

The University of the State of New York

REGENTS HIGH SCHOOL EXAMINATION

MATHEMATICS B

Wednesday, June 20, 2001 — 9:15 a.m. to 12:15 p.m., only

Print Your Name:

Print Your School's Name:

Print your name and the name of your school in the boxes above. Then turn to the last page of this booklet, which is the answer sheet for Part I. Fold the last page along the perforations and, slowly and carefully, tear off the answer sheet. Then fill in the heading of your answer sheet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. Any work done on this sheet of scrap graph paper will *not* be scored. All work should be written in pen, except graphs and drawings, which should be done in pencil.

This examination has four parts, with a total of 34 questions. You must answer all questions in this examination. Write your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers to the questions in Parts II, III, and IV directly in this booklet. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. The formulas that you may need to answer some questions in this examination are found on page 2.

When you have completed the examination, you must sign the statement printed at the end of the answer sheet, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer sheet cannot be accepted if you fail to sign this declaration.

Notice...

A graphing calculator, a straightedge (ruler), and a compass must be available for your use while taking this examination.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN.

Formulas

Area of Triangle

$$K = \frac{1}{2} ab \sin C$$

Functions of the Sum of Two Angles

$$\sin(A + B) = \sin A \cos B + \cos A \sin B$$

$$\cos(A + B) = \cos A \cos B - \sin A \sin B$$

Functions of the Difference of Two Angles

$$\sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A - B) = \cos A \cos B + \sin A \sin B$$

Law of Sines

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Law of Cosines

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Functions of the Double Angle

$$\sin 2A = 2 \sin A \cos A$$

$$\cos 2A = \cos^2 A - \sin^2 A$$

$$\cos 2A = 2 \cos^2 A - 1$$

$$\cos 2A = 1 - 2 \sin^2 A$$

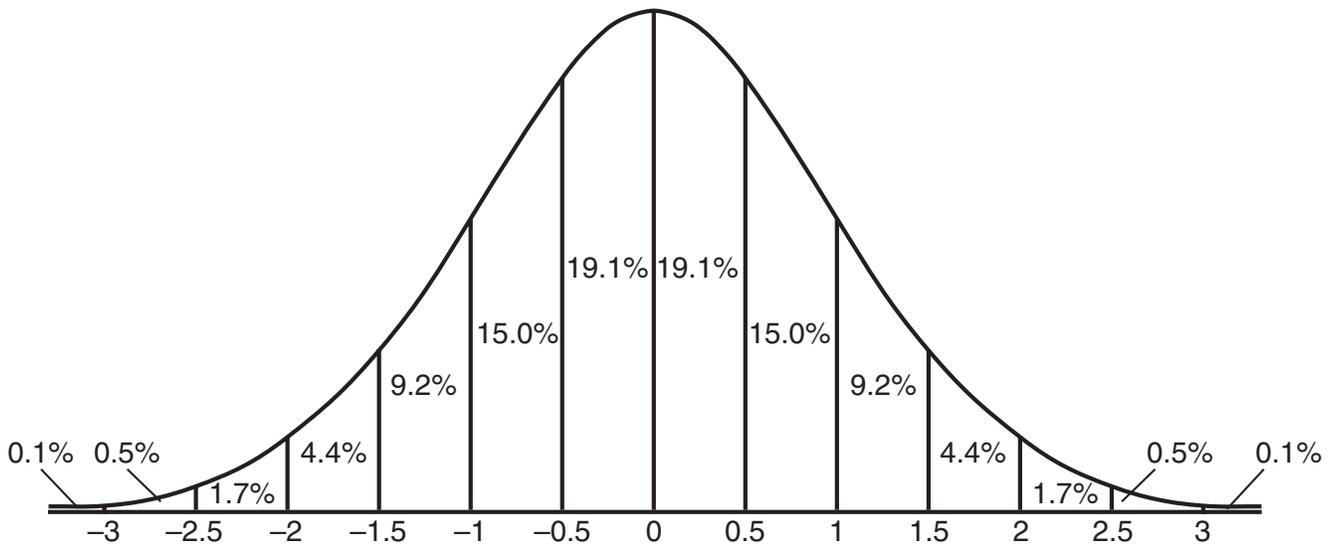
Functions of the Half Angle

$$\sin \frac{1}{2} A = \pm \sqrt{\frac{1 - \cos A}{2}}$$

$$\cos \frac{1}{2} A = \pm \sqrt{\frac{1 + \cos A}{2}}$$

Normal Curve

Standard Deviation



Part I

Answer all questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Record your answers in the spaces provided on the separate answer sheet. [40]

Use this space for
computations.

