

The University of the State of New York  
REGENTS HIGH SCHOOL EXAMINATION

# ALGEBRA II

Monday, August 19, 2024 — 12:30 to 3:30 p.m., only

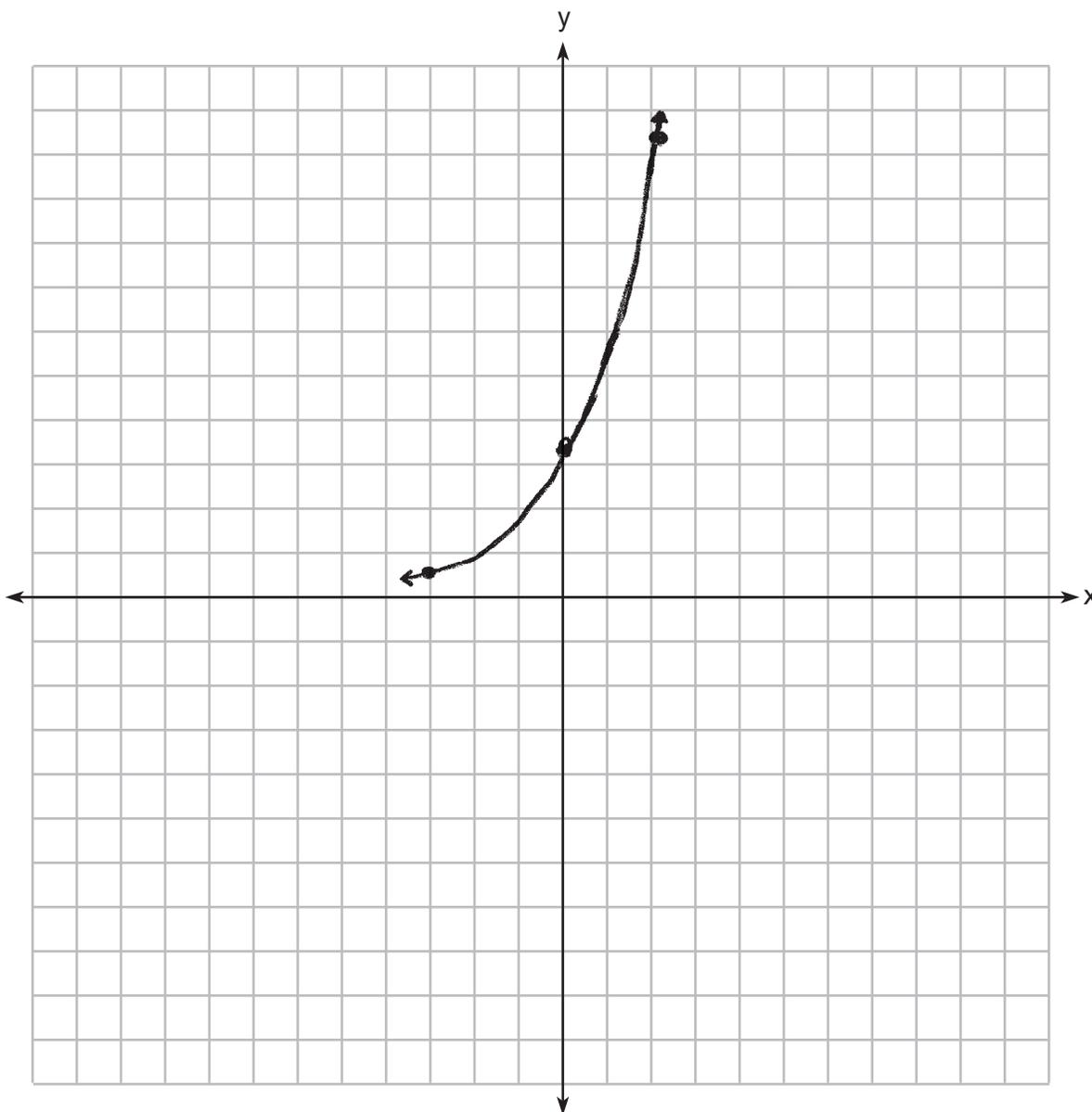
## MODEL RESPONSE SET

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Question 25

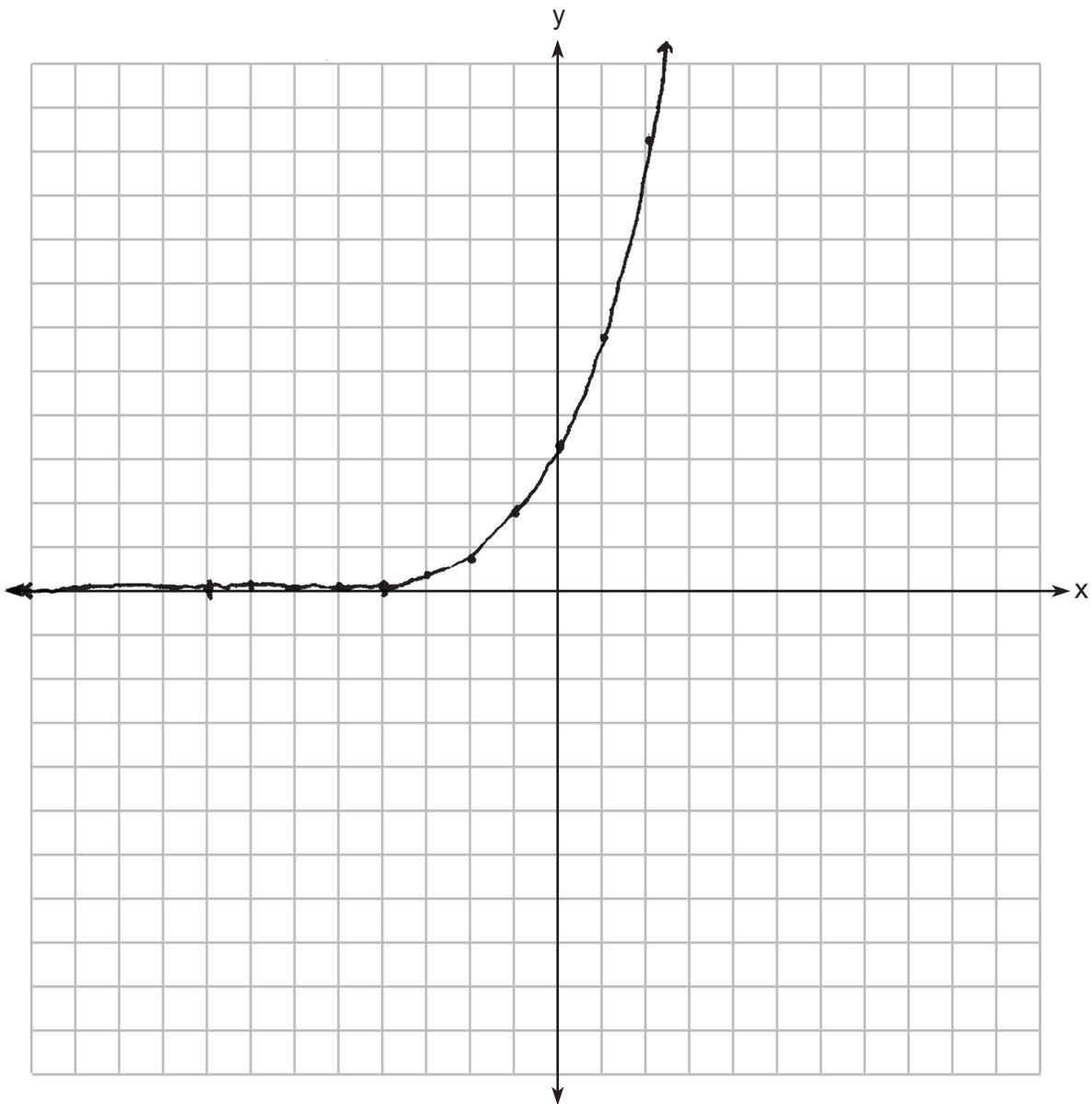
25 On the axes below, graph  $y = 3.2(1.8)^x$ .



