 3x - 5
 \end{array}$$

$$2x^2 - 3x - 8 + \frac{32x - 48}{x^2 + 3x - 5}$$

Score 2: The student made two unique computational errors.

Question 33

33 Determine the quotient and remainder of the expression below.

$$\frac{2x^4 - 27x^2 + 33x - 8}{x^2 + 3x - 5}$$

Express the result in the form $q(x) + \frac{r(x)}{d(x)}$.

Handwritten work for the polynomial division:

Attempt 1 (top):

$$\begin{array}{r} 2x^2 - 6x - 9 \\ x^2 + 3x - 5 \overline{) 2x^4 + 0x^3 - 27x^2 + 33x - 8} \\ \underline{-(2x^4 + 6x^3)} \\ -6x^3 - 27x^2 + 33x \\ \underline{-(-6x^3 - 18x^2)} \\ 9x^2 + 51x - 8 \end{array}$$

Attempt 2 (bottom):

$$\begin{array}{r} 2x^2 - 6x - 9 \\ x^2 + 3x - 5 \overline{) 2x^4 + 0x^3 - 27x^2 + 33x - 8} \\ \underline{-(2x^4 + 6x^3)} \\ -6x^3 - 27x^2 + 33x \\ \underline{-(-6x^3 - 18x^2)} \\ 9x^2 + 51x - 8 \end{array}$$

Circled expression:

$$2x^2 - 6x - 9$$

Score 1: The student made the same conceptual error distributing, and did not express their result in $q(x) + \frac{r(x)}{d(x)}$ form.

Question 33

33 Determine the quotient and remainder of the expression below.

$$\frac{2x^4 - 27x^2 + 33x - 8}{x^2 + 3x - 5}$$

Express the result in the form $q(x) + \frac{r(x)}{d(x)}$.

$$\begin{array}{r} 2x^2 + 11x + 11 \\ \underline{2x^2 + 27x^2 + 33x - 8} \\ -12x^2 + 6x^3 - 10x^2 \end{array}$$

$$\begin{array}{r} 27 + 16 \\ \hline x^2 + 3x - 5 \sqrt{2x^4 - 27x^2 + 33x - 8} \\ - \quad \quad + 27x^2 + 81x + 135 \\ \hline 2x^4 \quad - 48x \quad + 127 \\ \hline \end{array}$$

$$43 + \frac{2x^4 + 207}{x^2 + 3x - 5}$$

Score 0: The student's response did not contain enough relevant course-level work to receive any credit.

Question 33

33 Determine the quotient and remainder of the expression below.

$$\frac{2x^4 - 27x^2 + 33x - 8}{x^2 + 3x - 5}$$

Express the result in the form $q(x) + \frac{r(x)}{d(x)}$.

Handwritten work for the polynomial division:

$$\begin{array}{r}
 2x^2 + x^2 + x^2 + 11 \\
 x^2 + 3x - 5 \overline{) 2x^4 + 0x^3 - 2x^2 + 33x - 8} \\
 \underline{-(2x^4 - x^5)} \\
 x^2 - 2x^2 \\
 \underline{+ x^2 - 2x^2} \\
 4x^2 + 33x \\
 \underline{-(4x^2 - 33x)} \\
 8
 \end{array}$$

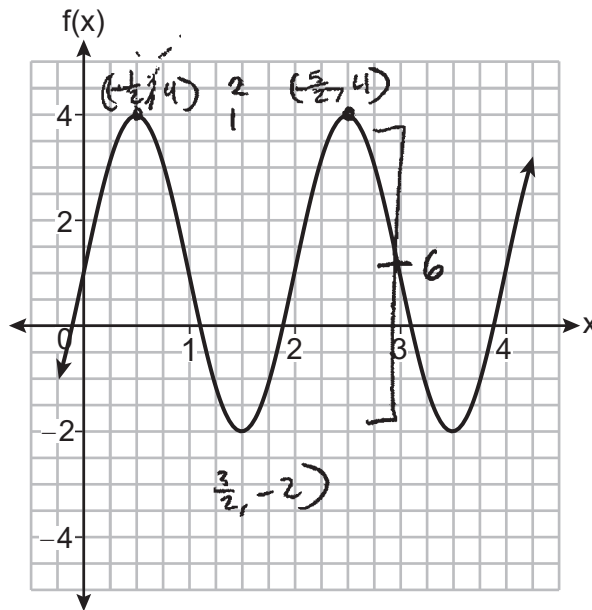
The student has circled the remainder 8 and written the final result as:

$$2x^2 + x^2 + x^2 + 11 + \frac{8}{x^2 + 3x - 5}$$

Score 0: The student did not satisfy the criteria for one or more credits.

Question 34

34 The sinusoidal function f is graphed below.



$$a = \frac{6}{2} = 3$$

State the period of the function f .

$$\frac{5}{2} - \frac{1}{2} = 2$$

Period of function f is 2

State the amplitude of the function f .

Amplitude of function f is 3

Write the equation in the form $f(x) = A \sin(Bx) + D$ to represent the sinusoidal function.

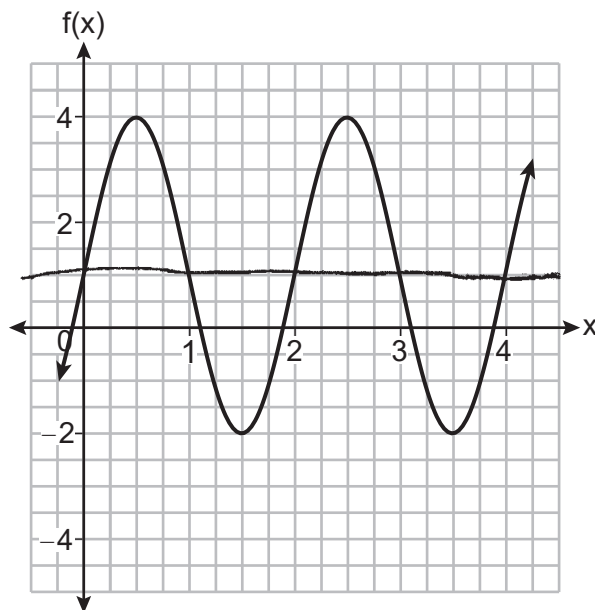
$$f(x) = 3 \sin(\pi x) + 1$$

$$\begin{aligned} \frac{2\pi}{B} &= \frac{2}{1} \\ \frac{2\pi}{2} &= \frac{2B}{2} \\ B &= \pi \end{aligned}$$

Score 4: The student gave a complete and correct response.

Question 34

34 The sinusoidal function f is graphed below.



State the period of the function f .

2

State the amplitude of the function f .

3

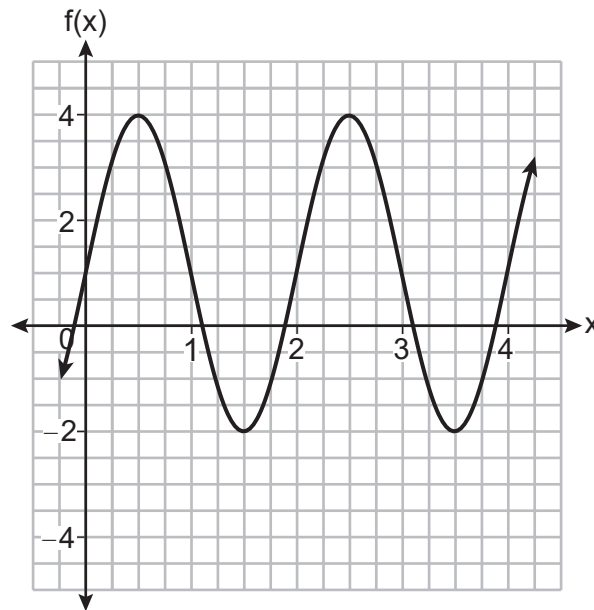
Write the equation in the form $f(x) = A \sin(Bx) + D$ to represent the sinusoidal function.

$$f(x) = 3\sin(\pi x) + 1$$

Score 4: The student gave a complete and correct response.