- 1 An archer shoots an arrow into the air such that its height at any time, t , is given by the function $h(t) = -16t^2 + kt + 3$. If the maximum height of the arrow occurs at time $t = 4$, what is the value of k ?

- (1) 128 (3) 8
(2) 64 (4) 4

- 2 The magnitude (R) of an earthquake is related to its intensity (I) by $R = \log \left(\frac{I}{T} \right)$, where T is the threshold below which the earthquake is not noticed. If the intensity is doubled, its magnitude can be represented by

- (1) $2(\log I - \log T)$
(2) $\log I - \log T$
(3) $2 \log I - \log T$
(4) $\log 2 + \log I - \log T$

- 3 Jacob is solving a quadratic equation. He executes a program on his graphing calculator and sees that the roots are real, rational, and unequal. This information indicates to Jacob that the discriminant is

- (1) zero (3) a perfect square
(2) negative (4) not a perfect square

- 4 Camisha is paying a band \$330 to play at her graduation party. The amount each member earns, d , varies inversely as the number of members who play, n . The graph of the equation that represents the relationship between d and n is an example of

- (1) a hyperbola (3) a parabola
(2) a line (4) an ellipse

- 5 A modulated laser heats a diamond. Its variable temperature, in degrees Celsius, is given by $f(t) = T \sin at$. What is the period of the curve?

- (1) $|T|$ (3) $\frac{1}{a}$
(2) $\frac{2\pi}{a}$ (4) $\frac{2a\pi}{a}$

6 The circumference of a circular plot of land is increased by 10%. What is the best estimate of the total percentage that the area of the plot increased?

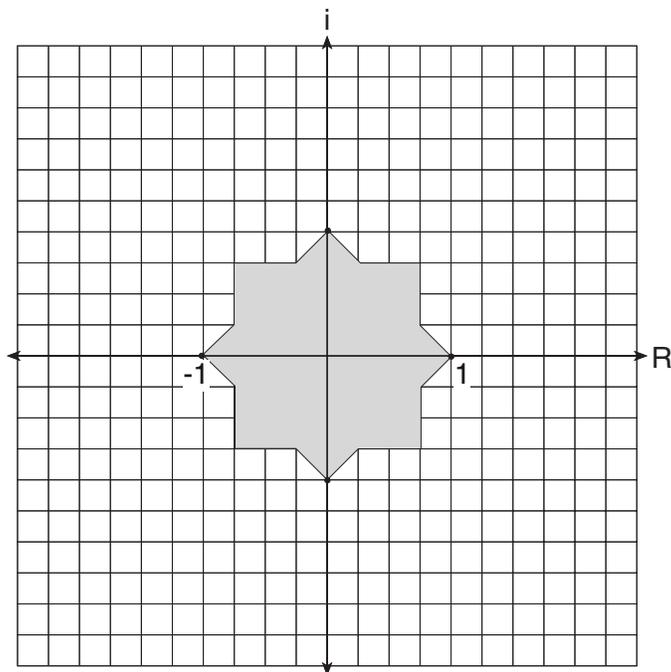
- (1) 10% (3) 25%
 (2) 21% (4) 31%

Use this space for computations.

7 Which equation states that the temperature, t , in a room is less than 3° from 68° ?

- (1) $|3 - t| < 68$ (3) $|68 - t| < 3$
 (2) $|3 + t| < 68$ (4) $|68 + t| < 3$

8 Fractal geometry uses the complex number plane to draw diagrams, such as the one shown in the accompanying graph.



Which number is *not* included in the shaded area?

- (1) $-0.5i$ (3) -0.9
 (2) $-0.5 - 0.5i$ (4) $-0.9 - 0.9i$

- 9 The relationship of a woman's shoe size and length of a woman's foot, in inches, is given in the accompanying table.