**Score 2:** The student gave a complete and correct response.

Question 25

25 On the axes below, graph  $y = 3.2(1.8)^x$ .

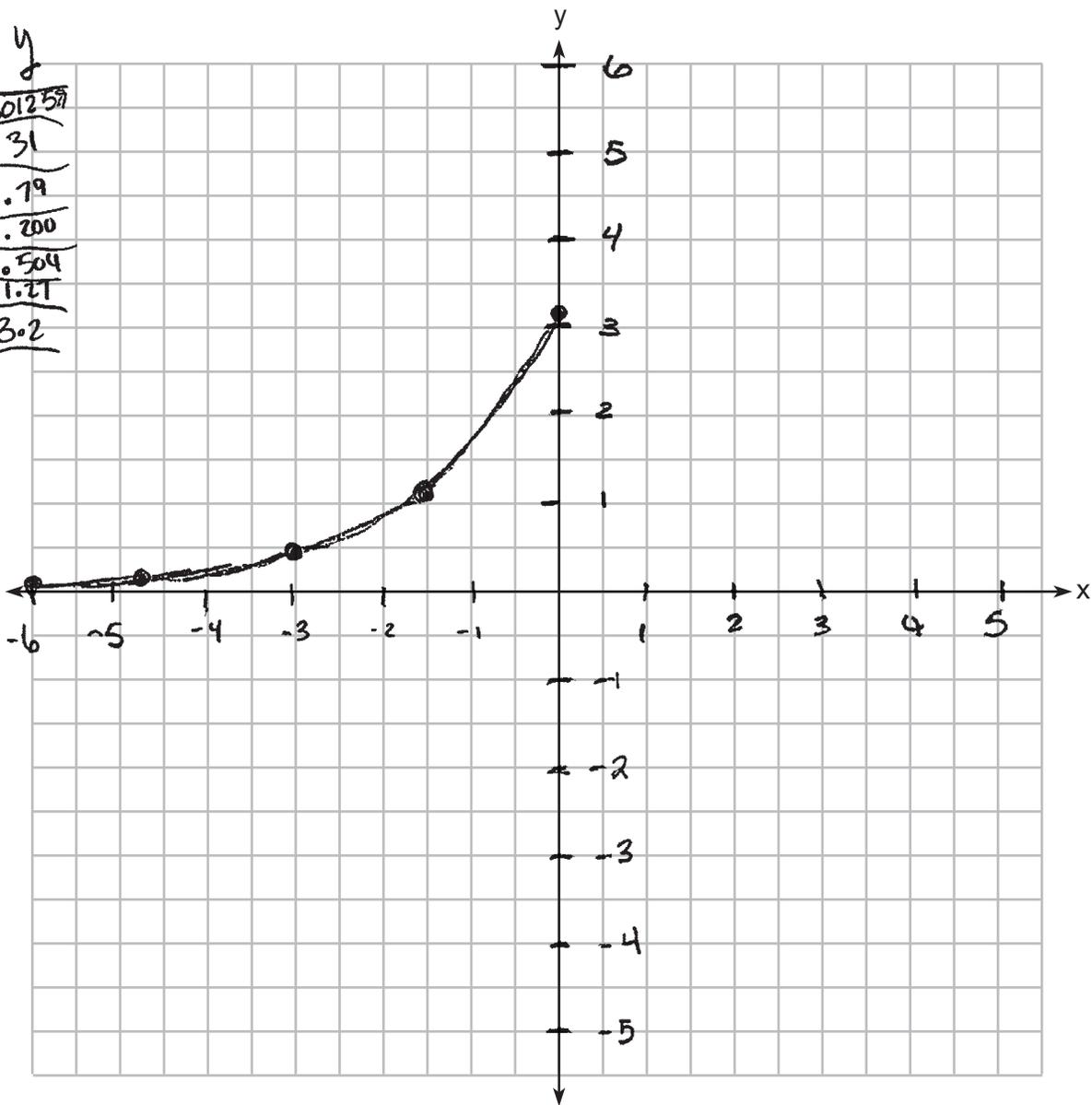


**Score 2:** The student gave a complete and correct response.

Question 25

25 On the axes below, graph  $y = 3.2(1.8)^x$ .

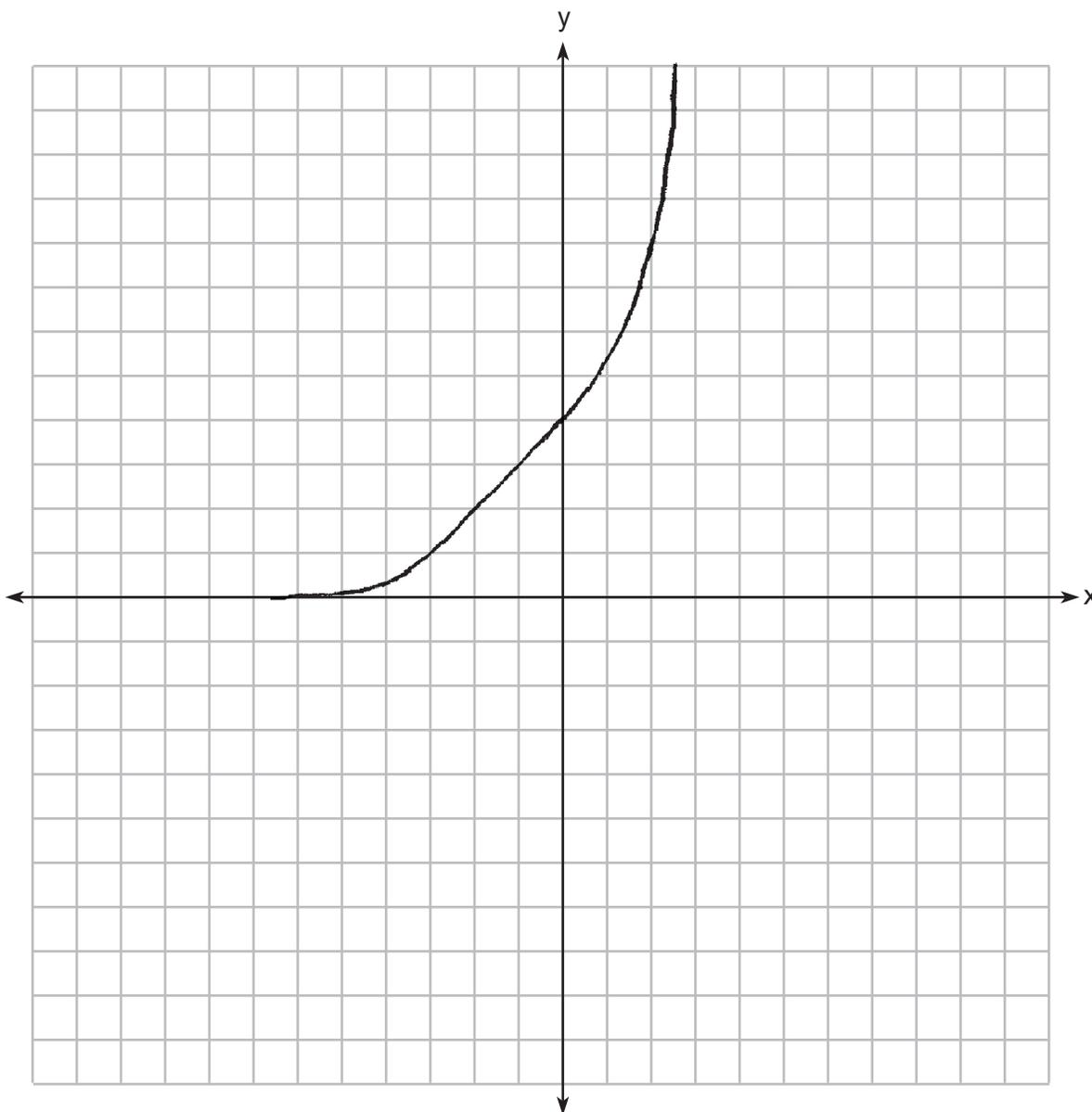
X	y
-9.4	0.1259
-7.8	.31
-6.2	.79
-4.7	.200
-3.1	.504
-1.5	1.21
0	3.2



**Score 1:** The student made an error by terminating the graph at the  $y$ -intercept.

Question 25

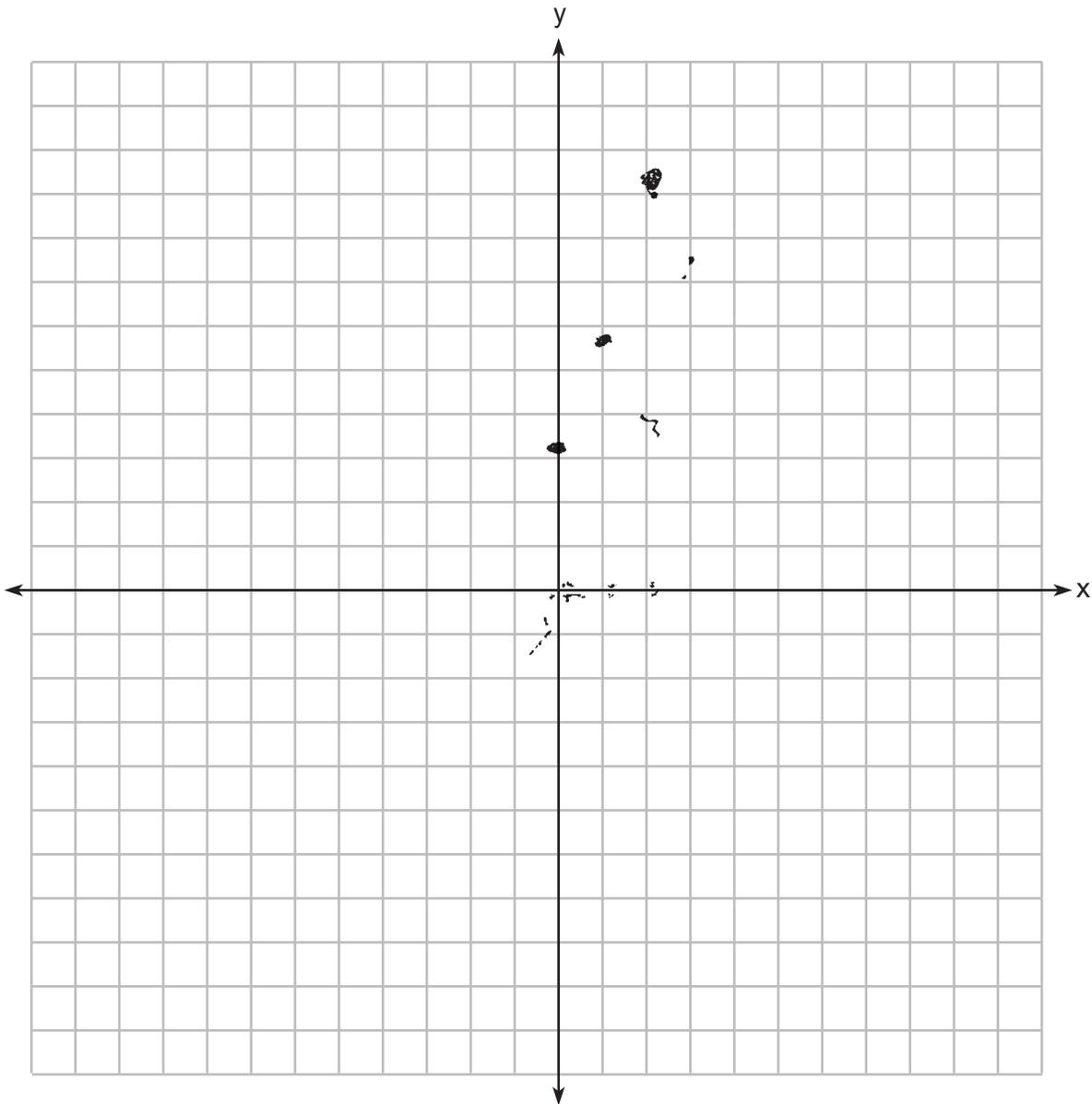
25 On the axes below, graph  $y = 3.2(1.8)^x$ .



**Score 0:** The student made multiple graphing errors.

Question 25

25 On the axes below, graph  $y = 3.2(1.8)^x$ .



**Score 0:** The student correctly plotted two points, but did not show enough relevant course-level work to receive any credit.

**Question 26**

26 Is  $x + 3$  a factor of  $7x^3 + 27x^2 + 9x - 27$ ?  
Justify your answer.

$$\begin{array}{r} 7x^2 + 6x - 9 \\ x+3 \overline{) 7x^3 + 27x^2 + 9x - 27} \\ \underline{-(7x^3 + 21x^2)} \phantom{+ 9x - 27} \\ 6x^2 + 9x \phantom{- 27} \\ \underline{-(6x^2 + 18x)} \phantom{- 27} \\ -9x - 27 \\ \underline{-(-9x - 27)} \\ 0 \end{array}$$

$x+3$  is a factor of  $7x^3 + 27x^2 + 9x - 27$   
because there's no remainder when you  
divide them together.

**Score 2:** The student gave a complete and correct response.

**Question 26**

**26** Is  $x + 3$  a factor of  $7x^3 + 27x^2 + 9x - 27$ ?  
Justify your answer.

$$7(-3)^3 + 27(-3)^2 + 9(-3) - 27$$

$$-189 + 243 + 27 - 27$$

$$= 0$$

$x + 3$  is a factor of  $7x^3 + 27x^2 + 9x - 27$

**Score 2:** The student gave a complete and correct response.

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**Question 26**

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**26** Is  $x + 3$  a factor of  $7x^3 + 27x^2 + 9x - 27$ ?

Justify your answer.

$$7(3)^3 + 27(3)^2 + 9(3) - 27 = 0$$

$$189 + 243 + \cancel{27} - 27 = 0$$

$$432 \neq 0$$

$x + 3$  is not a factor

---

**Score 1:** The student incorrectly evaluated 3 instead of  $-3$ .

**Question 26**

**26** Is  $x + 3$  a factor of  $7x^3 + 27x^2 + 9x - 27$ ?  
Justify your answer.

$$\begin{array}{r|rrrr} x+3 & & & & \\ -3 & 7 & 27 & 9 & -27 \\ & \downarrow & -21 & -24 & 45 \\ \hline & 7 & 8 & -15 & 18 \end{array}$$

$$7x^2 + 8x - 15 \quad \frac{+18}{x+3}$$

$x+3$  is not a factor of  
 $7x^3 + 27x^2 + 9x - 27$  because  
there is a remainder.

**Score 1:** The student made a computational error.

**Question 26**

26 Is  $x + 3$  a factor of  $7x^3 + 27x^2 + 9x - 27$ ?  
Justify your answer.

$$\begin{array}{r} \boxed{-3} \\ 7x^3 - 27x^2 + 9x - 27 \\ \underline{7x^3 - 21x^2 - 18x + 27} \\ 6x^2 + 27x - 54 \end{array}$$

$$7x^2 + 6x + 27$$

yes because when performing  
division,  $x-3$  goes into  
 $7x^3 + 27x^2 + 9x - 27$  perfectly.

**Score 0:** The student made multiple errors.

**Question 26**

**26** Is  $x + 3$  a factor of  $7x^3 + 27x^2 + 9x - 27$ ?  
Justify your answer.

$$\begin{aligned} &7(3)^3 + 27(3)^2 + 9(3) - 27 \\ &7(27) + \\ &1189 + 243 \\ &= 432 \end{aligned}$$

**Score 0:** The student incorrectly substituted 3 and did not indicate no/yes.

Question 27

27 Over the set of integers, factor the expression  $2x^4 - 10x^3 + 3x^2 - 15x$  completely.

$$2x^3(x-5) + 3x(x-5)$$

$$(2x^3 + 3x)(x-5)$$

$$x(2x^2 + 3)$$

$$x(2x^2 + 3)(x-5)$$

**Score 2:** The student gave a complete and correct response.

**Question 27**

27 Over the set of integers, factor the expression  $2x^4 - 10x^3 + 3x^2 - 15x$  completely.

$$2x^4 - 10x^3 + 3x^2 - 15x$$

$$x(2x^3 - 10x^2 + 3x - 15)$$

$$x(2x^2 + 3)(x - 5)$$

$$x(2x^2 + 3)(x - 5)$$

**Score 2:** The student gave a complete and correct response.

**Question 27**

27 Over the set of integers, factor the expression  $2x^4 - 10x^3 + 3x^2 - 15x$  completely.

$$(2x^4 - 10x^3)(3x^2 - 15x)$$

$$2x^3(x-5) + 3x(x-5)$$

$$(2x^3 + 3x)(x-5)$$

**Score 1:** The student did not factor out the greatest common factor.

**Question 27**

27 Over the set of integers, factor the expression  $2x^4 - 10x^3 + 3x^2 - 15x$  completely.

$$2x^3(x-5) + 3x(x-5)$$

$$(2x^3 + 3x)(x-5)^2$$

$$x(2x^2 + 3)(x-5)^2$$

**Score 1:** The student incorrectly squared  $(x - 5)$ .

Question 27

27 Over the set of integers, factor the expression  $2x^4 - 10x^3 + 3x^2 - 15x$  completely.

$$\begin{array}{l} \cancel{2} \cancel{3} \\ \cancel{2} \cancel{1} \\ \cancel{3} \end{array} \quad \begin{array}{l} 2x^3(x-5) \cdot 3x(x-5) \\ (2x^3+3x)(x-5) \\ x(2x+3) \\ (2x^3+1x)(x-5) \end{array}$$

**Score 0:** The student did not factor out the GCF and made a transcription error.

Question 28

28 The monthly unemployment rate of towns in the United States is approximately normally distributed with a mean rate of 5.2% and a standard deviation of 1.6%. Determine the percentage of towns, to the *nearest integer*, that have a monthly unemployment rate greater than 6%.

$$31\%$$
$$\text{Normal cdf}(6, 100, 5.2, 1.6)$$
$$\begin{array}{r} .368 \\ \approx \\ .31 \end{array}$$

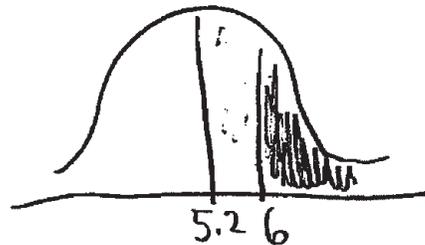
**Score 2:** The student gave a complete and correct response.