Question 34

34 The sinusoidal function f is graphed below.



State the period of the function f .

$$P = 2.5$$

State the amplitude of the function f .

$$A = 3$$

$$A = \frac{\text{max} - \text{min}}{2}$$

$$A = \frac{4 - (-2)}{2} = 3$$

Write the equation in the form $f(x) = A \sin(Bx) + D$ to represent the sinusoidal function.

$$f(x) = 3 \sin(0.8\pi x) + 1$$

$$D = \frac{\text{max} + \text{min}}{2} = \frac{4 + (-2)}{2} = 1$$

$$A = 3$$

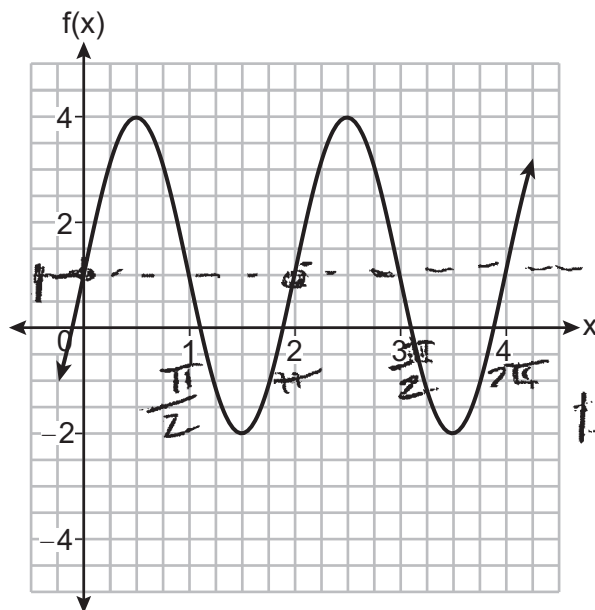
$$D = 1$$

$$B = \frac{2\pi}{2.5} = 0.8\pi$$

Score 3: The student made an error calculating the period.

Question 34

34 The sinusoidal function f is graphed below.



up 6 down 6
1 is the midline

State the period of the function f .

2 is the period

State the amplitude of the function f .

3...something idk no specific units

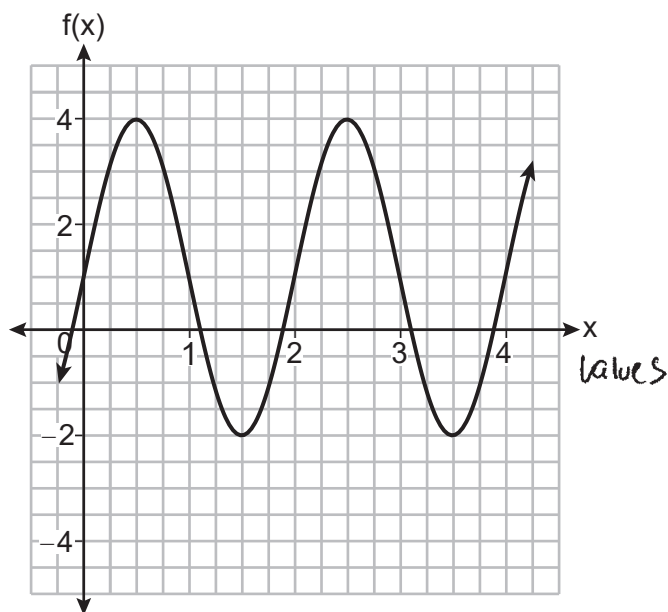
Write the equation in the form $f(x) = A \sin(Bx) + D$ to represent the sinusoidal function.

$$f(x) = 3 \sin(x) + 1$$

Score 3: The student wrote an incorrect B value.

Question 34

34 The sinusoidal function f is graphed below.



State the period of the function f .

$$\text{Period} = \frac{2\pi}{B}$$

$$\text{Period} = 2$$

State the amplitude of the function f .

$$4$$

$$\frac{2}{1} = \frac{2\pi}{B}$$

$$\frac{2x}{2} = \frac{2\pi}{2}$$

$$x = \pi$$

$$B$$

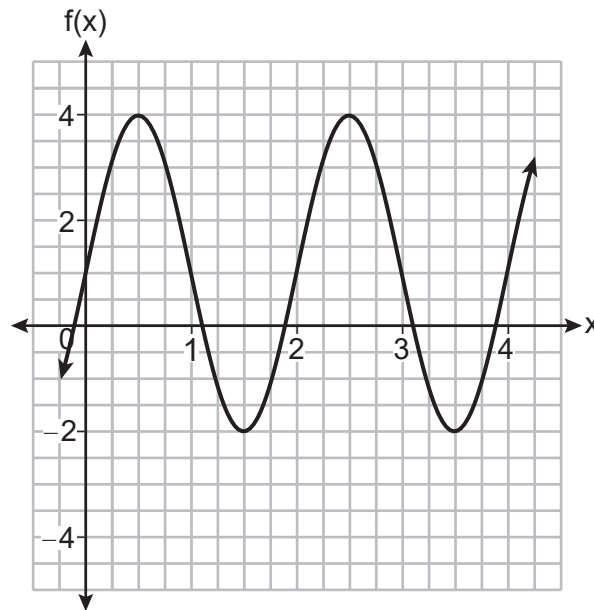
Write the equation in the form $f(x) = A \sin(Bx) + D$ to represent the sinusoidal function.

$$f(x) = 4 \sin \pi x + 2$$

Score 2: The student stated an incorrect amplitude and midline.

Question 34

34 The sinusoidal function f is graphed below.



$$2\pi$$

$$\frac{6\pi \div 3}{3 \div 3}$$

$$6 \div 36 \div \left(\frac{\pi}{180} \right)$$

$$6 \div$$

State the period of the function f .

$$2\pi$$

State the amplitude of the function f .

$$\text{The amplitude} = 3$$

Write the equation in the form $f(x) = A \sin(Bx) + D$ to represent the sinusoidal function.

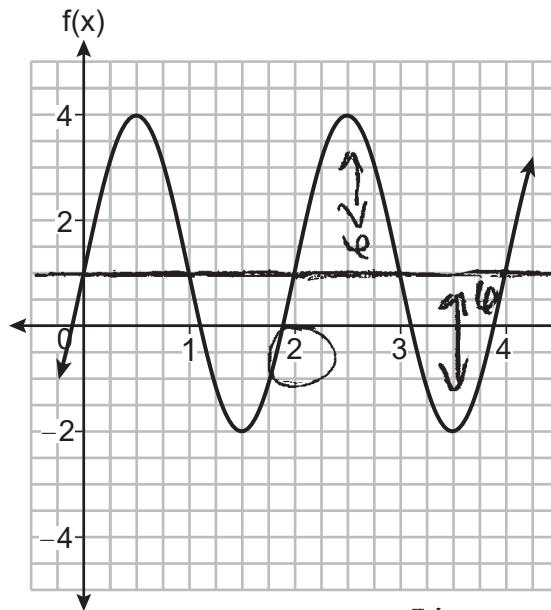
$$f(x) = 3 \sin(2x) + 1$$

$$\begin{matrix} a \\ b \\ c \\ d \end{matrix}$$

Score 2: The student incorrectly determined the period and B .

Question 34

34 The sinusoidal function f is graphed below.



midline 1
amplitude
 $|A| = 6$

$$B \cdot P = 2\pi$$

$$P = 2$$

$$B \cdot P = 2\pi$$

$$\frac{2}{2} \cdot P = \frac{2\pi}{2}$$

$$\pi$$

$\frac{\pi}{4}$ - count on x-axis

Sin grap

State the period of the function f .

$$\underline{P = 2}$$

State the amplitude of the function f .

Amplitude is 6

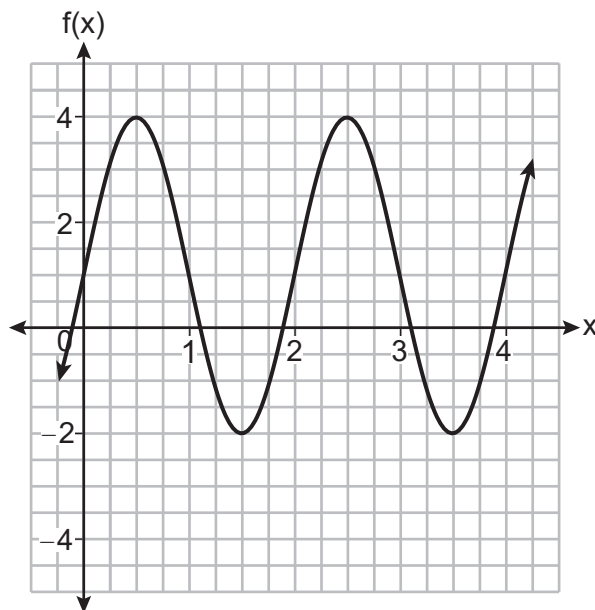
Write the equation in the form $f(x) = A \sin(Bx) + D$ to represent the sinusoidal function.

$$y = 6 \sin(\pi x) + 2$$

Score 1: The student correctly determined the period.