Use this space for computations.

Woman's Shoe Size	5	6	7	8
Foot Length (in)	9.00	9.25	9.50	9.75

The linear correlation coefficient for this relationship is

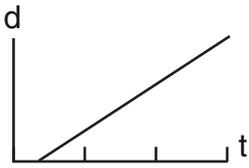
- (1) 1 (3) 0.5
(2) -1 (4) 0
- 10 The center of a circular sunflower with a diameter of 4 centimeters is $(-2,1)$. Which equation represents the sunflower?
- (1) $(x - 2)^2 + (y + 1)^2 = 2$
(2) $(x + 2)^2 + (y - 1)^2 = 4$
(3) $(x - 2)^2 + (y - 1)^2 = 4$
(4) $(x + 2)^2 + (y - 1)^2 = 2$
- 11 Melissa and Joe are playing a game with complex numbers. If Melissa has a score of $5 - 4i$ and Joe has a score of $3 + 2i$, what is their total score?
- (1) $8 + 6i$ (3) $8 - 6i$
(2) $8 + 2i$ (4) $8 - 2i$
- 12 In a science experiment, when resistor A and resistor B are connected in a parallel circuit, the total resistance is $\frac{1}{\frac{1}{A} + \frac{1}{B}}$. This complex fraction is equivalent to
- (1) 1 (3) $A + B$
(2) $\frac{AB}{A + B}$ (4) AB

Use this space for computations.

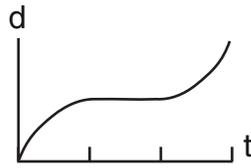
13 A store advertises that during its Labor Day sale \$15 will be deducted from every purchase over \$100. In addition, after the deduction is taken, the store offers an early-bird discount of 20% to any person who makes a purchase before 10 a.m. If Hakeem makes a purchase of x dollars, $x > 100$, at 8 a.m., what, in terms of x , is the cost of Hakeem's purchase?

- (1) $0.20x - 15$ (3) $0.85x - 20$
(2) $0.20x - 3$ (4) $0.80x - 12$

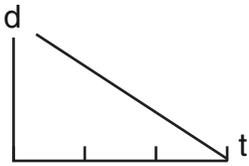
14 A bug travels up a tree, from the ground, over a 30-second interval. It travels fast at first and then slows down. It stops for 10 seconds, then proceeds slowly, speeding up as it goes. Which sketch best illustrates the bug's distance (d) from the ground over the 30-second interval (t)?



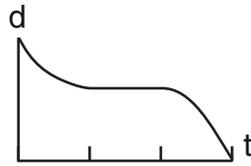
(1)



(3)



(2)



(4)

15 The inverse of a function is a logarithmic function in the form $y = \log_b x$. Which equation represents the original function?

- (1) $y = b^x$ (3) $x = b^y$
(2) $y = bx$ (4) $by = x$

Use this space for computations.

16 On her first trip, Sari biked 24 miles in T hours. The following week Sari biked 32 miles in T hours. Determine the ratio of her average speed on her second trip to her average speed on her first trip.

(1) $\frac{3}{4}$

(3) $\frac{4}{3}$

(2) $\frac{2}{3}$

(4) $\frac{3}{2}$

17 What is the value of $\sum_{m=1}^3 (2m + 1)^{m-1}$?

(1) 15

(3) 57

(2) 55

(4) 245

18 If θ is an obtuse angle and $\sin \theta = b$, then it can be concluded that

(1) $\tan \theta > b$

(3) $\cos 2\theta > b$

(2) $\cos \theta > b$

(4) $\sin 2\theta < b$

19 Main Street and Central Avenue intersect, making an angle measuring 34° . Angela lives at the intersection of the two roads, and Caitlin lives on Central Avenue 10 miles from the intersection. If Leticia lives 7 miles from Caitlin, which conclusion is valid?

(1) Leticia cannot live on Main Street.

(2) Leticia can live at only one location on Main Street.

(3) Leticia can live at one of two locations on Main Street.

(4) Leticia can live at one of three locations on Main Street.