Question 28

28 The monthly unemployment rate of towns in the United States is approximately normally distributed with a mean rate of 5.2% and a standard deviation of 1.6%. Determine the percentage of towns, to the *nearest integer*, that have a monthly unemployment rate greater than 6%.

$$\begin{aligned} \mu &= .052 \\ \sigma &= .016 \\ \text{low: } &.06 \\ \text{up: } &\infty \end{aligned}$$

normcdf



31% of towns

**Score 2:** The student gave a complete and correct response.

Question 28

28 The monthly unemployment rate of towns in the United States is approximately normally distributed with a mean rate of 5.2% and a standard deviation of 1.6%. Determine the percentage of towns, to the *nearest integer*, that have a monthly unemployment rate greater than 6%.

$$\text{Normal (DF)}(0.04, \text{aaaaa}, 0.052, 0.016) \\ = 0.309$$

$$\boxed{\sqrt{30.911}}$$

**Score 1:** The student made a rounding error.

Question 28

28 The monthly unemployment rate of towns in the United States is approximately normally distributed with a mean rate of 5.2% and a standard deviation of 1.6%. Determine the percentage of towns, to the *nearest integer*, that have a monthly unemployment rate greater than 6%.



$$\text{normCdf}(7, 100, 5.2, 1.6) = 0.13029\dots$$

13%

**Score 1:** The student used 7 as the lower value in the distribution.

Question 28

28 The monthly unemployment rate of towns in the United States is approximately normally distributed with a mean rate of 5.2% and a standard deviation of 1.6%. Determine the percentage of towns, to the *nearest integer*, that have a monthly unemployment rate greater than 6%.

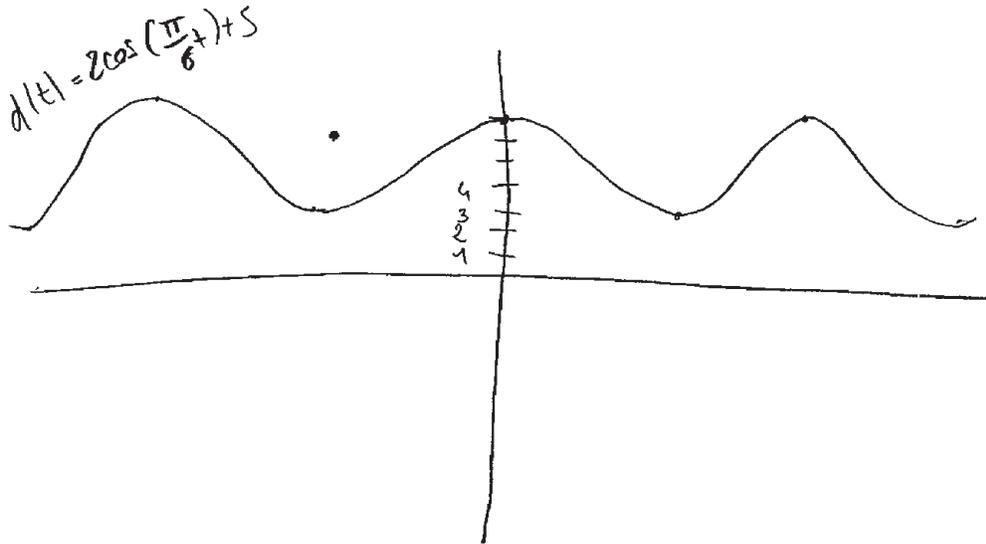
normal cdf (6, 100, 1.6, 5.2)

0.2

**Score 0:** The student made multiple errors.

**Question 29**

- 29 The function  $d(t) = 2\cos\left(\frac{\pi}{6}t\right) + 5$  models the water depth, in feet, at a location in a bay,  $t$  hours since the last high tide. Determine the *minimum* water depth of the location, in feet, and justify your answer.



When graphing the depth we see that it's at 3 feet where is the minimum depth of the spot.

**Score 2:** The student gave a complete and correct response.

**Question 29**

29 The function  $d(t) = 2\cos\left(\frac{\pi}{6}t\right) + 5$  models the water depth, in feet, at a location in a bay,  $t$  hours since the last high tide. Determine the minimum water depth of the location, in feet, and justify your answer.

$$d(t) = \underbrace{2}_{a} \cos\left(\frac{\pi}{6}t\right) + \underbrace{5}_{\text{midline}}$$
$$5 - 2 = \textcircled{3}$$

**Score 2:** The student gave a complete and correct response.

**Question 29**

- 29 The function  $d(t) = 2\cos\left(\frac{\pi}{6}t\right) + 5$  models the water depth, in feet, at a location in a bay,  $t$  hours since the last high tide. Determine the *minimum* water depth of the location, in feet, and justify your answer.

$$d(0) = 2\cos\left(\frac{\pi}{6} \cdot 0\right) + 5 = 7$$

$$d(1) = 6.73$$

$$d(2) = 6$$

$$d(5) = 3.27$$

$$d(10) = 6$$

$$d(7) = 3.27$$

$$d(6) = 3$$

6 hours

**Score 1:** The student found the time at which the tide reached its minimum.

**Question 29**

**29** The function  $d(t) = 2\cos\left(\frac{\pi}{6}t\right) + 5$  models the water depth, in feet, at a location in a bay,  $t$  hours since the last high tide. Determine the *minimum* water depth of the location, in feet, and justify your answer.

7 because the midline is  
at 5 and the amplitude  
is 2.

**Score 1:** The student stated the maximum instead of the minimum.

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**Question 29**

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**29** The function  $d(t) = 2\cos\left(\frac{\pi}{6}t\right) + 5$  models the water depth, in feet, at a location in a bay,  $t$  hours since the last high tide. Determine the *minimum* water depth of the location, in feet, and justify your answer.

-5 ft, because it is  
the minimum altitude

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**Score 0:** The student did not show enough relevant course-level work to receive any credit.

**Question 30**

30 A brewed cup of coffee contains 130 mg of caffeine. The half-life of caffeine in the bloodstream is 5.5 hours. Write a function,  $C(t)$  to represent the amount of caffeine in the bloodstream  $t$  hours after drinking one cup of coffee.

$$C(t) = 130 \left(\frac{1}{2}\right)^{\frac{t}{5.5}}$$

$$C(t) = 130 \left(\frac{1}{2}\right)^{\frac{t}{5.5}}$$

**Score 2:** The student gave a complete and correct response.

**Question 30**

30 A brewed cup of coffee contains 130 mg of caffeine. The half-life of caffeine in the bloodstream is 5.5 hours. Write a function,  $C(t)$  to represent the amount of caffeine in the bloodstream  $t$  hours after drinking one cup of coffee.

$$\frac{65}{130} = \frac{130 e^{-r \cdot 5.5}}{130}$$

$$.5 = e^{-r \cdot 5.5}$$

$$\frac{\ln .5}{5.5} = \frac{-r \cdot 5.5}{5.5}$$

$$C(t) = 130 e^{-.126t}$$

**Score 2:** The student gave a complete and correct response.

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**Question 30**

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**30** A brewed cup of coffee contains 130 mg of caffeine. The half-life of caffeine in the bloodstream is 5.5 hours. Write a function,  $C(t)$  to represent the amount of caffeine in the bloodstream  $t$  hours after drinking one cup of coffee.

$$C(t) = 130(0.5)^{5.5t}$$

**Score 1:** The student incorrectly expressed the exponent as a product.

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**Question 30**

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**30** A brewed cup of coffee contains 130 mg of caffeine. The half-life of caffeine in the bloodstream is 5.5 hours. Write a function,  $C(t)$  to represent the amount of caffeine in the bloodstream  $t$  hours after drinking one cup of coffee.

$$130\left(\frac{1}{2}\right)^{\frac{t}{5.5}}$$

**Score 1:** The student wrote an expression, not an equation.

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**Question 30**

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**30** A brewed cup of coffee contains 130 mg of caffeine. The half-life of caffeine in the bloodstream is 5.5 hours. Write a function,  $C(t)$  to represent the amount of caffeine in the bloodstream  $t$  hours after drinking one cup of coffee.

$$C(t) = 130 e^{-(5.5)t}$$

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**Score 0:** The student did not satisfy the criteria for one or more credits.

**Question 31**

31 Markus is a long-distance walker. In one race, he walked 55 miles in  $t$  hours and in another race walked 65 miles in  $t + 3$  hours. His rates are shown in the equations below.

$$r = \frac{55}{t} \quad r = \frac{65}{t + 3}$$

Markus walked at an equivalent rate,  $r$ , for each race. Determine the number of hours that *each* of the two races took.

$$55t + 165 = 65t$$

$$\frac{165}{10} = \frac{10t}{10}$$

16.5 hours  
19.5 hours

**Score 2:** The student gave a complete and correct response.

**Question 31**

31 Markus is a long-distance walker. In one race, he walked 55 miles in  $t$  hours and in another race walked 65 miles in  $t + 3$  hours. His rates are shown in the equations below.

$$r = \frac{55}{t} \quad r = \frac{65}{t+3}$$

Markus walked at an equivalent rate,  $r$ , for each race. Determine the number of hours that *each* of the two races took.

$\frac{10}{3}$   
3.33 mph

~~$\frac{55}{t} = \frac{65}{t+3}$   
 $\frac{55}{t} \times \frac{t+3}{t+3}$   
 $3575 = t^2 + 3$~~

$\frac{55}{3.33}$        $\frac{65}{3.33}$

race 1 16.5 h

race 2 19.5 h

**Score 2:** The student gave a complete and correct response.

**Question 31**

31 Markus is a long-distance walker. In one race, he walked 55 miles in  $t$  hours and in another race walked 65 miles in  $t + 3$  hours. His rates are shown in the equations below.

$$r = \frac{55}{t} \quad r = \frac{65}{t+3}$$

Markus walked at an equivalent rate,  $r$ , for each race. Determine the number of hours that *each* of the two races took.

$$\frac{55}{t} = \frac{65}{t+3}$$

$$55(t+3) = 65t$$

$$55t + 165 = 65t$$

$$\frac{10t}{10} = \frac{165}{10}$$

$$t = \underline{16}$$

$$t+3 = \underline{19}$$

**Score 1:** The student made one computational error.

**Question 31**

31 Markus is a long-distance walker. In one race, he walked 55 miles in  $t$  hours and in another race walked 65 miles in  $t + 3$  hours. His rates are shown in the equations below.

$$r = \frac{55}{t} \quad r = \frac{65}{t+3}$$

Markus walked at an equivalent rate,  $r$ , for each race. Determine the number of hours that *each* of the two races took.

$$t \cdot \frac{55}{t} = \frac{65}{t+3} \cdot (t+3)$$

$$55t = 65(t+3)$$

$$55t = 65t + 195$$

$$19.5$$

$$19.5 + 3$$

$$= 22.5$$

**Score 0:** The student made multiple errors.

Question 32

32 Solve the equation  $x^2 + 3x + 11 = 0$  algebraically. Express the answer in  $a + bi$  form.

$$\begin{aligned} a &= 1 \\ b &= 3 \\ c &= 11 \end{aligned}$$
$$x = \frac{-3 \pm \sqrt{9 - 4(1)(11)}}{2}$$
$$x = \frac{-3 \pm \sqrt{-35}}{2}$$
$$\sqrt{-35} = \sqrt{-1 \cdot 35} = i\sqrt{35}$$
$$x = -\frac{3}{2} \pm \frac{i\sqrt{35}}{2}$$