Question 34

34 The sinusoidal function f is graphed below.



State the period of the function f .

$$\text{Per.} = \frac{2\pi}{b} = \frac{2\pi}{3} \quad a = 6 \quad 6 \div 2 = 3$$

State the amplitude of the function f .

$$a = 6$$

Write the equation in the form $f(x) = A \sin(Bx) + D$ to represent the sinusoidal function.

$$f(x) = 6 \sin\left(\frac{2\pi}{3}(x)\right) + 1$$

Score 1: The student earned one credit for the equation.

Question 34

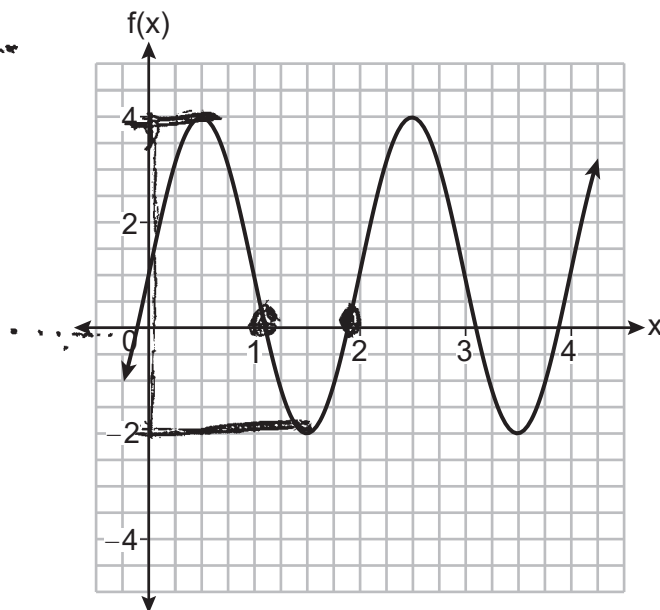
34 The sinusoidal function f is graphed below.

2 Anchors

$$D = \frac{2}{\pi}$$

B

A
B
M



sin

4

State the period of the function f .

2π

State the amplitude of the function f .

4

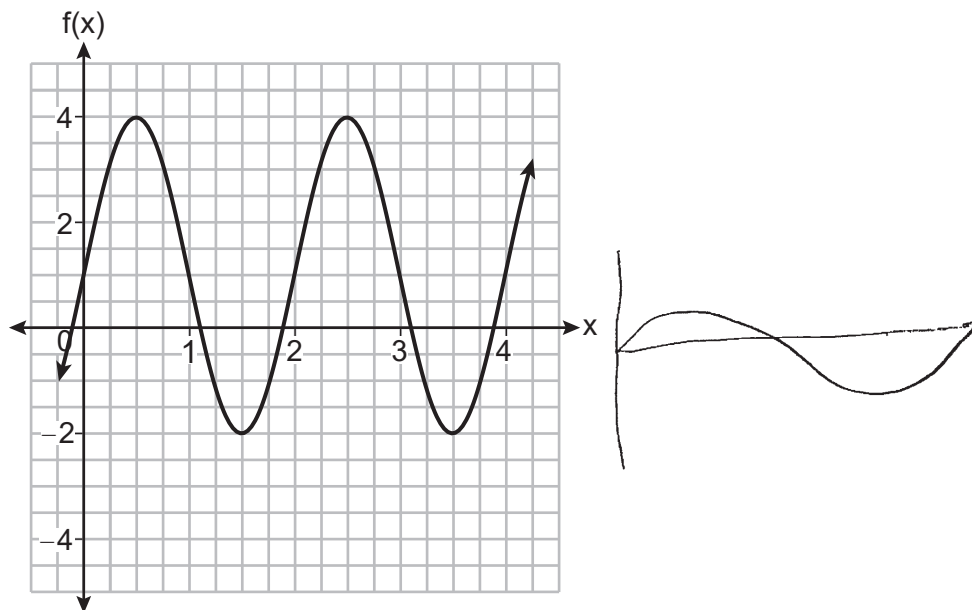
Write the equation in the form $f(x) = A \sin(Bx) + D$ to represent the sinusoidal function.

$$4 \sin\left(\frac{\pi}{2}x\right) + 2$$

Score 0: The student did not satisfy the criteria for one or more credits.

Question 34

34 The sinusoidal function f is graphed below.



State the period of the function f .

The period of the function
is 4.

State the amplitude of the function f .

Amp = 6

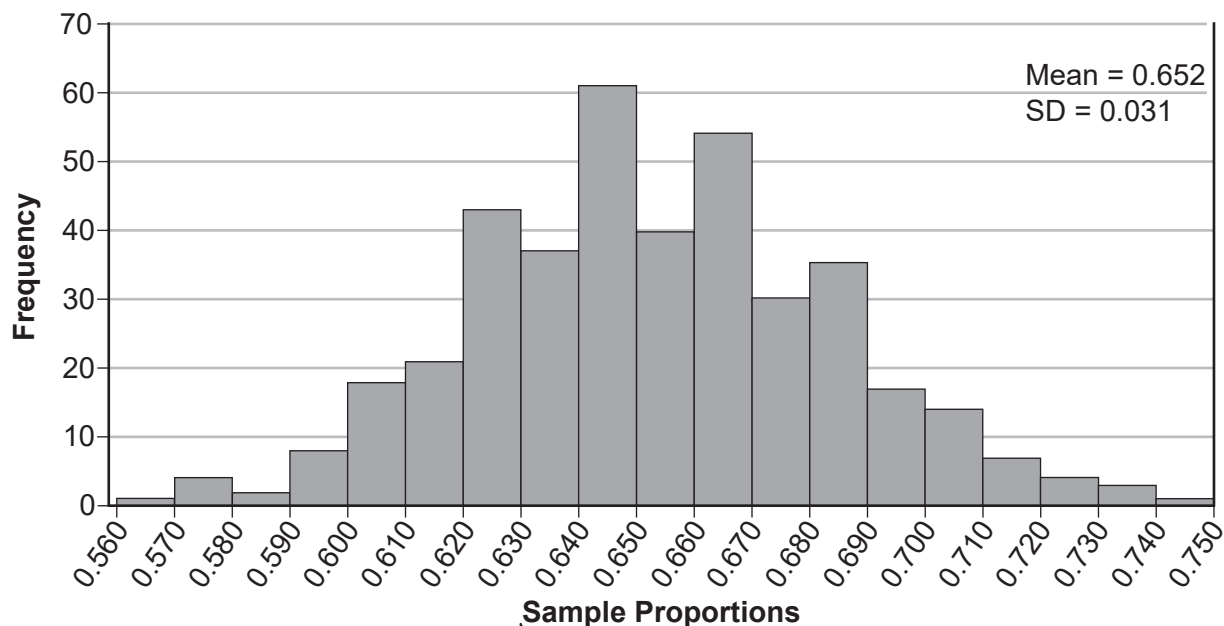
Write the equation in the form $f(x) = A \sin(Bx) + D$ to represent the sinusoidal function.

$$f(x) = 6 \cos(4x) - 2$$

Score 0: The student did not satisfy the criteria for one or more credits.

Question 35

- 35 A principal wonders what percentage of parents at her large high school restrict their child's cell phone privileges. The school surveys a random sample of 250 parents at the school and finds that 65% of them restrict their child's cell phone privileges. The school runs a simulation with 400 samples of 250 parents, assuming that 65% of them restrict cell phone privileges. The simulation results are shown below.