20 Through how many radians does the minute hand of a clock turn in 24 minutes?

(1) 0.2π

(3) 0.6π

(2) 0.4π

(4) 0.8π

Part II

Answer all questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [12]

21 Gregory wants to build a garden in the shape of an isosceles triangle with one of the congruent sides equal to 12 yards. If the area of his garden will be 55 square yards, find, to the *nearest tenth of a degree*, the *three* angles of the triangle.

22 At a certain intersection, the light for eastbound traffic is red for 15 seconds, yellow for 5 seconds, and green for 30 seconds. Find, to the *nearest tenth*, the probability that out of the next eight eastbound cars that arrive randomly at the light, exactly three will be stopped by a red light.

23 The cost of a long-distance telephone call is determined by a flat fee for the first 5 minutes and a fixed amount for each additional minute. If a 15-minute telephone call costs \$3.25 and a 23-minute call costs \$5.17, find the cost of a 30-minute call.

24 A rectangular prism has a length of $\frac{2x^2+2x-24}{4x^2+x}$, a width of $\frac{x^2+x-6}{x+4}$, and a height of $\frac{8x^2+2x}{x^2-9}$. For all values of x for which it is defined, express, in terms of x , the volume of the prism in simplest form.

25 The scientists in a laboratory company raise amebas to sell to schools for use in biology classes. They know that one ameba divides into two amebas every hour and that the formula $t = \log_2 N$ can be used to determine how long in hours, t , it takes to produce a certain number of amebas, N . Determine, to the *nearest tenth of an hour*, how long it takes to produce 10,000 amebas if they start with one ameba.

26 Professor Bartrich has 184 students in her mathematics class. The scores on the final examination are normally distributed and have a mean of 72.3 and a standard deviation of 8.9. How many students in the class can be expected to receive a score between 82 and 90?