**Score 2:** The student gave a complete and correct response.

**Question 32**

32 Solve the equation  $x^2 + 3x + 11 = 0$  algebraically. Express the answer in  $a + bi$  form.

$$x^2 + 3x + \underline{\quad} = -11 + \underline{\quad}$$

$$x^2 + 3x + \frac{9}{4} = -11 + \frac{9}{4}$$

$$\left(x + \frac{3}{2}\right)^2 = \pm \sqrt{\frac{-35}{4}}$$

$$x + \frac{3}{2} = \pm \frac{\sqrt{35}}{2}$$

$$x = -\frac{3}{2} \pm \frac{\sqrt{35}}{2}$$

**Score 2:** The student gave a complete and correct response.

**Question 32**

32 Solve the equation  $x^2 + 3x + 11 = 0$  algebraically. Express the answer in  $a + bi$  form.

$$x^2 + 3x + 11 = 0$$

$$\begin{aligned} a &= 1 \\ b &= 3 \\ c &= 11 \end{aligned}$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-3 \pm \sqrt{(3)^2 - 4(1)(11)}}{2(1)}$$

$$x = \frac{-3 \pm \sqrt{-35}}{2} \begin{matrix} \swarrow \sqrt{-1} \rightarrow i \\ \searrow \sqrt{35} \end{matrix}$$

$$x = \frac{-3 \pm \sqrt{35}i}{2}$$

**Score 1:** The student did not write the answer in  $a + bi$  form.

**Question 32**

32 Solve the equation  $x^2 + 3x + 11 = 0$  algebraically. Express the answer in  $a + bi$  form.

$$a = 1$$

$$b = 3$$

$$c = 11$$

$$x = \frac{-3 \pm \sqrt{3^2 - 4(1)(11)}}{2(1)}$$

$$x = \frac{-3 \pm \sqrt{9 - 44}}{2}$$

$$x = \frac{-3 \pm \sqrt{-35}}{2}$$

$$x = \frac{-3 \pm 35i}{2}$$

$$x = \frac{-3}{2} \pm \frac{35i}{2}$$

**Score 1:** The student incorrectly removed the radical when simplifying.

Question 32

32 Solve the equation  $x^2 + 3x + 11 = 0$  algebraically. Express the answer in  $a + bi$  form.

$$a + bi$$
$$\frac{-3 \pm \sqrt{3^2 - 4(1)(11)}}{2(1)}$$

$$\frac{-3 \pm \sqrt{-35}}{2}$$
$$-3 \pm 7\sqrt{5}$$

$$\sqrt{35}$$
$$\begin{array}{c} \swarrow \quad \searrow \\ \sqrt{7} \quad \sqrt{5} \\ \downarrow \quad \downarrow \\ 1 \quad 1 \\ \hline \end{array}$$

$$-15 \pm 6.9i$$

**Score 0:** The student made multiple errors simplifying.

**Question 32**

32 Solve the equation  $x^2 + 3x + 11 = 0$  algebraically. Express the answer in  $a + bi$  form.

$$x = \frac{-1 \pm \sqrt{b^2 + 4ac}}{2a}$$

$$x = \frac{-3 \pm \sqrt{(-3)^2 - 4(1)(11)}}{2(1)}$$

$$x = \frac{-3 \pm \sqrt{9 - 44}}{2}$$

$$x = \frac{-3 \pm \sqrt{-35}}{2}$$

$$x = \frac{-3 \pm \sqrt{35} \sqrt{-1}}{2}$$

$$x = \frac{-3 \pm i\sqrt{35}}{2}$$

**Score 0:** The student did not satisfy the criteria for one or more credits.

**Question 33**

33 The population of China, in millions, can be modeled by the function  $P(x) = 316.93e^{0.0133x}$ , where  $x$  is the number of years since 1900.

The population of India since 1900 is summarized in the table below:

Years since 1900	0	10	20	30	40	50	60	70	80	90	100	110	120
Population (millions)	243	254	268	285	324	376.3	450.6	555.1	699	873.3	1056.6	1234.3	1380

Which country's population had a greater average rate of change between 1950 and 2020? Justify your answer.

$$2020 - 1950 = 70$$

India:

$$1380 - 376.3 = 1003.7$$

China:

$$P(50) = 316.93e^{0.0133(50)} =$$

$$P(50) = 616.267$$

$$P(120) = 316.93e^{0.0133(120)}$$

$$P(120) = 1563.498$$

$$1563.498 - 616.267 = 947.231$$

$$\frac{1003.7}{70} > \frac{947.231}{70}$$

↓

India had a greater average rate of change

**Score 4:** The student gave a complete and correct response.

**Question 33**

33 The population of China, in millions, can be modeled by the function  $P(x) = 316.93e^{0.0133x}$ , where  $x$  is the number of years since 1900.

The population of India since 1900 is summarized in the table below:

Years since 1900	0	10	20	30	40	50	60	70	80	90	100	110	120
Population (millions)	243	254	268	285	324	376.3	450.6	555.1	699	873.3	1056.6	1234.3	1380

Which country's population had a greater average rate of change between 1950 and 2020? Justify your answer.

China  
(50, 616.27)  
(120, 1563.50)

$$\frac{1563.50 - 616.27}{120 - 50} = \frac{947.23}{70} = 13.5$$

India  
(50, 376.3)

$$\frac{1380 - 376.3}{120 - 50} = \frac{1003.7}{70} = 14.3$$

India population had a greater average rate of change between 1950 and 2020.

**Score 4:** The student gave a complete and correct response.

**Question 33**

33 The population of China, in millions, can be modeled by the function  $P(x) = 316.93e^{0.0133x}$ , where  $x$  is the number of years since 1900.

The population of India since 1900 is summarized in the table below:

<b>Years since 1900</b>	0	10	20	30	40	50	60	70	80	90	100	110	120
<b>Population (millions)</b>	243	254	268	285	324	376.3	450.6	555.1	699	873.3	1056.6	1234.3	1380

Which country's population had a greater average rate of change between 1950 and 2020? Justify your answer.

$$\text{India: } \frac{120 - 50}{1380 - 376.3} = 0.0697419548$$

$$\text{China: } P(120) = 1563.498 \quad \frac{120 - 50}{1563.5 - 616.3} = 0.0739$$

$$P(50) = 616.27$$

China had a greater average rate of change

**Score 3:** The student calculated  $\frac{\Delta x}{\Delta y}$  for the average rate of change.

**Question 33**

33 The population of China, in millions, can be modeled by the function  $P(x) = 316.93e^{0.0133x}$ , where  $x$  is the number of years since 1900.

The population of India since 1900 is summarized in the table below:

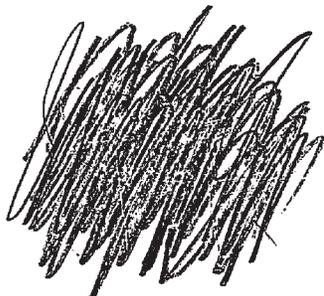
Years since 1900	0	10	20	30	40	50	60	70	80	90	100	110	120
Population (millions)	243	254	268	285	324	376.3	450.6	555.1	699	873.3	1056.6	1234.3	1380

Which country's population had a greater average rate of change between 1950 and 2020? Justify your answer.

$$\frac{1380 - 376.3}{80} = 14.3$$

$$\frac{1563 - 16.27}{80} = 13.5$$

China is greater average of change since it has a average of  $14.3 > 13.5$



**Score 3:** The student stated an incorrect conclusion.

**Question 33**

33 The population of China, in millions, can be modeled by the function  $P(x) = 316.93e^{0.0133x}$ , where  $x$  is the number of years since 1900.

The population of India since 1900 is summarized in the table below:

Years since 1900	0	10	20	30	40	50	60	70	80	90	100	110	120
Population (millions)	243	254	268	285	324	376.3	450.6	555.1	699	873.3	1056.6	1234.3	1380

Which country's population had a greater average rate of change between 1950 and 2020? Justify your answer.

India

$$\frac{1380 - 376.3}{120 - 50} = \frac{1003.7}{70} = 14.3385$$

China

$$\frac{70}{316.93} = \frac{316.93 e^{0.0133x}}{316.93}$$

$$\frac{70}{316.93} = e^{0.0133x}$$

$$\frac{\ln \frac{70}{316.93}}{0.0133} = \frac{0.0133x}{0.0133}$$

$$x = -113.54$$

India had  
the greatest  
rate of  
Change.  
from 1950  
to 2020

**Score 2:** The student correctly calculated the average rate of change for India, incorrectly calculated China's average rate of change, and wrote a correct conclusion.

**Question 33**

33 The population of China, in millions, can be modeled by the function  $P(x) = 316.93e^{0.0133x}$ , where  $x$  is the number of years since 1900.

The population of India since 1900 is summarized in the table below:

Years since 1900	0	10	20	30	40	50	60	70	80	90	100	110	120
Population (millions)	243	254	268	285	324	376.3	450.6	555.1	699	873.3	1056.6	1234.3	1380

Which country's population had a greater average rate of change between 1950 and 2020?  
Justify your answer.

$$\frac{1563.5 - 616.267}{2} = \frac{1380 - 376.3}{2} = 1151$$

China

**Score 1:** The student showed correct differences in the numerators.

**Question 33**

33 The population of China, in millions, can be modeled by the function  $P(x) = 316.93e^{0.0133x}$ , where  $x$  is the number of years since 1900.

The population of India since 1900 is summarized in the table below:

Years since 1900	0	10	20	30	40	50	60	70	80	90	100	110	120
Population (millions)	243	254	268	285	324	376.3	450.6	555.1	699	873.3	1056.6	1234.3	1380

Which country's population had a greater average rate of change between 1950 and 2020? Justify your answer.

$$\text{China: } 316.93e^{0.0133(70)} = 804$$

$$\text{India: } \frac{120 - 50}{1380 - 376.3} = \frac{70}{1003.7} \approx 0.0697$$

(70)  
Not Correct

India has a greater rate of change between 1950 - 2020

**Score 0:** The student did not show enough correct work to receive any credit.

**Question 33**

33 The population of China, in millions, can be modeled by the function  $P(x) = 316.93e^{0.0133x}$ , where  $x$  is the number of years since 1900.

The population of India since 1900 is summarized in the table below:

Years since 1900	0	10	20	30	40	50	60	70	80	90	100	110	120
Population (millions)	243	254	268	285	324	376.3	450.6	555.1	699	873.3	1056.6	1234.3	1380

Which country's population had a greater average rate of change between 1950 and 2020? Justify your answer.

$$\text{China} \quad \frac{y_2 - y_1}{x_2 - x_1} = \frac{268 - 254}{20 - 10} = \frac{14}{10} = 1.4$$

$$\text{India} \quad \frac{y_2 - y_1}{x_2 - x_1} = \frac{413.51 - 364.43}{20 - 10} = \frac{49.08}{10} = 4.908$$

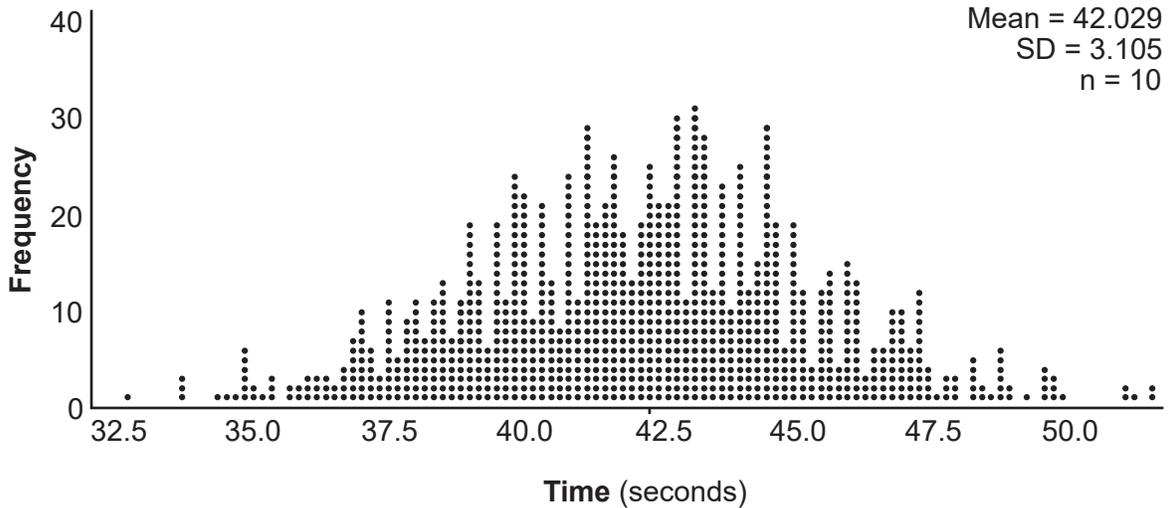
China's average rate of change between 1950 and 2020 is greater than India's average rate of change because China's average rate of change is 1.4 while India's is 4.908.