Use the simulation to determine an interval containing the middle 95% of simulated proportions. Justify your answer. Round all values to the *nearest hundredth*.

$$0.031 \cdot 2 = 0.062 \quad 0.652 + 0.062 = 0.714$$

$$0.652 - 0.062 = 0.59$$

$$(0.59 - 0.71)$$

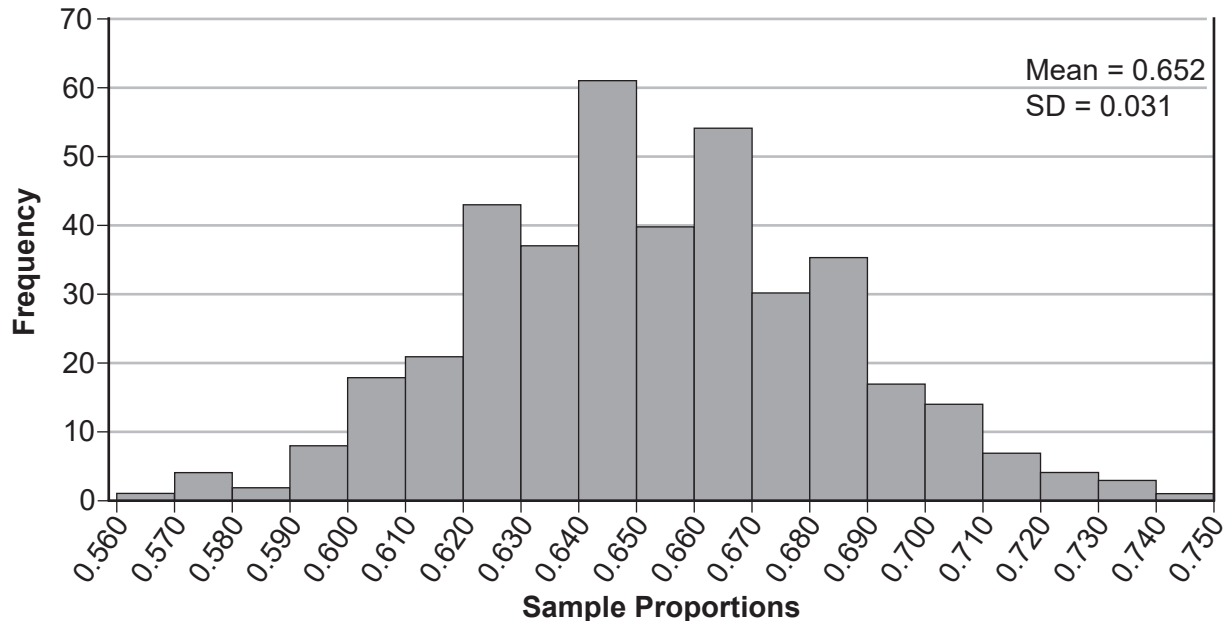
The school district's superintendent worries that less than half of parents restrict their child's cell phone privileges. Do the simulation results support the superintendent's concern? Explain.

No because the lowest the sample proportions go is 0.560 which is still more than half so anything less than 0.5 would be miniscule.

Score 4: The student gave a complete and correct response.

Question 35

35 A principal wonders what percentage of parents at her large high school restrict their child's cell phone privileges. The school surveys a random sample of 250 parents at the school and finds that 65% of them restrict their child's cell phone privileges. The school runs a simulation with 400 samples of 250 parents, assuming that 65% of them restrict cell phone privileges. The simulation results are shown below.



Use the simulation to determine an interval containing the middle 95% of simulated proportions. Justify your answer. Round all values to the *nearest hundredth*.

$$0.652 \pm 2(0.031)$$
$$(.59, .714) \quad (.59, .71)$$

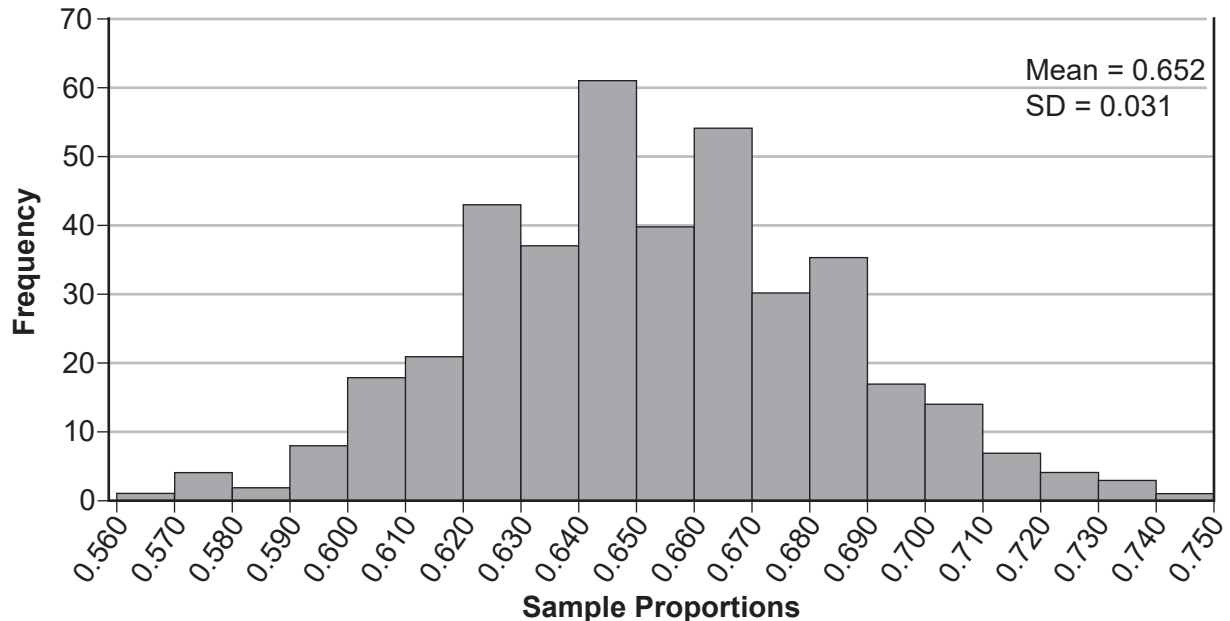
The school district's superintendent worries that less than half of parents restrict their child's cell phone privileges. Do the simulation results support the superintendent's concern? Explain.

no because 50% falls
below the 59%-71% interval.

Score 4: The student gave a complete and correct response.

Question 35

35 A principal wonders what percentage of parents at her large high school restrict their child's cell phone privileges. The school surveys a random sample of 250 parents at the school and finds that 65% of them restrict their child's cell phone privileges. The school runs a simulation with 400 samples of 250 parents, assuming that 65% of them restrict cell phone privileges. The simulation results are shown below.



Use the simulation to determine an interval containing the middle 95% of simulated proportions. Justify your answer. Round all values to the *nearest hundredth*.

.59 to .71

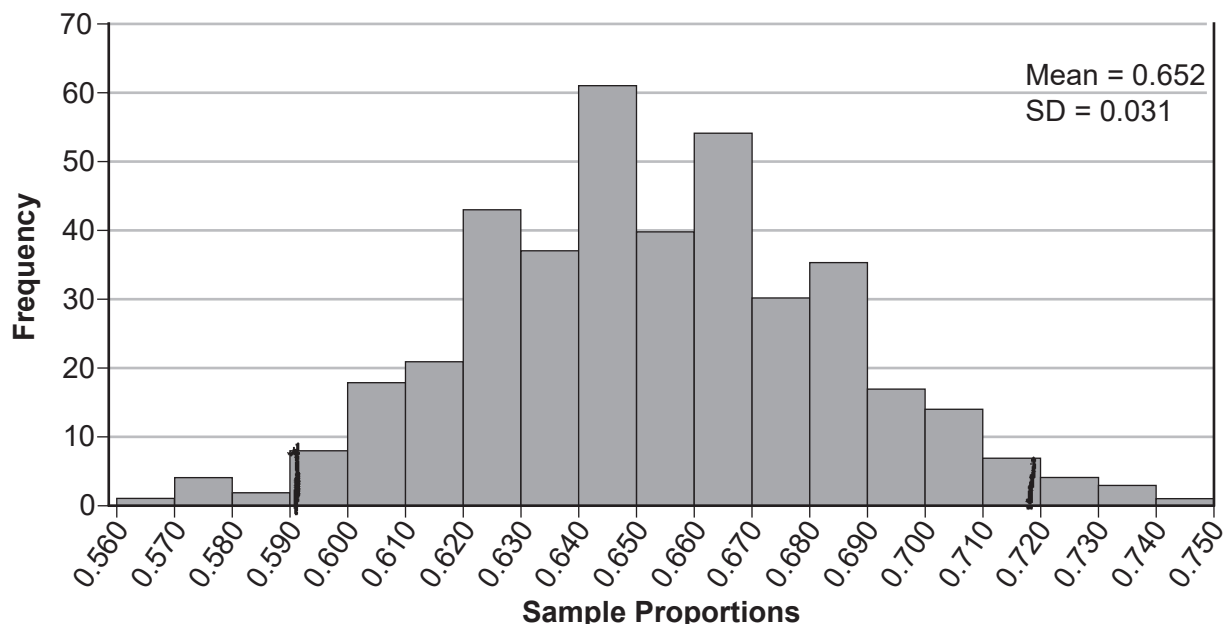
The school district's superintendent worries that less than half of parents restrict their child's cell phone privileges. Do the simulation results support the superintendent's concern? Explain.