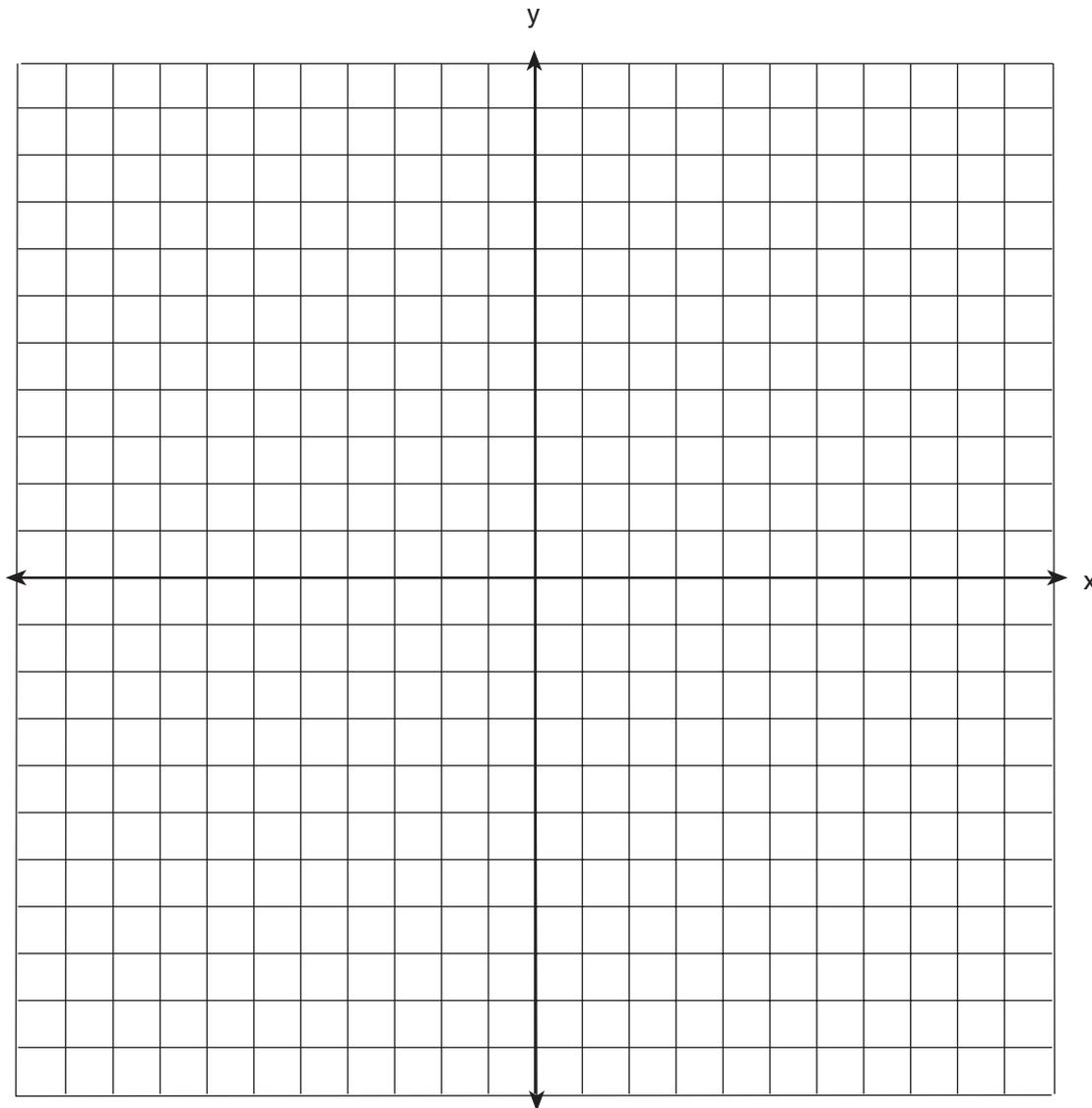
Part III

Answer all questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [24]

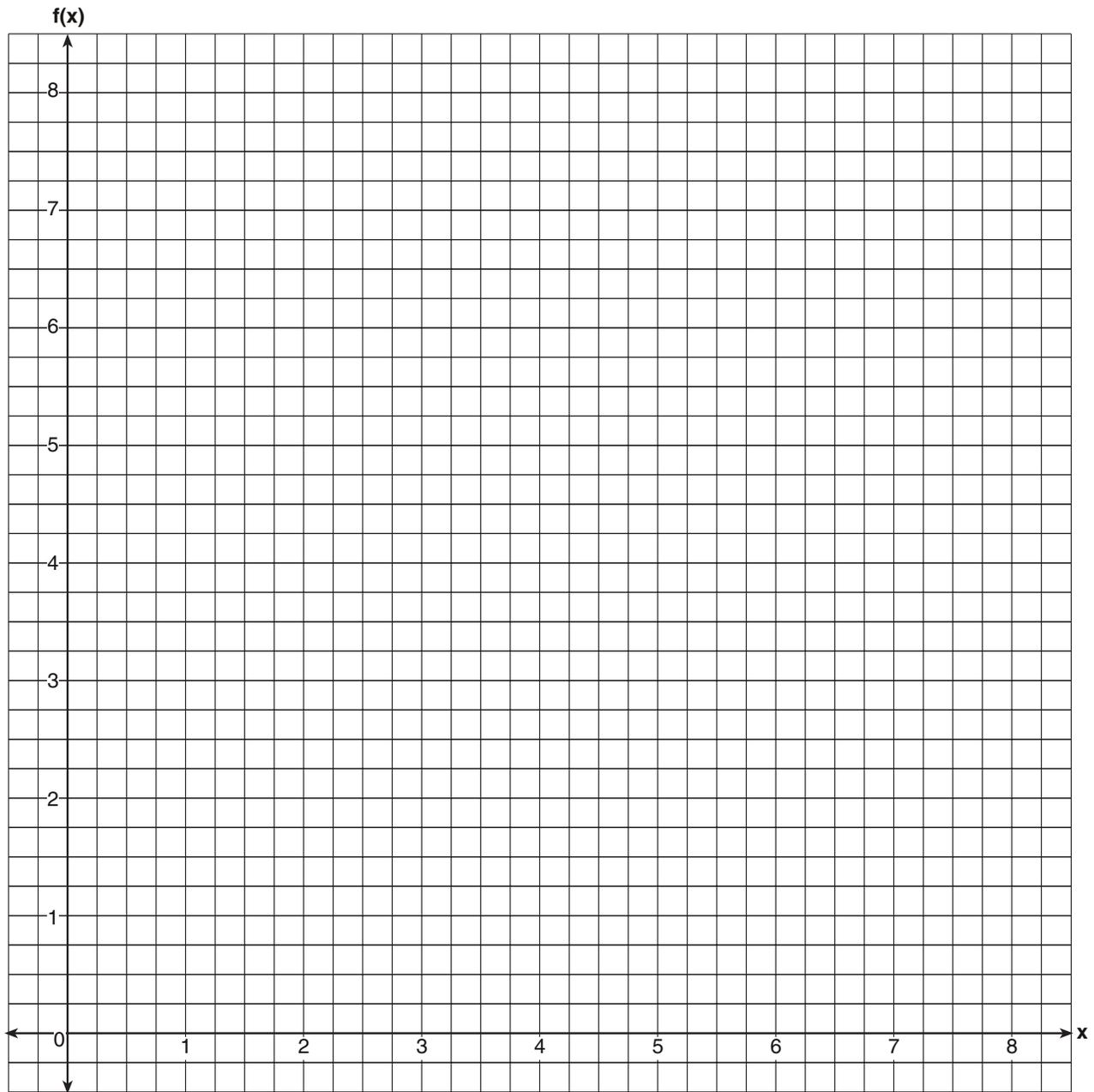
27 A wooden frame is to be constructed in the form of an isosceles trapezoid, with diagonals acting as braces to strengthen the frame. The sides of the frame each measure 5.30 feet, and the longer base measures 12.70 feet. If the angles between the sides and the longer base each measure 68.4° , find the length of one brace to the *nearest tenth of a foot*.