**Score 0:** The student did not satisfy the criteria for one or more credits.

**Question 34**

34 In a packaging plant, a machine packs boxes with jars. The machine's manufacturer states that a box is packed, on average, every 42 seconds. To test that claim, the packaging plant randomly selects a sample of 10 boxes and finds the sample mean to be 49.8 seconds.

The company ran a simulation of 1000 trials based on the manufacturer's claim. The approximately normal results are shown below.



Based on the simulation, determine an interval containing the middle <sup>250</sup>95% of plausible mean times. Round your answer to the *nearest hundredth*.

$$\begin{array}{r}
 42.029 \\
 + 6.21 \\
 \hline
 48.239
 \end{array}
 \qquad
 \begin{array}{r}
 42.029 \\
 - 6.21 \\
 \hline
 35.819
 \end{array}$$

35.82 to 48.24

Is the time 49.8 seconds unusual? Use statistical evidence to justify your answer.

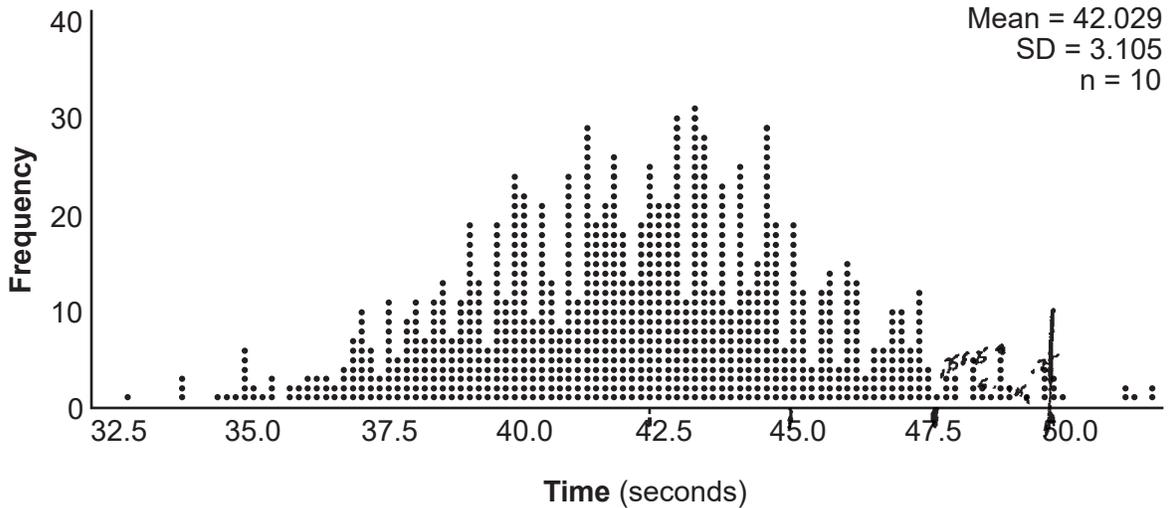
Yes because it falls out of the range in which we could be 95% sure.

**Score 4:** The student gave a complete and correct response.

**Question 34**

34 In a packaging plant, a machine packs boxes with jars. The machine's manufacturer states that a box is packed, on average, every 42 seconds. To test that claim, the packaging plant randomly selects a sample of 10 boxes and finds the sample mean to be 49.8 seconds.

The company ran a simulation of 1000 trials based on the manufacturer's claim. The approximately normal results are shown below.



Based on the simulation, determine an interval containing the middle 95% of plausible mean times. Round your answer to the nearest hundredth.

$$M.O.C = 2(3.105) \quad (35.82, 48.24)$$

$$M.o.c = 6.21$$

$$42.029 + 6.21 = 48.239$$

$$42.029 - 6.21 = 35.819$$

Is the time 49.8 seconds unusual? Use statistical evidence to justify your answer.

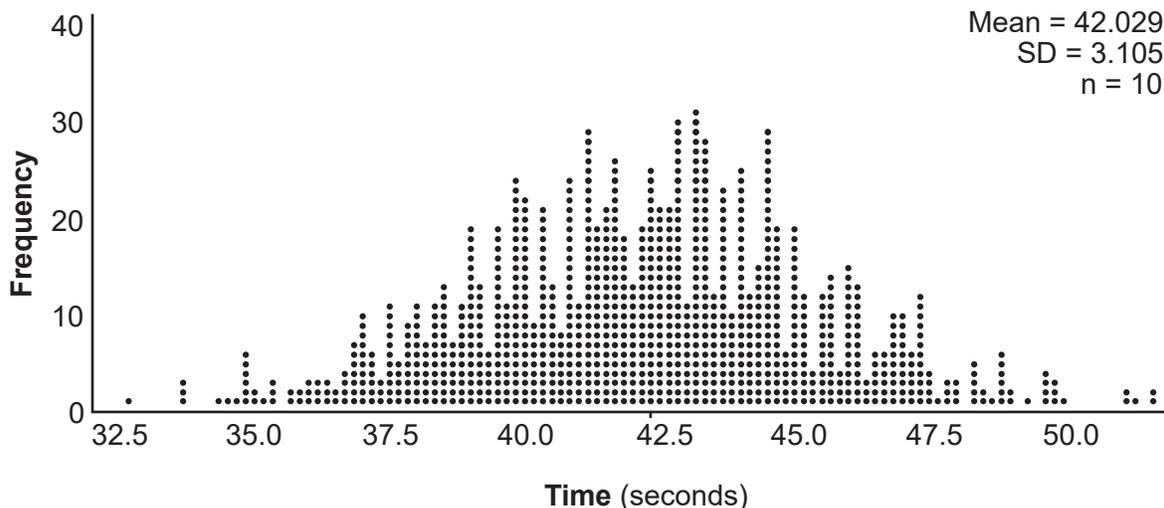
$\frac{9}{1000} = 0.009 = 0.9\%$  Yes very unusual,  
 it is not within the 95%  
 confidence interval and  
 49.8 seconds or greater  
 only happens 0.9% of  
 the time which is statistically  
 significant, so much so that  
 is very small.

**Score 4:** The student gave a complete and correct response.

**Question 34**

34 In a packaging plant, a machine packs boxes with jars. The machine's manufacturer states that a box is packed, on average, every 42 seconds. To test that claim, the packaging plant randomly selects a sample of 10 boxes and finds the sample mean to be 49.8 seconds.

The company ran a simulation of 1000 trials based on the manufacturer's claim. The approximately normal results are shown below.



Based on the simulation, determine an interval containing the <sup>-2 to 2</sup> middle 95% of plausible mean times. Round your answer to the nearest hundredth.

$$\text{mean} + 2(\text{SD}) \quad (35.819, 48.239)$$

$$\text{mean} - 2(\text{SD})$$

$$42.029 + 2(3.105) = 48.239$$

$$42.029 - 2(3.105) = 35.819$$

Is the time 49.8 seconds unusual? Use statistical evidence to justify your answer.

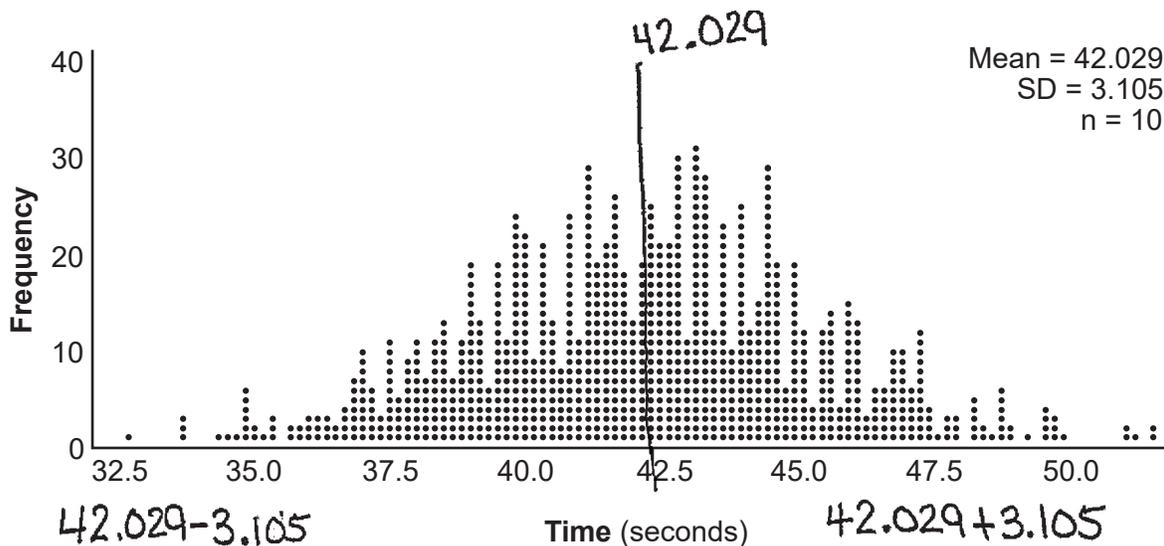
Yes because 49.8 falls outside the (35.819, 48.239) interval

**Score 3:** The student did not round to the nearest hundredth.

### Question 34

34 In a packaging plant, a machine packs boxes with jars. The machine's manufacturer states that a box is packed, on average, every 42 seconds. To test that claim, the packaging plant randomly selects a sample of 10 boxes and finds the sample mean to be 49.8 seconds.

The company ran a simulation of 1000 trials based on the manufacturer's claim. The approximately normal results are shown below.



Based on the simulation, determine an interval containing the middle 95% of plausible mean times. Round your answer to the *nearest hundredth*.

$$38.92 \text{ to } 45.134$$

Is the time 49.8 seconds unusual? Use statistical evidence to justify your answer.

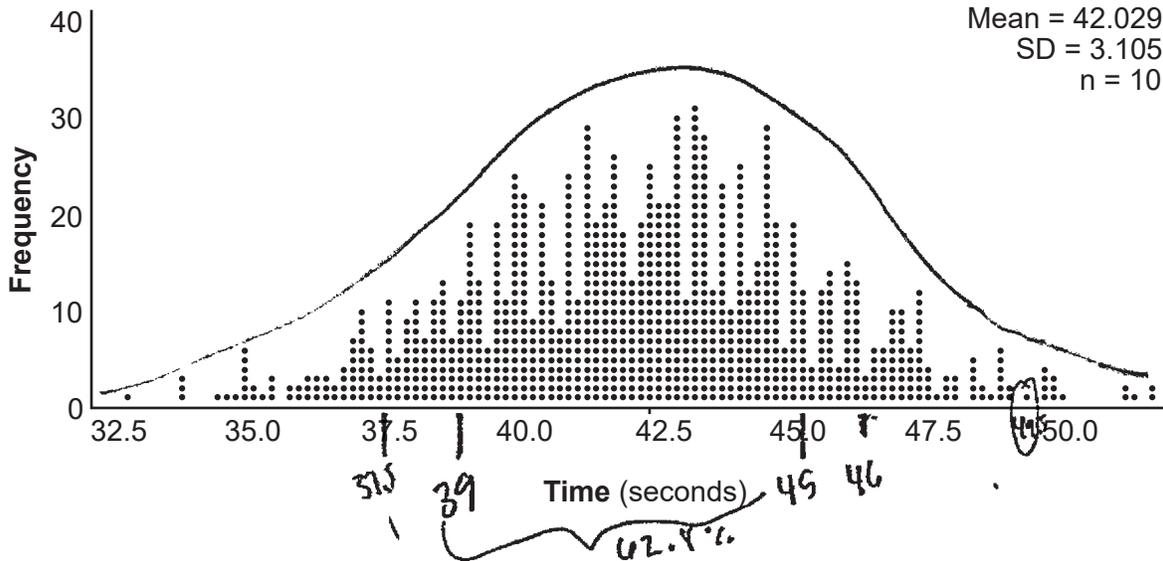
Yes, 49.8 sec. is unusual because it does not fall between the intervals.