No.
The plausible outcomes are all more than 50%, so it would be statistically significant for less than 1/2 to restrict.

Score 3: The student did not show work to determine the interval.

Question 35

35 A principal wonders what percentage of parents at her large high school restrict their child's cell phone privileges. The school surveys a random sample of 250 parents at the school and finds that 65% of them restrict their child's cell phone privileges. The school runs a simulation with 400 samples of 250 parents, assuming that 65% of them restrict cell phone privileges. The simulation results are shown below.



Use the simulation to determine an interval containing the middle 95% of simulated proportions. Justify your answer. Round all values to the nearest hundredth.

~~mean = 0.652, SD = 0.031~~
 ~~$0.652 \pm (2)(0.031)$~~
 ~~0.652 ± 0.062~~
 ~~$0.590 - 0.714$~~
 $0.59, 0.714$

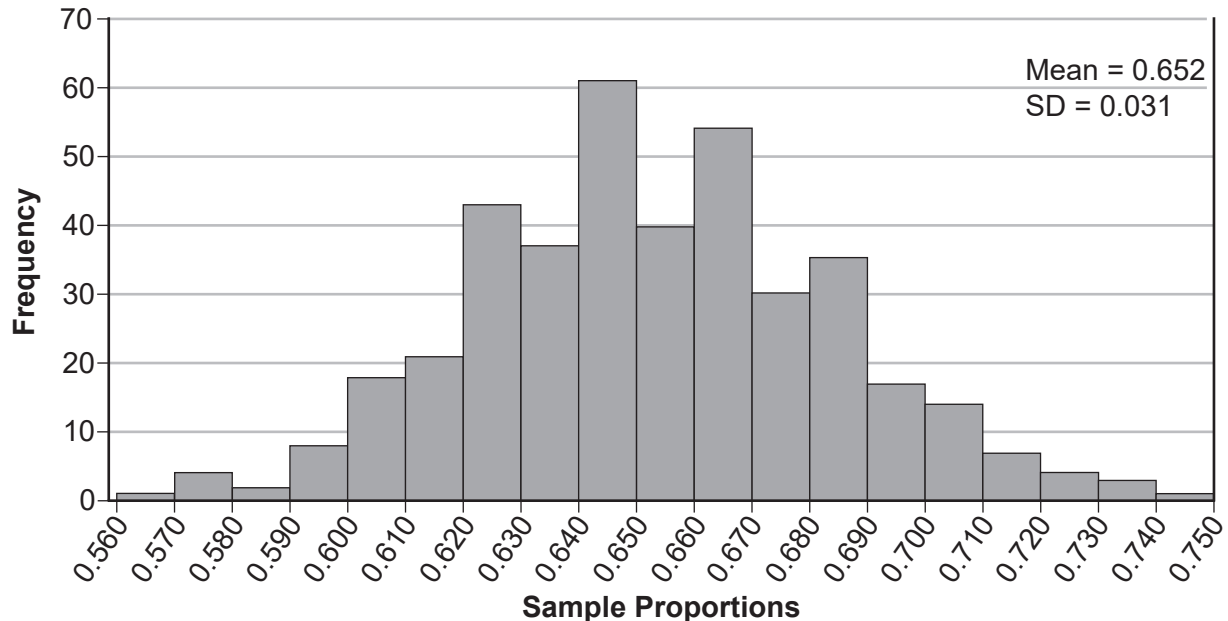
The school district's superintendent worries that less than half of parents restrict their child's cell phone privileges. Do the simulation results support the superintendent's concern? Explain.

no, since every number
 in the 95% interval
 is above .5 we have
 statistical evidence that
 the majority of parents restrict
 their child's cell phone privileges

Score 3: The student did not round to the nearest hundredth.

Question 35

- 35 A principal wonders what percentage of parents at her large high school restrict their child's cell phone privileges. The school surveys a random sample of 250 parents at the school and finds that 65% of them restrict their child's cell phone privileges. The school runs a simulation with 400 samples of 250 parents, assuming that 65% of them restrict cell phone privileges. The simulation results are shown below.



Use the simulation to determine an interval containing the middle 95% of simulated proportions. Justify your answer. Round all values to the *nearest hundredth*.

$$(.59, .71)$$

$$0.652 \pm 2(0.031)$$

$$0.652 \pm .062$$

$$0.652 + .062$$

$$.714$$

$$0.652 - .062$$

$$.59$$

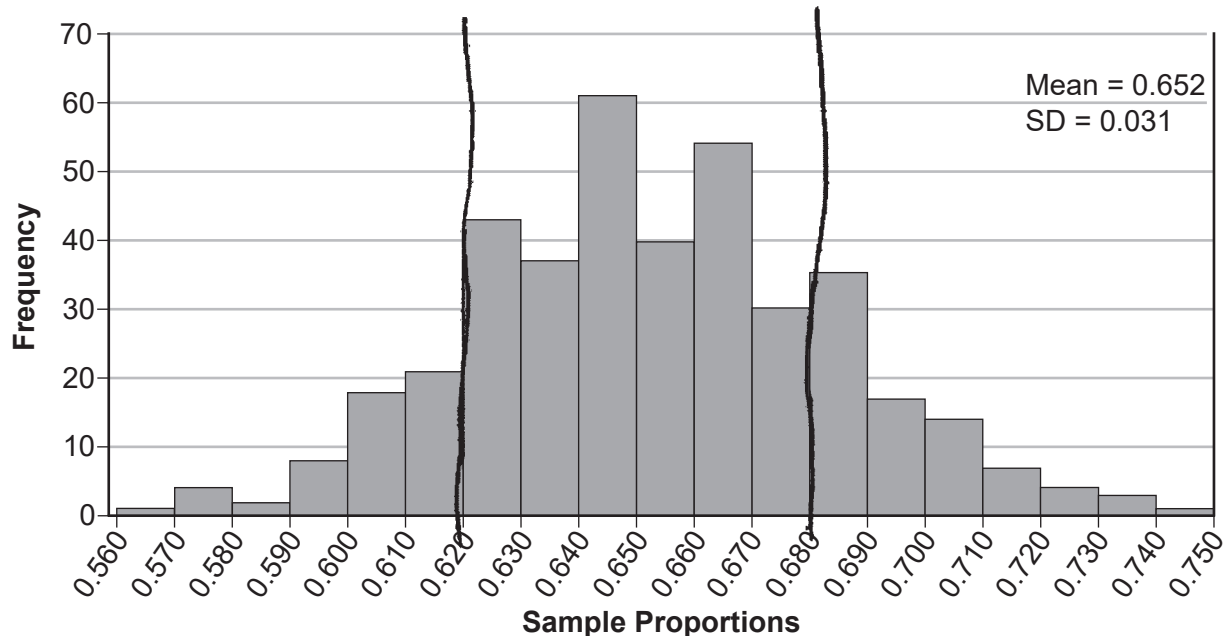
The school district's superintendent worries that less than half of parents restrict their child's cell phone privileges. Do the simulation results support the superintendent's concern? Explain.

Yes because the interval of 95% is less than half.

Score 2: The student's explanation is incorrect.

Question 35

35 A principal wonders what percentage of parents at her large high school restrict their child's cell phone privileges. The school surveys a random sample of 250 parents at the school and finds that 65% of them restrict their child's cell phone privileges. The school runs a simulation with 400 samples of 250 parents, assuming that 65% of them restrict cell phone privileges. The simulation results are shown below.