28 A homeowner wants to increase the size of a rectangular deck that now measures 15 feet by 20 feet, but building code laws state that a homeowner cannot have a deck larger than 900 square feet. If the length and the width are to be increased by the same amount, find, to the *nearest tenth*, the maximum number of feet that the length of the deck may be increased in size legally.

29 Two parabolic arches are to be built. The equation of the first arch can be expressed as $y = -x^2 + 9$, with a range of $0 \leq y \leq 9$, and the second arch is created by the transformation $T_{7,0}$. On the accompanying set of axes, graph the equations of the two arches. Graph the line of symmetry formed by the parabola and its transformation and label it with the proper equation.



30 Draw $f(x) = 2x^2$ and $f^{-1}(x)$ in the interval $0 \leq x \leq 2$ on the accompanying set of axes. State the coordinates of the points of intersection.



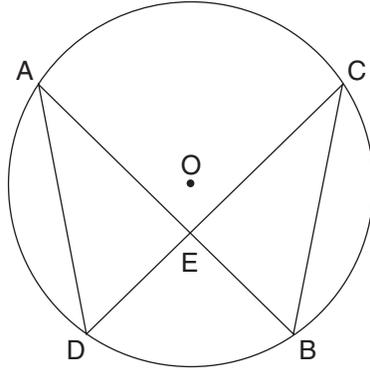
31 In the interval $0^\circ \leq A < 360^\circ$, solve for all values of A in the equation $\cos 2A = -3 \sin A - 1$.

32 Point P lies outside circle O , which has a diameter of \overline{AOC} . The angle formed by tangent \overline{PA} and secant \overline{PBC} measures 30° . Sketch the conditions given above and find the number of degrees in the measure of minor arc CB .

Part IV

Answer all questions in this part. Each correct answer will receive 6 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [12]

- 33 Given: chords \overline{AB} and \overline{CD} of circle O intersect at E , an interior point of circle O ; chords \overline{AD} and \overline{CB} are drawn.



Prove: $(AE)(EB) = (CE)(ED)$

34 The 1999 win-loss statistics for the American League East baseball teams on a particular date is shown in the accompanying chart.