**Score 2:** The student provided a complete justification.

**Question 34**

34 In a packaging plant, a machine packs boxes with jars. The machine's manufacturer states that a box is packed, on average, every 42 seconds. To test that claim, the packaging plant randomly selects a sample of 10 boxes and finds the sample mean to be 49.8 seconds.

The company ran a simulation of 1000 trials based on the manufacturer's claim. The approximately normal results are shown below.



Based on the simulation, determine an interval containing the middle 95% of plausible mean times. Round your answer to the *nearest hundredth*.

$(37.50, 46.00)$

Is the time 49.8 seconds unusual? Use statistical evidence to justify your answer.

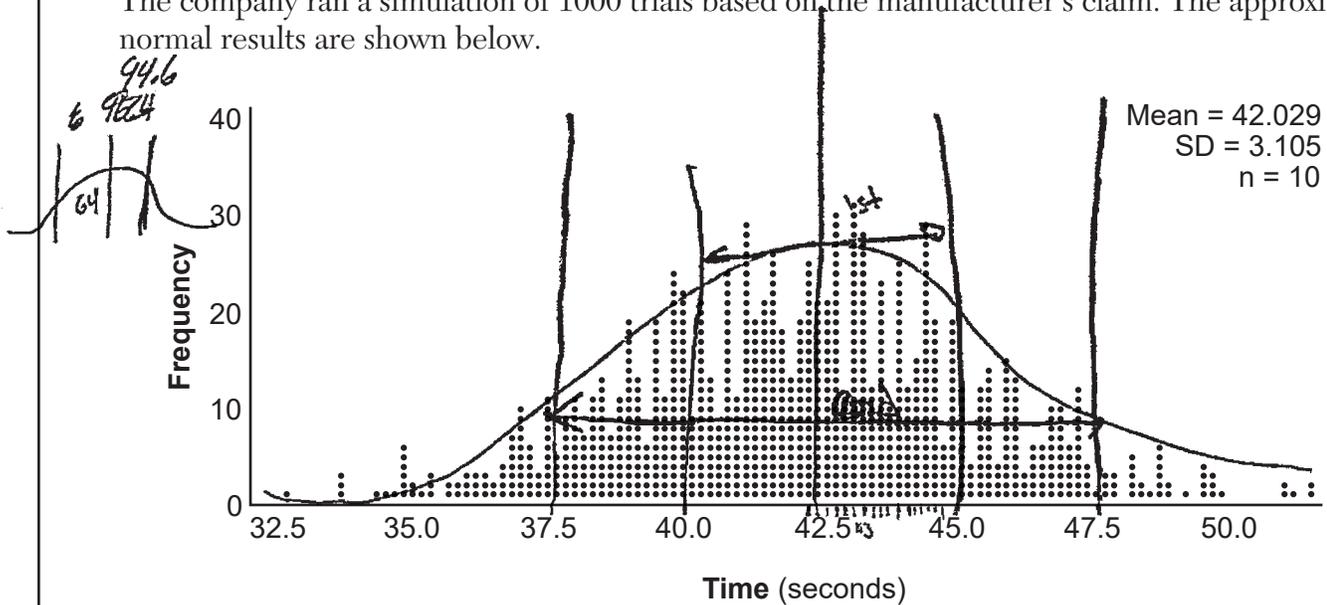
yes, 49.8 very rarely occurs

**Score 1:** The student provided an incomplete justification.

**Question 34**

34 In a packaging plant, a machine packs boxes with jars. The machine's manufacturer states that a box is packed, on average, every 42 seconds. To test that claim, the packaging plant randomly selects a sample of 10 boxes and finds the sample mean to be 49.8 seconds.

The company ran a simulation of 1000 trials based on the manufacturer's claim. The approximately normal results are shown below.



Based on the simulation, determine an interval containing the middle 95% of plausible mean times. Round your answer to the *nearest hundredth*.

10 seconds

$$37.5 \rightarrow 47.5$$

$$\begin{array}{r} 47.5 \\ -37.5 \\ \hline 10 \end{array}$$

Is the time 49.8 seconds unusual? Use statistical evidence to justify your answer.

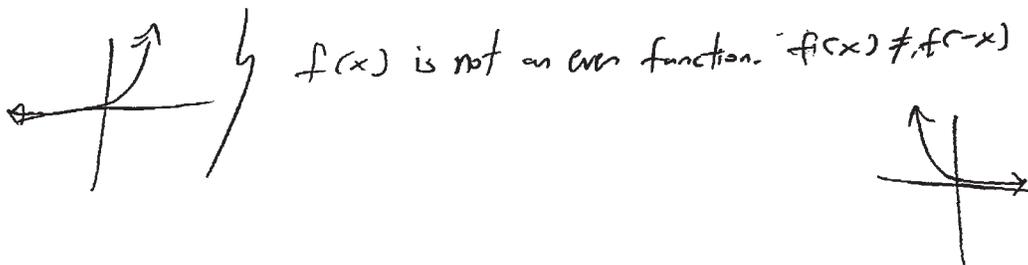
No it is above the 2nd notation and is greater than the 94.6 percent in the standard deviation

**Score 0:** The student did not satisfy the criteria for one or more credits.

**Question 35**

35 Consider the function  $f(x) = 2^x$ .

Is  $f(x)$  an even function? Justify your answer.



Write an equation for  $g(x)$ , the function that results after  $f(x)$  is shifted up 5 units.

$$g(x) = 2^x + 5$$

Write an equation for  $h(x)$ , the inverse of  $g(x)$ .

$$x = 2^y + 5$$

$$x - 5 = 2^y$$

$$\log_2(x - 5) = \log_2(2^y)$$

$$\log_2(x - 5) = y$$

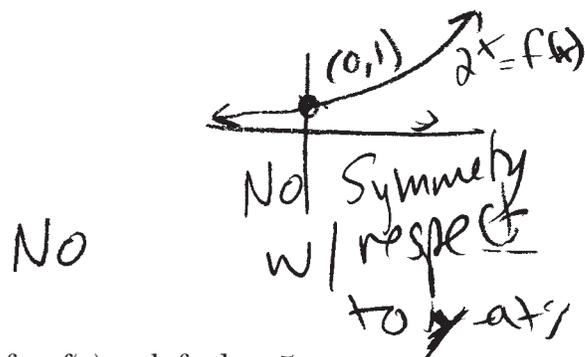
$$h(x) = \log_2(x - 5)$$

**Score 4:** The student gave a complete and correct response.

**Question 35**

35 Consider the function  $f(x) = 2^x$ .

Is  $f(x)$  an even function? Justify your answer.



Write an equation for  $g(x)$ , the function that results after  $f(x)$  is shifted up 5 units.

$$f(x) + 5 = g(x)$$

Write an equation for  $h(x)$ , the inverse of  $g(x)$ .

$$x = 2^y + 5$$
$$x - 5 = 2^y$$
$$\log(x - 5) = y \log 2$$
$$h(x) = \frac{\log(x - 5)}{\log 2}$$

**Score 4:** The student gave a complete and correct response.

**Question 35**

35 Consider the function  $f(x) = 2^x$ .

Is  $f(x)$  an even function? Justify your answer.

$$f(-x) = 2^{-x}$$

$$-f(x) = -2^x$$

(No)

Write an equation for  $g(x)$ , the function that results after  $f(x)$  is shifted up 5 units.

$$f(x) = 2^x$$

$$g(x) = 2^x + 5$$

Write an equation for  $h(x)$ , the inverse of  $g(x)$ .

$$y = 2^x + 5$$

$$x = 2^y + 5$$

$$x - 5 = 2^y$$

$$\frac{\log(x-5)}{\log(2)} = \frac{y \log 2}{\log 2}$$

$$h(x) = \frac{\log(x-5)}{\log(2)}$$

~~$h(x) = \log(x-5) - .30103$~~

~~$\log(x-5) - \log(2)$~~

**Score 3:** The student did not provide a sufficient justification.

**Question 35**

35 Consider the function  $f(x) = 2^x$ .

Is  $f(x)$  an even function? Justify your answer.

$f(x)$  is not an even function,  
It's exponential meaning there's  
no reflection or rotation on the graph.

Write an equation for  $g(x)$ , the function that results after  $f(x)$  is shifted up 5 units.

$$g(x) = 2^x + 5$$

Write an equation for  $h(x)$ , the inverse of  $g(x)$ .

$$y = 2^x + 5$$

$$x = 2^y + 5$$

$$x - 5 = 2^y$$

$$2^y = x - 5$$

$$\log_2 x - 5 = y$$

$$h(x) = \log_2 x - 5$$

**Score 2:** The student did not provide a sufficient justification and is missing parentheses when expressing  $h(x)$ .

**Question 35**

35 Consider the function  $f(x) = 2^x$ .

Is  $f(x)$  an even function? Justify your answer.

No, it's not symmetrical/equal when mirrored across the y-axis

Write an equation for  $g(x)$ , the function that results after  $f(x)$  is shifted up 5 units.

$$g(x) = 2^{x+5}$$

Write an equation for  $h(x)$ , the inverse of  $g(x)$ .

$$h(x) = -2^{x-5}$$

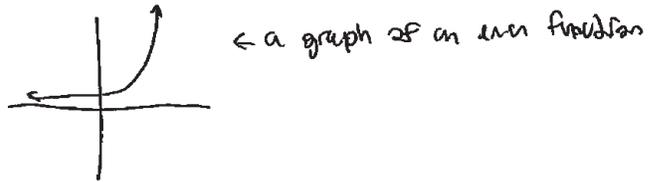
**Score 1:** The student provided a correct justification.

**Question 35**

35 Consider the function  $f(x) = 2^x$ .

Is  $f(x)$  an even function? Justify your answer.

$f(x)$  is an even function because when observing the graph



Write an equation for  $g(x)$ , the function that results after  $f(x)$  is shifted up 5 units.

$$g(x) = 2^x + 5$$

Write an equation for  $h(x)$ , the inverse of  $g(x)$ .

$$h(x) = 2^x + 5$$

$$y = 2^x + 5$$

$$y - 5 = 2^x$$

$$\log_2(y - 5) = x$$

**Score 1:** The student correctly stated an equation for  $g(x)$ .

**Question 35**

35 Consider the function  $f(x) = 2^x$ .

Is  $f(x)$  an even function? Justify your answer.

Yes - slope is going up to the right which makes it even.

Write an equation for  $g(x)$ , the function that results after  $f(x)$  is shifted up 5 units.

$$g(x) = 2^x - 5$$

Write an equation for  $h(x)$ , the inverse of  $g(x)$ .

$$x = 2^y - 5$$

$$x + 5 = 2^y$$

$$\log_2(x + 5) = y$$

$$h(x)^{-1} = \log_2(x + 5)$$

**Score 0:** The student did not satisfy the criteria for one or more credits.

**Question 35**

35 Consider the function  $f(x) = 2^x$ .

Is  $f(x)$  an even function? Justify your answer.

$f(x)$  is an even function because it is positive and it contains a coefficient and exponent

Write an equation for  $g(x)$ , the function that results after  $f(x)$  is shifted up 5 units.

$$f(x) = 2^x + 5$$

Write an equation for  $h(x)$ , the inverse of  $g(x)$ .

$$-2x - 5$$

**Score 0:** The student did not satisfy the criteria for one or more credits.

Question 36

36 Solve the system of equations shown below algebraically:

$$\begin{array}{l} (x-4)^2 + (y-1)^2 = 9 \\ x - y = 6 \\ \hline +y \\ \hline x = 6 + y \end{array}$$

$$(6+y-4)^2 + (y-1)^2 = 9$$

$$(2+y)^2 + (y-1)^2 = 9$$

$$(2+y)(2+y) + (y-1)(y-1) = 9$$

$$\underline{4+4y+y^2} + \underline{y^2-2y+1} = 9$$

$$2y^2 + 2y + 5 = 9$$

$$2y^2 + 2y - 4 = 0$$

$$2(y^2 + y - 2) = 0$$

$$\frac{2(y+2)(y-1)}{2 \neq 0} = 0$$

$$y = -2 \quad | \quad y = 1$$

$$\boxed{-2}$$

$$x - y = 6$$

$$x - (-2) = 6$$

$$x + 2 = 6$$

$$\boxed{x = 4}$$

$$\boxed{y = 1}$$

$$x - y = 6$$

$$x - 1 = 6$$

$$\boxed{x = 7}$$

$$\boxed{\begin{matrix} (4, -2) \\ (7, 1) \end{matrix}}$$

Score 4: The student gave a complete and correct response.