Use the simulation to determine an interval containing the middle 95% of simulated proportions. Justify your answer. Round all values to the nearest hundredth.

$$1.95 = 250(+ - 2SD) \quad (0.62, 0.68)$$

$$0.652 + 0.031 = 0.683$$

$$0.652 - 0.031 = 0.621$$

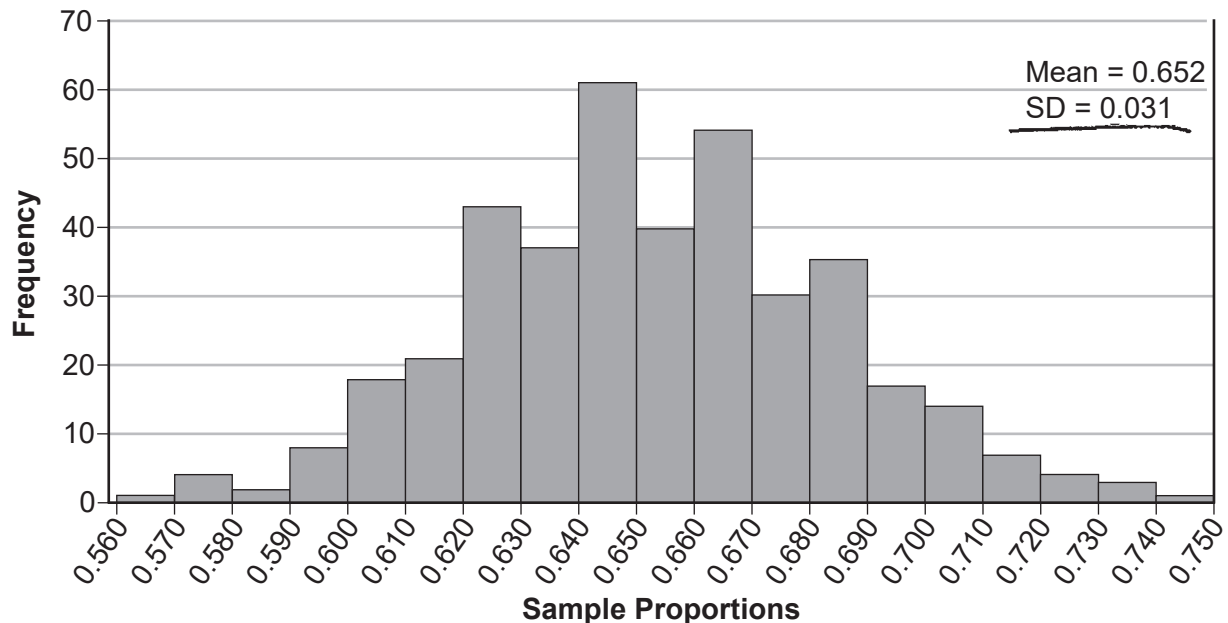
The school district's superintendent worries that less than half of parents restrict their child's cell phone privileges. Do the simulation results support the superintendent's concern? Explain.

The simulation results does not support the superintendent concern because I compared 50% to the interval.

Score 2: The student calculated an incorrect interval and their explanation was incomplete.

Question 35

35 A principal wonders what percentage of parents at her large high school restrict their child's cell phone privileges. The school surveys a random sample of 250 parents at the school and finds that 65% of them restrict their child's cell phone privileges. The school runs a simulation with 400 samples of 250 parents, assuming that 65% of them restrict cell phone privileges. The simulation results are shown below.



Use the simulation to determine an interval containing the middle 95% of simulated proportions. Justify your answer. Round all values to the *nearest hundredth*.

$$\bar{x} \pm 2.0x$$

$$0.59 - 0.714$$

$$0.652 + 2(0.031) = 0.714 = 71.4\%$$

$$0.652 - 2(0.031) = 0.59 = 59\%$$

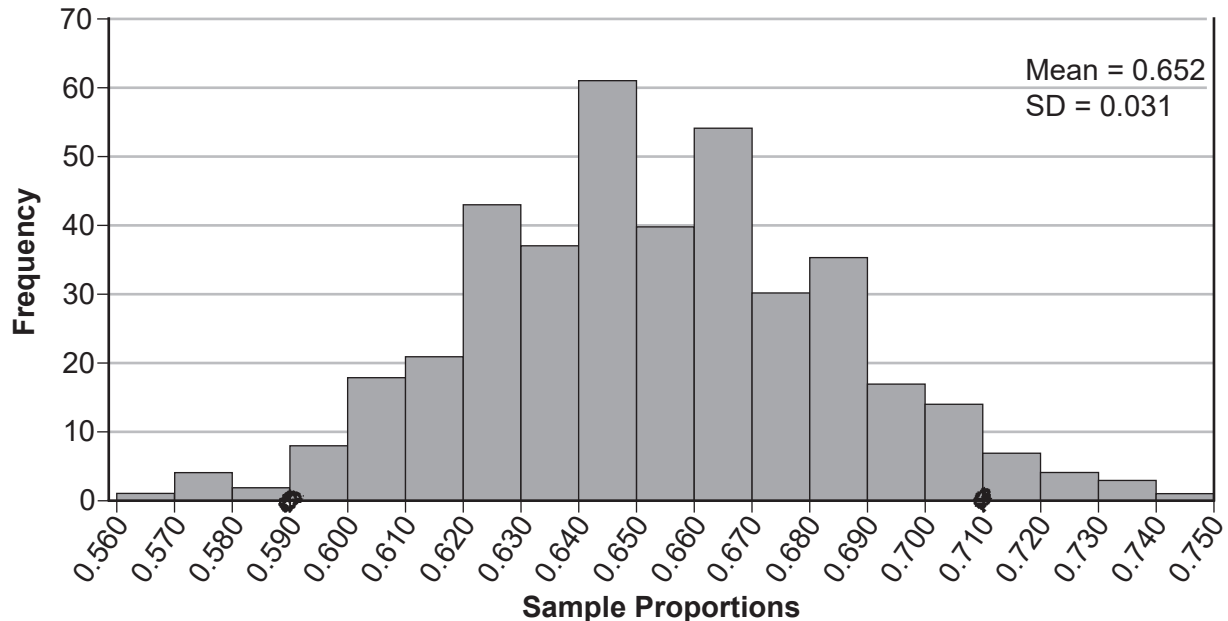
The school district's superintendent worries that less than half of parents restrict their child's cell phone privileges. Do the simulation results support the superintendent's concern? Explain.

The simulation results do not support the superintendent's concern because it is within the middle 95%.

Score 1: The student earned one credit for the interval.

Question 35

35 A principal wonders what percentage of parents at her large high school restrict their child's cell phone privileges. The school surveys a random sample of 250 parents at the school and finds that 65% of them restrict their child's cell phone privileges. The school runs a simulation with 400 samples of 250 parents, assuming that 65% of them restrict cell phone privileges. The simulation results are shown below.



Use the simulation to determine an interval containing the middle 95% of simulated proportions. Justify your answer. Round all values to the *nearest hundredth*.

$$\begin{aligned}
 &\text{Mean} \pm 2(\text{SD}) \\
 &.65 \pm 2(.031) \\
 &.588 \text{ to } .712 \approx \boxed{.59 \text{ to } .71}
 \end{aligned}$$

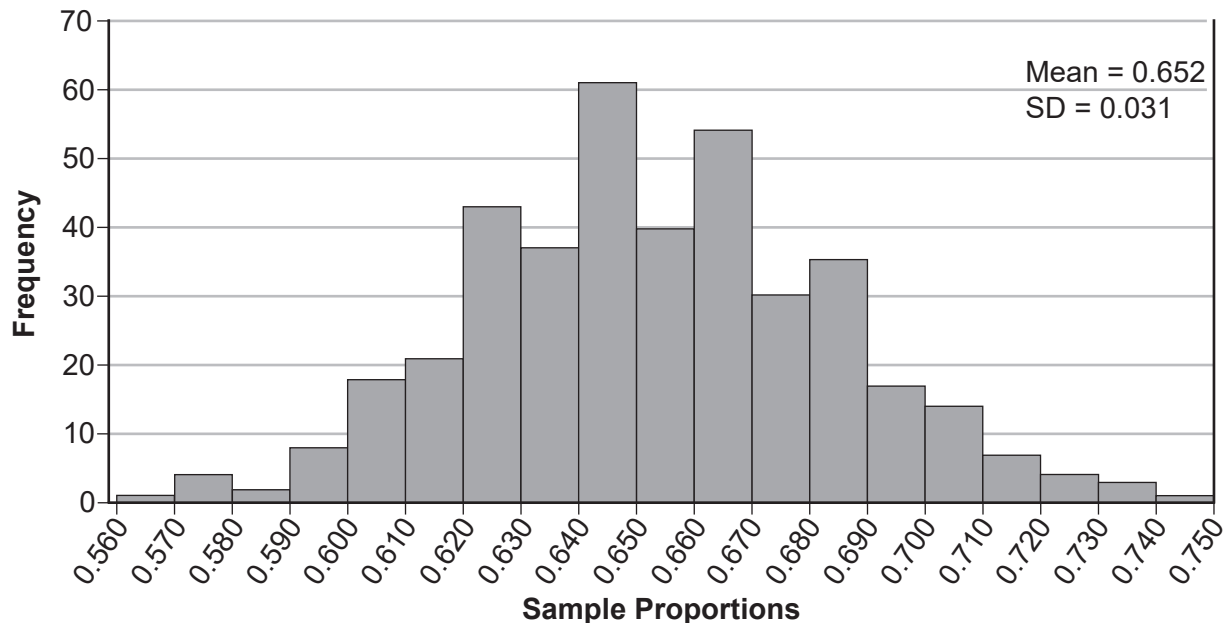
The school district's superintendent worries that less than half of parents restrict their child's cell phone privileges. Do the simulation results support the superintendent's concern? Explain.