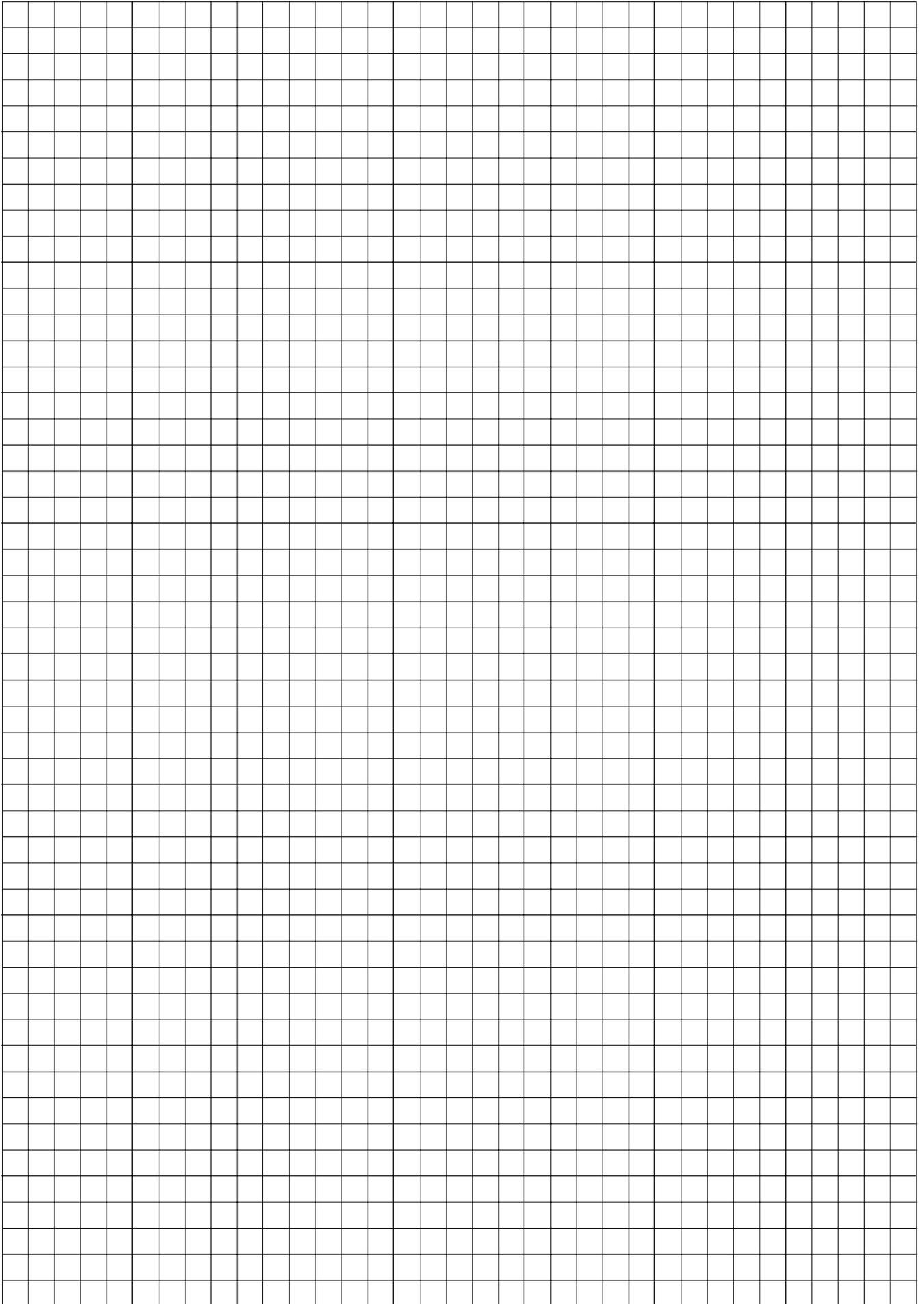
	W	L
New York	52	34
Boston	49	39
Toronto	47	43
Tampa Bay	39	49
Baltimore	36	51

Find the mean for the number of wins, \bar{W} , and the mean for the number of losses, \bar{L} , and determine if the point (\bar{W}, \bar{L}) is a point on the line of best fit. Justify your answer.