Question 36

36 Solve the system of equations shown below algebraically:

$$(x-4)(x-4)$$

$$(x-4)^2 + (y-1)^2 = 9$$

$$x - y = 6$$

$$-y = -x + 6$$

$$y = x - 6$$

$$(x-4)^2 + ((x-6)-1)^2 = 9$$

$$x^2 - 8x + 16 + x^2 - 14x + 49 = 9$$

$$2x^2 - 22x + 56 = 0$$

$$2(x^2 - 11x + 28) = 0$$

$$(x-7)(x-4) = 0$$

$$\frac{\quad}{x=7} \quad \frac{\quad}{x=4}$$

$$(7) - y = 6$$

$$-y = -1$$

$$\boxed{y=1}$$

$$(7, 1)$$

$$4 - y = 6$$

$$-y = 2$$

$$\boxed{y=-2}$$

$$(4, -2)$$

Score 4: The student gave a complete and correct response.

**Question 36**

**36** Solve the system of equations shown below algebraically:

$$(x - 4)^2 + (y - 1)^2 = 9$$

$$x - y = 6$$

$$\begin{array}{r} -x \quad -x \\ \hline \end{array}$$

$$\frac{-y = -x + 6}{-1}$$

$$y = x - 6$$

$$(x - 4)^2 + (x - 6 - 1)^2 = 9$$

$$x^2 - 4x - 4x + 16 + (x - 7)^2 = 9$$

$$x^2 - 8x + 16 + x^2 - 7x - 7x + 49 = 9$$

$$\begin{array}{r} x^2 - 8x + 16 + x^2 - 14x + 49 = 9 \\ \hline -49 -49 \end{array}$$

$$\begin{array}{r} 2x^2 - 22x + 16 = -40 \\ \hline -16 \quad -16 \end{array}$$

$$\frac{2x^2 - 22x = -56}{2}$$

$$\begin{array}{r} x^2 - 11x = -28 \\ \hline +28 \quad +28 \end{array}$$

$$x^2 - 11x + 28 = 0$$

$$(x - 7)(x - 4) = 0$$

$$\begin{array}{l} x = 7 \\ x = 4 \end{array}$$

**Score 3:** The student correctly found both values of  $x$ .

**Question 36**

36 Solve the system of equations shown below algebraically:

$$\begin{aligned} (x-4)^2 + (y-1)^2 &= 9 \\ x-y &= 6 \end{aligned}$$

$$\begin{aligned} x-y &= 6 \\ +y &+y \end{aligned}$$

$$x = 6+y$$

$$x-y = 6$$

$$\begin{aligned} x-1 &= 6 \\ +1 &+1 \end{aligned}$$

$$x = 7$$

$$\begin{aligned} x &= 7 \\ y &= 1 \\ \text{or} \\ y &= 2 \end{aligned}$$

$$(x-4)(x-4) + (y-1)(y-1) = 9$$

$$x^2 - 4x - 4x + 16 + y^2 - y - y + 1 = 9$$

$$x^2 - 8x + 16 + y^2 - 2y + 1 = 9$$

$$-17 \quad -17$$

$$x^2 - 8x + y^2 - 2y = -8$$

$$(y+6)(y+6) - 8(6+y) + y^2 - 2y = -8$$

$$y^2 + 6y + 6y + 36 - 48 - 8y + y^2 - 2y = -8$$

$$2y^2 + 2y - 12 = -8$$

$$+8 \quad +8$$

$$2y^2 + 2y - 4 = 0$$

$$2(y^2 + 1y - 2) = 0$$

$$\cancel{2}(y+2)(y-1) = \frac{0}{2}$$

$$(y+2)(y-1) = 0$$

$$\begin{aligned} y+2 &= 0 \\ -2 &-2 \end{aligned}$$

$$\begin{aligned} y-1 &= 0 \\ +1 &+1 \end{aligned}$$

$$y = 2$$

$$y = 1$$

**Score 3:** The student found one correct solution.



Question 36

36 Solve the system of equations shown below algebraically:

$$\begin{array}{l}
 (x+4)(x+4) \\
 x^2 + 4x + 4x + 16 \\
 x^2 + 8x + 16
 \end{array}
 \quad
 \begin{array}{l}
 (x-4)^2 + (y-1)^2 = 9 \\
 x - y = 6 \\
 \begin{array}{r}
 -x \quad -x \\
 \hline
 -y = -x + 6 \\
 \frac{-1}{-1} \quad \frac{-1}{-1} \quad \frac{+6}{-1} \\
 y = x - 6
 \end{array}
 \end{array}
 \quad
 \begin{array}{l}
 (x-6-1)(x-6-1) \\
 x^2 - 6x - x - 6x + 36 + 6 - x + 6 + 1 \\
 x^2 - 12x - 2x + 49 \\
 x^2 - 14x + 49
 \end{array}$$

$$\begin{array}{l}
 (x-4)^2 + (x-6-1)^2 = 9 \\
 x^2 + 8x + 16 + x^2 - 14x + 49 = 9
 \end{array}$$

$$\begin{array}{r}
 2x^2 - 6x + 65 = 9 \\
 \quad \quad -9 \quad -9 \\
 \hline
 2x^2 - 6x + 56 = 0
 \end{array}$$

$$\begin{array}{r}
 x - 7 = 0 \quad x + 4 = 0 \\
 +7 \quad +7 \quad \quad -4 \quad -4 \\
 \hline
 x = 7 \quad \quad x = -4
 \end{array}$$

$$\begin{array}{r}
 2x^2 - 6x + 56 = 0 \\
 \frac{2x^2}{2} - \frac{6x}{2} + \frac{56}{2} = 0 \\
 x^2 - 3x + 28
 \end{array}$$

$$X = \{7, -4\}$$

$$x^2 - 3x + 28$$

$$\begin{array}{l}
 \frac{28}{-7 \cdot 4} \quad \left| \begin{array}{l} -3 \\ -7 + 4 \end{array} \right. \quad (x-7)(x+4)
 \end{array}$$

$$\begin{array}{r}
 x = 7 \quad x = -4 \\
 y = 1 \quad y = -10
 \end{array}$$

Score 2: The student made one computational and one factoring error.

Question 36

36 Solve the system of equations shown below algebraically:

$$\begin{aligned}(x - 4)^2 + (y - 1)^2 &= 9 \\ x - y &= 6\end{aligned}$$

$$\begin{aligned}x - y &= 6 \\ -x &\quad -x \\ \hline -y &= 6 - x \\ -1 &\quad -1 \\ \hline y &= -6 + x\end{aligned}$$

$$\begin{aligned}(x - 4)^2 + (y - 1)^2 &= 9 \\ (x - 4)(x - 4) + (-6 + x - 1)(-6 + x - 1) &= 9 \\ x^2 - 4x + 4x + 16 + 36 - 6x + 6x + x^2 - x - x &= 9 \\ 2x^2 - 20x + 59 &= 9 \\ &\quad -9 \quad -9 \\ 2x^2 - 20x - 50 & \\ \begin{array}{r} \cancel{100} \\ \cancel{-10} \quad \cancel{-10} \\ \cancel{-20} \end{array} & \begin{array}{l} 2x^2 - 10x - 10x - 50 \\ 2x(x - 5) \quad | \quad -10(x - 5) \end{array} \\ \hline (2x - 10) & | (x - 5) \\ \hline 2x = 10 & \quad | \quad x = 5 \\ \hline x = 5 & \end{array}$$

**Score 1:** The student wrote a correct quadratic equation in one variable.

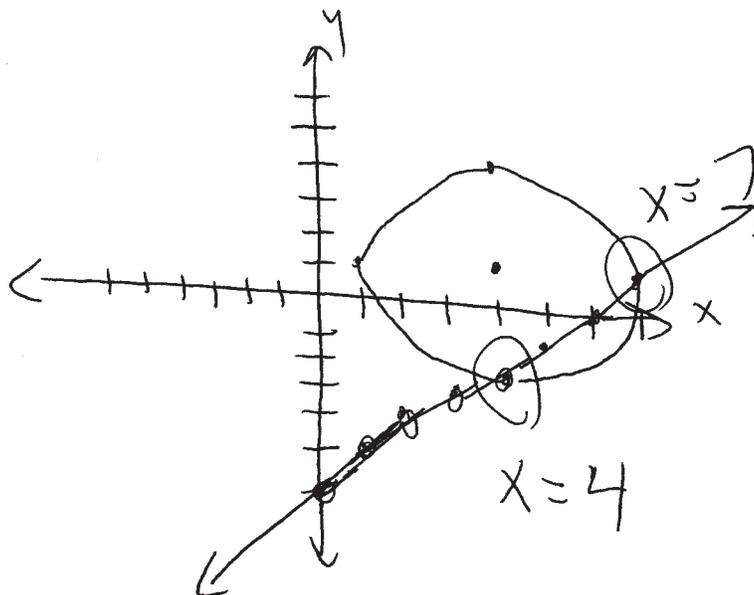
Question 36

36 Solve the system of equations shown below algebraically:

$$\begin{aligned}(x - 4)^2 + (y - 1)^2 &= 9 \\ x - y &= 6\end{aligned}$$

$$\begin{array}{r} -6 + y \quad -6 + y \\ \hline x - 6 = y \end{array}$$

$$\begin{aligned}(h, k) &= (4, 1) \\ r &= 3\end{aligned}$$



**Score 1:** The student solved graphically and only stated the x-values.

Question 36

36 Solve the system of equations shown below algebraically:

	$y$	$+8$
$y$	$y^2$	$8y$
$4$	$4y$	$32$

	$y$	$+1$
$y$	$y^2$	$y$
$-1$	$-y$	$-1$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$y = (-3 \pm 32i) - 6$$

$$\begin{aligned} &\Rightarrow (x+2)(x-2) + (y+1)(y-1) = 9 \\ &\Rightarrow (x-4)^2 + (y-1)^2 = 9 \\ &x - y = 6 \quad y = x - 6 \\ &x = y + 6 \end{aligned}$$

$$(y+8)(y+4) + (y+1)(y-1) = 9$$

$$y^2 + 12y + 32 + y^2 - 1 = 9$$

$$2y^2 + 12y + 31 = 9$$

$$-9 - 9$$

$$2y^2 + 12y + 22 = 0$$

$$x = \frac{-(12) \pm \sqrt{(12)^2 - 4(2)(22)}}{2(2)}$$

$$x = \frac{-12 \pm \sqrt{-32}}{4}$$

$$x = -3 \pm \frac{\sqrt{-32}}{4}$$

$$x = -3 \pm 32i$$

**Score 0:** The student did not satisfy the criteria for one or more credits.

### Question 37

37 Taylor wants to open an investment account with the \$1200 she received for her birthday. She has narrowed her choices down to two banks. America's Bank offers 6.4% annual interest compounded quarterly. Barnyard Bank offers 6.35% annual interest compounded continuously.

Write functions for  $A(t)$  and  $B(t)$  to represent the value of her investment with America's Bank and Barnyard Bank as a function of time,  $t$ , in years.

$$1200 \left(1 + \frac{r}{n}\right)^{nt}$$
$$A(t) = 1200 \left(1 + \frac{0.064}{4}\right)^{4t} \rightarrow \underline{A(t) = 1200(1.016)^{4t}}$$
$$\underline{B(t) = 1200(e)^{0.0635t}}$$

Taylor would like to invest the \$1200 into one bank for ten years making no additional deposits and no withdrawals. With which bank will Taylor earn the most money? Justify your answer.

$$A(t) = 1200(1.016)^{40} = 2264.28$$

$$\underline{B(t) = 1200e^{0.0635(10)} = \boxed{2264.43}}$$

She should choose bank B (Barnyard Bank)

Question 37 is continued on the next page.

**Score 6:** The student gave a complete and correct response.

### Question 37

Taylor chooses to invest her money in Barnyard Bank. Algebraically determine how long, to the nearest tenth of a year, it will take her initial investment to triple assuming she makes no deposits or withdrawals.

$$\frac{3600}{1200} = \frac{1200 e^{0.0635t}}{1200}$$

$$3 = e^{0.0635t}$$

$$\log_e 3 = 0.0635t$$

$$\textcircled{17.3} = \frac{1.098612289}{0.0635} = \frac{0.0635t}{0.0635}$$

**Question 37**

37 Taylor wants to open an investment account with the \$1200 she received for her birthday. She has narrowed her choices down to two banks. America's Bank offers 6.4% annual interest compounded quarterly. Barnyard Bank offers 6.35% annual interest compounded continuously.