65% falls within the middle 95%.

Score 1: The student used an incorrect mean when calculating the interval, did not state yes or no, and the explanation is irrelevant.

Question 35

35 A principal wonders what percentage of parents at her large high school restrict their child's cell phone privileges. The school surveys a random sample of 250 parents at the school and finds that 65% of them restrict their child's cell phone privileges. The school runs a simulation with 400 samples of 250 parents, assuming that 65% of them restrict cell phone privileges. The simulation results are shown below.



Use the simulation to determine an interval containing the middle 95% of simulated proportions. Justify your answer. Round all values to the *nearest hundredth*.

0

Lower: 250
Upper: 400
M: 0.652
SD: 0.031

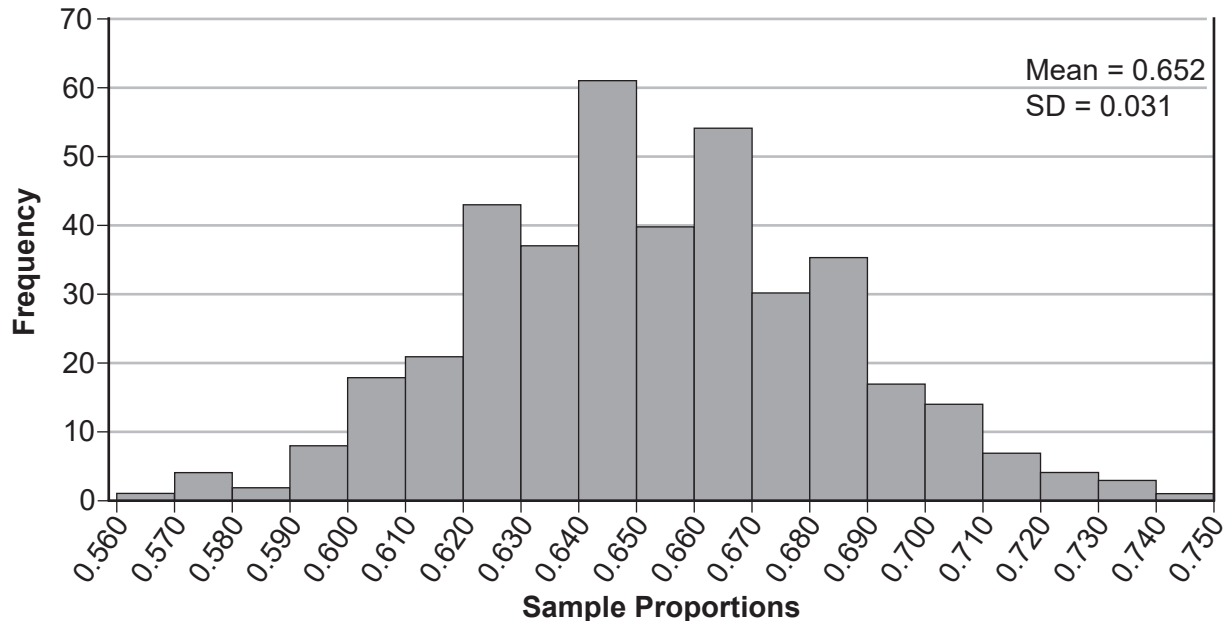
The school district's superintendent worries that less than half of parents restrict their child's cell phone privileges. Do the simulation results support the superintendent's concern? Explain.

The simulation results. Does not support the superintendent's concern because, more than half do not restrict their children.

Score 0: The student did not satisfy the criteria for one or more credits.

Question 35

35 A principal wonders what percentage of parents at her large high school restrict their child's cell phone privileges. The school surveys a random sample of 250 parents at the school and finds that 65% of them restrict their child's cell phone privileges. The school runs a simulation with 400 samples of 250 parents, assuming that 65% of them restrict cell phone privileges. The simulation results are shown below.



Use the simulation to determine an interval containing the middle 95% of simulated proportions. Justify your answer. Round all values to the *nearest hundredth*.

$$0.652 + 2(0.031) = 0.714$$

0.714

The school district's superintendent worries that less than half of parents restrict their child's cell phone privileges. Do the simulation results support the superintendent's concern? Explain.

Because 65% of them restrict
Cell Phone Privileges that's more than
half

Score 0: The student did not satisfy the criteria for one or more credits.

Question 36

- 36 Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

$$\begin{aligned} T(0) &= 110e^0 + 74 \\ T(0) &= 110 + 74 \\ T(0) &= 184 \end{aligned} \quad 184^\circ\text{F}$$

To the *nearest tenth*, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

$$\begin{aligned} T(5) &= 110e^{-0.0453(5)} + 74 \\ T(5) &= 161.705 \end{aligned} \quad \begin{aligned} m &= \frac{184 - 161.705}{0 - 5} \\ m &= -4.5 \end{aligned}$$

Question 36 is continued on the next page.

Score 6: The student gave a complete and correct response.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

From the time the tea was poured to 5 minutes after, the tea cooled about 4.5°F every minute.

To the *nearest tenth of a minute*, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

$$\begin{aligned} 120 &= 110e^{-0.0453(t)} - 74 && 19.2 \text{ minutes} \\ 194 &= 110e^{-0.0453(t)} \\ \frac{194}{110} &= e^{-0.0453t} \\ \ln\left(\frac{194}{110}\right) &= \ln(e^{-0.0453t}) \\ \ln\left(\frac{194}{110}\right) &= -0.0453t \\ t &= \frac{\ln\left(\frac{194}{110}\right)}{-0.0453} \\ t &= 19.2 \end{aligned}$$

Question 36

- 36** Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

$$\begin{aligned} & 110e^{-0.0453 \cdot 0} + 74 \\ &= 110 + 74 = 184^\circ\text{F} \end{aligned}$$

To the *nearest tenth*, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

$$\frac{T(5) - T(0)}{5} = -4.5$$

Question 36 is continued on the next page.

Score 6: The student gave a complete and correct response.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

The temp decreases at a rate of 4.5°F
per minute on average.

To the *nearest tenth of a minute*, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

$$110e^{-0.0453x} + 74 = 120$$

$$110e^{-0.0453x} = 46$$

$$e^{-0.0453x} = 0.41818$$

$$-0.0453x = -0.8718$$

$$x = 19.24589$$

$$x \approx 19.2$$

Question 36

- 36 Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

~~74°F~~ 184°F

To the *nearest tenth*, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

$$\begin{array}{r} 161.705 - 184 \\ \hline 5 - 0 \\ \hline -22.295 \\ \hline -4.5 \end{array}$$

Question 36 is continued on the next page.

Score 5: The student's interpretation is incorrect.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

4.5°F less every
minute the cup is cooled

To the *nearest tenth of a minute*, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

$$120 = 110e^{-0.453x} + 74$$

$$\ln \frac{46}{110} = -\cancel{0.453}x$$

-0.453

19.2 minutes

Question 36

- 36 Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

~~110~~ $T(0) = 110e^{-0.0453(0)} + 74$
 184°F

To the *nearest tenth*, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

$$\frac{161.7051\dots - 184^\circ}{5 - 0} = -4.5^\circ$$

$$\begin{aligned} T(0) &= 184^\circ\text{F} \\ T(5) &= 110e^{-0.0453(5)} + 74 \\ T(5) &= 161.7051\dots^\circ\text{F} \end{aligned}$$

Question 36 is continued on the next page.