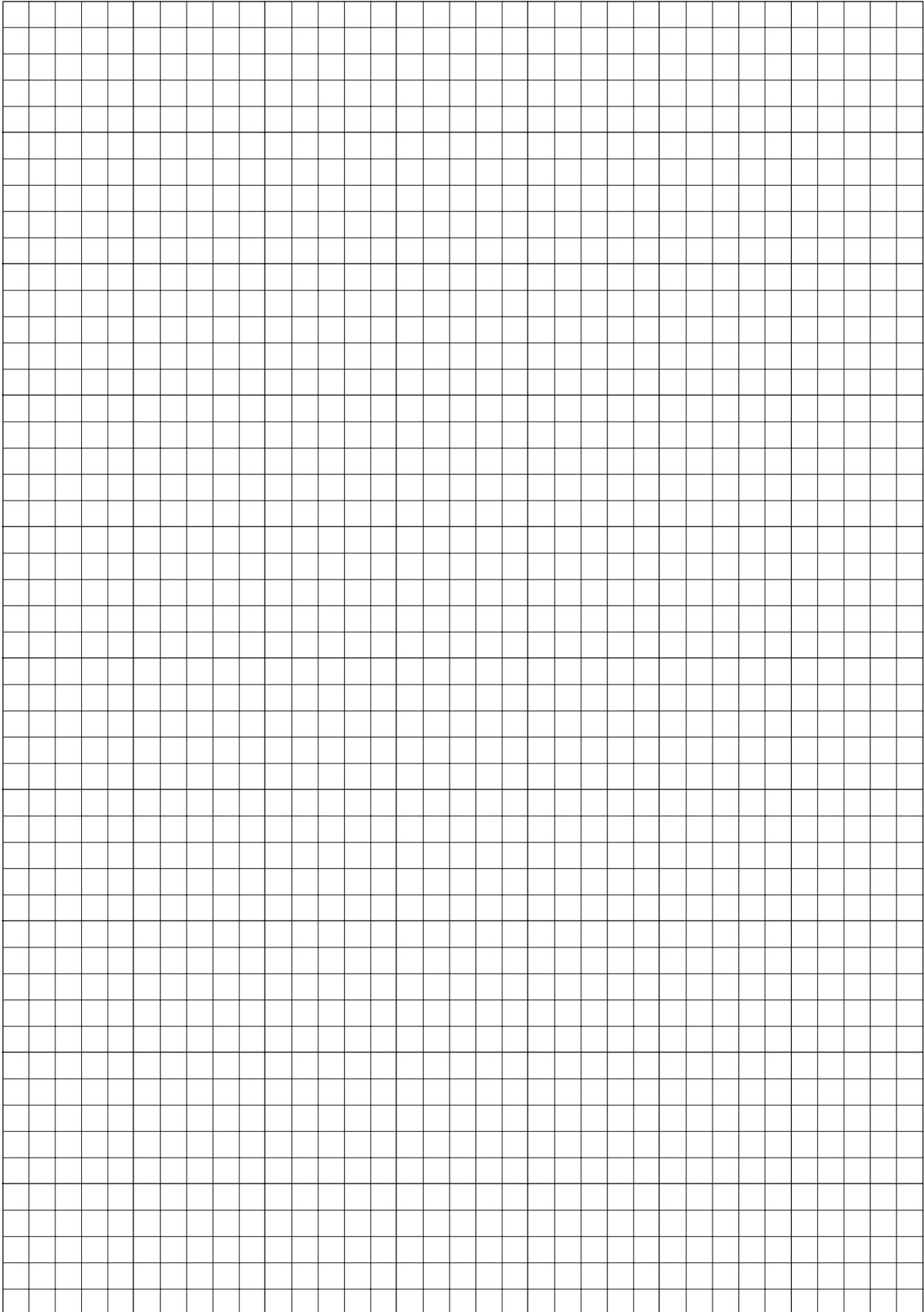
Scrap Graph Paper — This sheet will *not* be scored.

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MATHEMATICS B

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ANSWER SHEET

Pupil Sex: Male Female Grade

Teacher School

Your answers to Part I should be recorded on this answer sheet.

Part I

Answer all 20 questions in this part.

- 1 6 11 16
2 7 12 17
3 8 13 18
4 9 14 19
5 10 15 20

Your answers for Parts II, III, and IV should be written in the test booklet.

The declaration below should be signed when you have completed the examination.

I do hereby affirm, at the close of this examination, that I had no unlawful knowledge of the questions or answers prior to the examination and that I have neither given nor received assistance in answering any of the questions during the examination.

Signature

Tear Here