Write functions for  $A(t)$  and  $B(t)$  to represent the value of her investment with America's Bank and Barnyard Bank as a function of time,  $t$ , in years.

$$A(t) = 1200 \left( 1 + \frac{.064}{4} \right)^{4t}$$

$$B(t) = 1200 (1 + .0635)^t$$

Taylor would like to invest the \$1200 into one bank for ten years making no additional deposits and no withdrawals. With which bank will Taylor earn the most money? Justify your answer.

$$A(t) = 1200 \left( 1 + \frac{.064}{4} \right)^{4t}$$

$$A(t) = 1200 (1.016)^{4(10)}$$

$$A(t) = \$2264.28$$

↑  
America's Bank  
will earn the most  
money.

$$B(t) = 1200 (1.0635)^{10}$$

$$B(t) = \$2221.04$$

Question 37 is continued on the next page.

**Score 5:** The student wrote the incorrect equation for  $B(t)$ .

### Question 37

Taylor chooses to invest her money in Barnyard Bank. Algebraically determine how long, to the *nearest tenth of a year*, it will take her initial investment to triple assuming she makes no deposits or withdrawals.

$$\frac{3600}{1200} = \frac{1200}{1200} (1.0635)^t$$

$$3 = (1.0635)^t$$

$$\log 3 = \frac{\log 1.0635^t}{\log 1.0635}$$

$$\log 3 = \frac{t \log 1.0635}{\log 1.0635}$$

$$17.9 = t$$

**Question 37**

37 Taylor wants to open an investment account with the \$1200 she received for her birthday. She has narrowed her choices down to two banks. America's Bank offers 6.4% annual interest compounded quarterly. Barnyard Bank offers 6.35% annual interest compounded continuously.

Write functions for  $A(t)$  and  $B(t)$  to represent the value of her investment with America's Bank and Barnyard Bank as a function of time,  $t$ , in years.

$$A(t) = 1200 \left(1 + \frac{0.064}{4}\right)^{4t}$$

$$B(t) = 1200e^{0.0635t}$$

Taylor would like to invest the \$1200 into one bank for ten years making no additional deposits and no withdrawals. With which bank will Taylor earn the most money? Justify your answer.

$$A(t) = 1200 \left(1 + \frac{0.064}{4}\right)^{40}$$

$$B(t) = 1200e^{0.2540}$$

$$A(t) = 2267.29$$

$$B(t) = 1547.01$$

America's Bank  
 $2267.29 > 1547.01$

$$\begin{array}{r} 1.2 \\ 635 \\ \hline 2540 \end{array}$$

Question 37 is continued on the next page.

**Score 5:** The student incorrectly evaluated  $B(4)$  rather than  $B(10)$ .

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**Question 37**

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Taylor chooses to invest her money in Barnyard Bank. Algebraically determine how long, to the *nearest tenth of a year*, it will take her initial investment to triple assuming she makes no deposits or withdrawals.

$$3600 = 1200e^{0.0635t}$$

$$3 = e^{0.0635t}$$

$$\ln(3) = 0.0635t$$

$$t = 17.3 \text{ years}$$

**Question 37**

37 Taylor wants to open an investment account with the \$1200 she received for her birthday. She has narrowed her choices down to two banks. America's Bank offers 6.4% annual interest compounded quarterly. Barnyard Bank offers 6.35% annual interest compounded continuously.

Write functions for  $A(t)$  and  $B(t)$  to represent the value of her investment with America's Bank and Barnyard Bank as a function of time,  $t$ , in years.

$$A(t) = 1200(.064)^{4t}$$

$$B(t) = 1200e^{.0635t}$$

Taylor would like to invest the \$1200 into one bank for ten years making no additional deposits and no withdrawals. With which bank will Taylor earn the most money? Justify your answer.

$$A(t) = 1200(.064)^{4(10)} = 2212021647773$$

$$B(t) = 1200e^{.0635(10)} = 2264.42656975$$

Taylor should choose Barnyard Bank.

Question 37 is continued on the next page.

**Score 4:** The student wrote an incorrect equation for  $A(t)$  and incorrectly evaluated  $A(10)$ .

Question 37

Taylor chooses to invest her money in Barnyard Bank. Algebraically determine how long, to the nearest tenth of a year, it will take her initial investment to triple assuming she makes no deposits or withdrawals.

$$\frac{3600}{1200} = \frac{1200e^{.0635t}}{1200}$$

$$3 = e^{.0635t}$$

$$\ln 3 = \ln e^{.0635t}$$

$$\frac{\ln 3}{.0635} = \frac{.0635t}{.0635}$$

$$t \approx 17.3009809239$$

It will take  
17.3 years.

Question 37

37 Taylor wants to open an investment account with the \$1200 she received for her birthday. She has narrowed her choices down to two banks. America's Bank offers 6.4% annual interest compounded quarterly. Barnyard Bank offers 6.35% annual interest compounded continuously.

Write functions for  $A(t)$  and  $B(t)$  to represent the value of her investment with America's Bank and Barnyard Bank as a function of time,  $t$ , in years.

$$A(T) = 1200 \left(1 + \frac{0.064}{4}\right)^{4t}$$

America

$$B(T) = 1200e^{0.0635t}$$

Barnyard

Taylor would like to invest the \$1200 into one bank for ten years making no additional deposits and no withdrawals. With which bank will Taylor earn the most money? Justify your answer.

$$1200 \left(1 + \frac{0.064}{4}\right)^{4(10)} = \cancel{\$2264.277}$$
$$1200e^{0.0635(10)} = \$2264.426$$

Barnyard Bank of America

Question 37 is continued on the next page.

Score 4: The student incorrectly solved for the time it takes for the deposit to triple.

### Question 37

Taylor chooses to invest her money in Barnyard Bank. Algebraically determine how long, to the *nearest tenth of a year*, it will take her initial investment to triple assuming she makes no deposits or withdrawals.

$$\frac{3600 = 1200e^{0.0635t}}{1200e}$$

$$\frac{8.154 = 0.0635t}{0.0635}$$

$$129.4 \text{ years}$$

### Question 37

37 Taylor wants to open an investment account with the \$1200 she received for her birthday. She has narrowed her choices down to two banks. America's Bank offers 6.4% annual interest compounded quarterly. Barnyard Bank offers 6.35% annual interest compounded continuously.

Write functions for  $A(t)$  and  $B(t)$  to represent the value of her investment with America's Bank and Barnyard Bank as a function of time,  $t$ , in years.

$$A(t) = 1200(1 + 0.064)^{4t}$$

$$B(t) = 1200e^{.0635t}$$

Taylor would like to invest the \$1200 into one bank for ten years making no additional deposits and no withdrawals. With which bank will Taylor earn the most money? Justify your answer.

$$1200(1 + 0.064)^{4(10)} = 14349.82$$

She should choose America's bank.

$$(1200)e^{.0635(10)} = 762$$

↓ greater than

Question 37 is continued on the next page.

**Score 3:** The student wrote an incorrect equation for  $A(t)$ , incorrectly evaluated  $B(10)$ , and made a rounding error.

Question 37

Taylor chooses to invest her money in Barnyard Bank. Algebraically determine how long, to the nearest tenth of a year, it will take her initial investment to triple assuming she makes no deposits or withdrawals.

17 years

$$\frac{3600}{1200} = \frac{1200 e^{.0635t}}{1200}$$

$$(1n) \quad 3 = e^{.0635t} \quad (1n)$$

$$\ln 3 = .0635t$$

Question 37

37 Taylor wants to open an investment account with the \$1200 she received for her birthday. She has narrowed her choices down to two banks. America's Bank offers 6.4% annual interest compounded quarterly. Barnyard Bank offers 6.35% annual interest compounded continuously.

Write functions for  $A(t)$  and  $B(t)$  to represent the value of her investment with America's Bank and Barnyard Bank as a function of time,  $t$ , in years.

America  
Bank

$$A(t) = 1200 \left(1 + \frac{0.064}{4}\right)^{4t}$$

Barnyard

$$B(t) = 1200 e^{(0.0635)t}$$

Taylor would like to invest the \$1200 into one bank for ten years making no additional deposits and no withdrawals. With which bank will Taylor earn the most money? Justify your answer.

$$A(t) = 1200 \left(1 + \frac{0.064}{4}\right)^{40}$$

$$A(t) = 1,248.58$$

$$B(t) = 1200 e^{(0.0635)(10)}$$

$$B(t) \approx 2,264.43$$

∴ Taylor should use Barnyard Bank

Question 37 is continued on the next page.

**Score 3:** The student wrote an incorrect equation for  $A(t)$ , but provided a correct justification.

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**Question 37**

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Taylor chooses to invest her money in Barnyard Bank. Algebraically determine how long, to the *nearest tenth of a year*, it will take her initial investment to triple assuming she makes no deposits or withdrawals.

$$\frac{3600}{1200} = \frac{\cancel{1200} e^{(.0635)(t)}}{\cancel{1200}}$$
$$3 = e^{(.0635)(t)}$$

**Question 37**

37 Taylor wants to open an investment account with the \$1200 she received for her birthday. She has narrowed her choices down to two banks. America's Bank offers 6.4% annual interest compounded quarterly. Barnyard Bank offers 6.35% annual interest compounded continuously.

Write functions for  $A(t)$  and  $B(t)$  to represent the value of her investment with America's Bank and Barnyard Bank as a function of time,  $t$ , in years.

A

$$1200(1 + 0.064)^{4t}$$

B

Per t

$$1200 e^{(0.0635)t}$$

Taylor would like to invest the \$1200 into one bank for ten years making no additional deposits and no withdrawals. With which bank will Taylor earn the most money? Justify your answer.

$$2231.50$$

$$2264.43$$

Barnyard because she will get more money

**Question 37 is continued on the next page.**

**Score 2:** The student provided an appropriate justification for choosing Barnyard Bank.

Question 37

Taylor chooses to invest her money in Barnyard Bank. Algebraically determine how long, to the nearest tenth of a year, it will take her initial investment to triple assuming she makes no deposits or withdrawals.

Around 17 years

$$3600 \quad | \quad 1200 e^{(.0675)t}$$
$$1200$$
$$3$$

Question 37

37 Taylor wants to open an investment account with the \$1200 she received for her birthday. She has narrowed her choices down to two banks. America's Bank offers 6.4% annual interest compounded quarterly. Barnyard Bank offers 6.35% annual interest compounded continuously.

Write functions for  $A(t)$  and  $B(t)$  to represent the value of her investment with America's Bank and Barnyard Bank as a function of time  $t$ , in years.

$$A(t) = 1200 \left( \frac{0.064}{4} \right)^{\frac{t}{12}}$$

$$B(t) = 1200 \left( \frac{0.0635}{365} \right)^{\frac{t}{12}}$$

Taylor would like to invest the \$1200 into one bank for ten years making no additional deposits and no withdrawals. With which bank will Taylor earn the most money? Justify your answer.

~~America's Bank, receives more interest in 10 year period.~~

$$A(10) = 38.25$$

$$B(10) = .884$$

Question 37 is continued on the next page.

**Score 1:** The student correctly evaluated their incorrect equations at 10 years.

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**Question 37**

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Taylor chooses to invest her money in Barnyard Bank. Algebraically determine how long, to the *nearest tenth of a year*, it will take her initial investment to triple assuming she makes no deposits or withdrawals.

$$B(t) = 1200 \left( \frac{0.0635}{365} \right)^{\frac{t}{12}}$$

### Question 37

37 Taylor wants to open an investment account with the \$1200 she received for her birthday. She has narrowed her choices down to two banks. America's Bank offers 6.4% annual interest compounded quarterly. Barnyard Bank offers 6.35% annual interest compounded continuously.

Write functions for  $A(t)$  and  $B(t)$  to represent the value of her investment with America's Bank and Barnyard Bank as a function of time,  $t$ , in years.

$$A(t) = 1200(1 + 0.064)^{\frac{t}{4}}$$

$$B(t) = 1200(1 + 0.0635)^t$$

Taylor would like to invest the \$1200 into one bank for ten years making no additional deposits and no withdrawals. With which bank will Taylor earn the most money? Justify your answer.

she should chose America's bank.

Question 37 is continued on the next page.

**Score 0:** The student did not satisfy the criteria for one or more credits.

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**Question 37**

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Taylor chooses to invest her money in Barnyard Bank. Algebraically determine how long, to the *nearest tenth of a year*, it will take her initial investment to triple assuming she makes no deposits or withdrawals.

23.6 years