Score 5: The student had a transcription error with the exponent in the last part.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

On average the tea
cooled by 4.5°F
each minute ~~in~~ in
the first five minutes.

To the *nearest tenth of a minute*, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

$$120^{\circ} = 110e^{-0.045x} + 74$$

19.4 minutes = x

$$\frac{46}{110} = \frac{110e^{-0.045x}}{110}$$

$$\frac{23}{55} = e^{-0.045x}$$

$$\ln \frac{23}{55} = \ln e^{-0.045x}$$

$$\ln \frac{23}{55} = -0.045x(1)$$

$$\frac{\ln \frac{23}{55}}{-0.045} = \frac{-0.045x}{-0.045}$$

Question 36

- 36 Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

$$\begin{aligned} T(0) &= 110e^{-0.0453(0)} + 74 \\ T(0) &= 110e^{(0)} + 74 \\ T(0) &= 110(1) + 74 \\ \boxed{T(0) = 184} \end{aligned}$$

To the *nearest tenth*, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

$$\begin{aligned} T(5) &\approx 161.7 \\ \frac{184 - 161.7}{-5} &= 4.5 \end{aligned}$$

Question 36 is continued on the next page.

Score 4: The student made a computational error calculating the average rate of change and gave an incomplete interpretation.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

The tea cooled by about 4.5°

To the *nearest tenth of a minute*, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

$$\begin{array}{ccc} 120 & = & 110e^{-0.0453x} + 74 \\ -74 & & -74 \end{array}$$

$$\frac{46}{110} = \frac{110e^{-0.0453x}}{110}$$

$$\ln\left(\frac{46}{110}\right) = \ln e^{-0.0453x}$$

$$\frac{\ln\left(\frac{46}{110}\right)}{-0.0453} = \frac{-0.0453x}{-0.0453}$$

$$\boxed{19.2 \approx x}$$

Question 36

- 36** Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

184°

To the *nearest tenth*, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

$(0, 184)$

$(5, 161.71)$

$$\frac{184 - 161.71}{0.25} = -41.5^\circ$$

Question 36 is continued on the next page.

Score 4: The student gave an incomplete interpretation and rounded too early in the last part.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

-41.5° per minute

To the *nearest tenth of a minute*, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

$$\begin{aligned} 120 &= 110e^{-.0453x} + 74 & \ln(.418) &= -.0453x \\ 46 &= 110e^{-.0453x} & \div .0453 & \\ .418 &= e^{-.0453x} & & \\ \ln(.418) &= -.0453x \ln(e) & & \end{aligned}$$

19.3 min

Question 36

- 36 Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

$$T(0) = 110e^{-0.0453(0)} + 74$$

$$T(0) = \boxed{184^\circ\text{F}}$$

To the *nearest tenth*, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

$$\frac{162 - 184}{5 - 0} = \frac{-22}{5} = -4.4$$

$$T(5) = 110e^{-0.0453(5)} + 74 = 161.7$$

$$T(0) = 110e^{-0.0453(0)} + 74 = 184$$

Question 36 is continued on the next page.

Score 3: The student rounded too early calculating the average rate of change, gave no interpretation, and did not express their final answer to the nearest tenth.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

$$\text{Average rate of change} = -4.4$$

To the *nearest tenth of a minute*, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

plug in $y =$ $\nearrow$

$$T(x) = 110e^{-0.0453(x)} + 74$$

19 minutes

19	120.52
20	118.46

$$\begin{array}{r} 120.52 \\ \downarrow \\ 120.5 \end{array}$$

Question 36

- 36** Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

$$T(0) = 100 e^{-0.0453(0)} + 74$$

$$T(0) = 174^{\circ}\text{F}$$

To the *nearest tenth*, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

$$\frac{\Delta y}{\Delta x} = \frac{153.13 - 174}{5 - 0} = -4.1$$

Question 36 is continued on the next page.

Score 3: The student had a transcription error of 100 but calculated and interpreted the average rate of change appropriately.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

This means the temperature will decrease at an average rate of 4.1°F per minute.

To the *nearest tenth of a minute*, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

$$120 = 100e^{-0.0453x} + 74$$
$$-74$$

$$46 = 100e^{-0.0453x}$$
$$\log 46 = \log 100e^{-0.0453x}$$
$$\frac{\log 46}{-.453 \log 100e} = \frac{-.453x \log 100e}{-.453 \log 100e}$$

Question 36

- 36 Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

$$\begin{aligned} T(x) &= 110e^{-0.0453x} + 74 && \text{0 minutes} \\ T(0) &= 110e^{-0.0453(0)} + 74 \\ T(0) &= \boxed{184^\circ} \end{aligned}$$

To the nearest tenth, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

$$\begin{aligned} T(5) &= 110e^{-0.0453(5)} + 74 \\ T(5) &= \boxed{161.7^\circ} \end{aligned}$$

Question 36 is continued on the next page.

Score 2: The student earned one credit on the first and last parts.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

Rate of change = 4.5° per minute

To the nearest tenth of a minute, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

$$T(19) = 110e^{-0.053(19)} + 74 = 120.5^\circ$$
$$T(20) = 118.5^\circ$$

19 minutes

Question 36

- 36 Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

$$110e^{-0.0453(0)} + 74 = 184$$

To the *nearest tenth*, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

$$\begin{array}{l} \begin{matrix} x_2 & y_2 \\ (0, & 184) \\ x_1 & y_1 \\ (5, & 161.71) \end{matrix} \end{array} \quad \frac{184 - 161.71}{0 - 5} = -5.5$$

Question 36 is continued on the next page.

Score 2: The student earned one credit in the first and the second parts.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

this means that each minute the temperature decrease

To the *nearest tenth of a minute*, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

Question 36

- 36** Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

$$184^{\circ}$$

To the *nearest tenth*, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

$$\begin{array}{r} 178.17 \\ + -161.7 \\ \hline 17.473 \\ \hline 5 \end{array} = \boxed{3.5}$$

Question 36 is continued on the next page.

Score 1: The student earned one credit for the first part.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

To the *nearest tenth of a minute*, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

19 minutes

Question 36

- 36 Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

110° degrees Fahrenheit

To the *nearest tenth*, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

slope

$$\begin{aligned} x_1 &= 0 \\ y_1 &= 110 \\ x_2 &= 5 \\ y_2 &= 161.7051277 \end{aligned}$$
$$\frac{y_2 - y_1}{x_2 - x_1}$$

average rate = 9.5

Question 36 is continued on the next page.

Score 1: The student earned one credit for the average rate of change.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

To the *nearest tenth of a minute*, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

around 19.3
or 19.2

Question 36

- 36 Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

To the *nearest tenth*, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

$$184 \quad 161.7$$

$$T(0) = 110e^{-0.0453(0)} + 74 = 184$$

$$T(5) = 110e^{-0.0453(5)} + 74 = 161.7$$

Question 36 is continued on the next page.

Score 0: The student did not satisfy the criteria for one or more credits.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

To the *nearest tenth of a minute*, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

1 hour and 14 minutes

Question 36

- 36 Lubin pours green tea into a cup to cool. The function below can be used to model the temperature, in degrees Fahrenheit, of Lubin's tea x minutes after he pours it into the cup.

$$T(x) = 110e^{-0.0453x} + 74$$

State the temperature of the tea, in degrees Fahrenheit, when Lubin poured it into the cup.

$$110e^{-0.0453(0)} + 74$$

$$185$$

To the nearest tenth, use $T(x)$ to determine the average rate of change in degrees per minute, from $x = 0$ to $x = 5$.

$$110e^{-0.0453(5)} + 74$$

$$162.7051277$$

$$\begin{array}{r} 185 \\ - 162.7051277 \\ \hline 22.2948723 \end{array}$$

22.3

Question 36 is continued on the next page.

Score 0: The student did not satisfy the criteria for one or more credits.

Question 36

Question 36 continued

Interpret the value of the average rate of change within the given context.

To the nearest tenth of a minute, determine how long Lubin must wait after pouring his tea into the cup before the tea's temperature reaches 120° Fahrenheit.

$$19.8 \text{ minutes}$$
$$110e^{-0.0453(19.8)} + 74$$
$$119.8$$
$$\approx$$
$$120^\circ$$